

Fifth Annual French Complex Systems Summer School
Institut des Systèmes Complexes, Paris Ile-de-France, July 4-16, 2011

A Tour of Complex Systems

René Doursat

<http://iscpif.fr/~doursat>



**INSTITUT
DES SYSTÈMES COMPLEXES**



Instructor

René Doursat

➤ Experience

- Fmr. Director, ISC-PIF / Researcher, Ecole Polytechnique (CREA), 2006-
- Visiting Assistant Professor, University of Nevada, Reno, 2004-2006
- *Senior Software Engineer & Architect, Paris and San Francisco, 1995-2004*
- Research Associate, Ecole Polytechnique (CREA), Paris, 1996-1997
- Postdoctoral Fellow, Ruhr-Universität Bochum, Germany, 1991-1995

➤ Education

- HDR Sciences pour l'ingénieur, Université Paris 6 (UPMC), 2010
- Ph.D. in applied math (computational neuroscience), Université Paris 6, 1991
- M.S. in physics, Ecole Normale Supérieure, Paris, 1987

➤ Research interests

- computational modeling and simulation of complex systems, especially neural, biological and social, which can foster novel principles and applications in ICT
- self-organization of *reproducible* and *programmable* structures in (a) large-scale spiking neural dynamics, (b) developmental artificial life, (c) multi-agent networks

Course Contents

- **What this course is about** (dense preview, will be repeated)
 - ✓ an *exploration* of various complex systems *objects*:
 - cellular automata, pattern formation, swarm intelligence, complex networks, spatial communities, structured morphogenesis
 - ✓ and their common *questions*:
 - emergence, self-organization, positive feedback, decentralization, between simple and disordered, “more is different”, adaptation & evolution
 - ✓ by interactive *experimentation* (using NetLogo),
 - ✓ introducing *practical* complex systems *modeling* and simulation
 - ✓ from a *computational* viewpoint, in contrast with a “mathematical” one (i.e., formal or numerical resolution of symbolic equations),
 - ✓ based on discrete *agents* moving in discrete or quasi-continuous space, and *interacting* with each other and their environment

A Tour of Complex Systems

1. Introduction
2. A Complex Systems Sampler
3. Commonalities
4. NetLogo Tutorial

A Tour of Complex Systems

1. Introduction

- a. What are complex systems?
- b. A vast archipelago
- c. Computational modeling

2. A Complex Systems Sampler

3. Commonalities

4. NetLogo Tutorial

A Tour of Complex Systems

1. Introduction

a. What are complex systems?

- *Few agents*
- *Many agents*
- *CS in this course*

b. A vast archipelago

c. Computational modeling

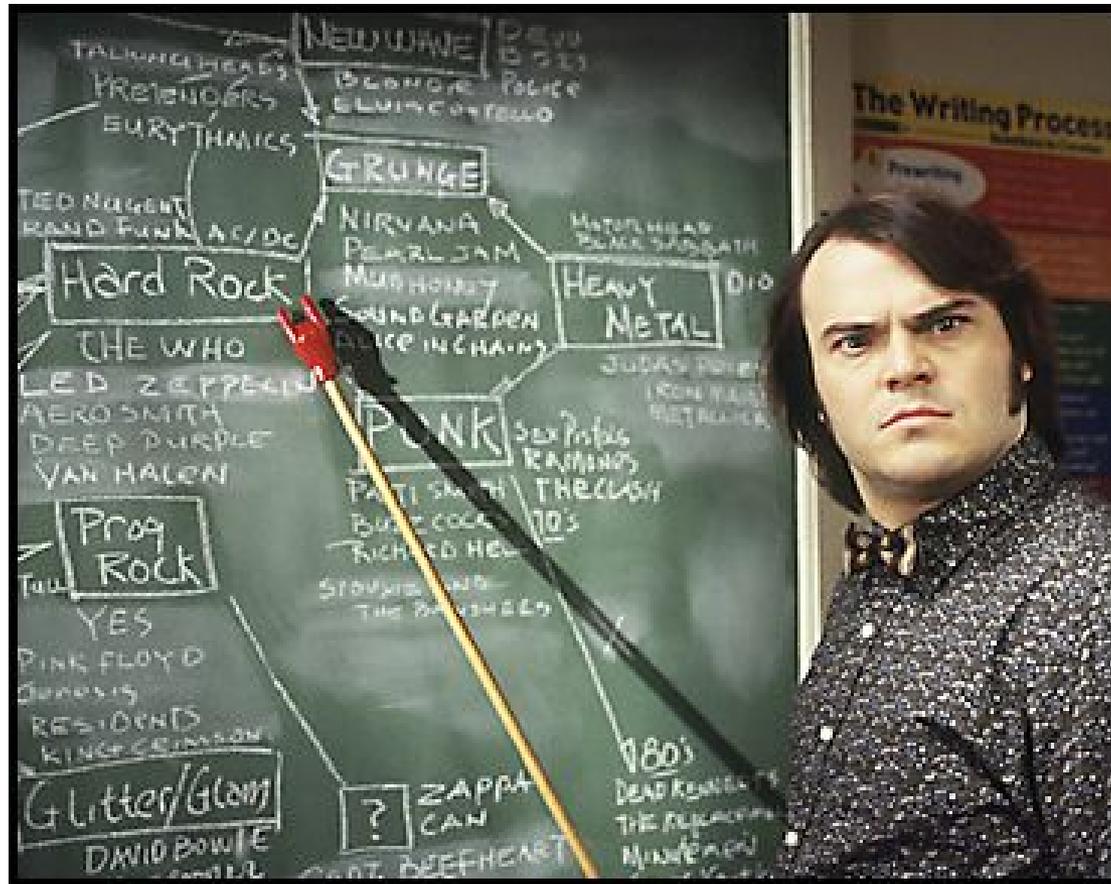
2. A Complex Systems Sampler

3. Commonalities

4. NetLogo Tutorial

1. Introduction — a. What are complex systems?

➤ Any ideas?



The School of Rock (2003)
Jack Black, Paramount Pictures

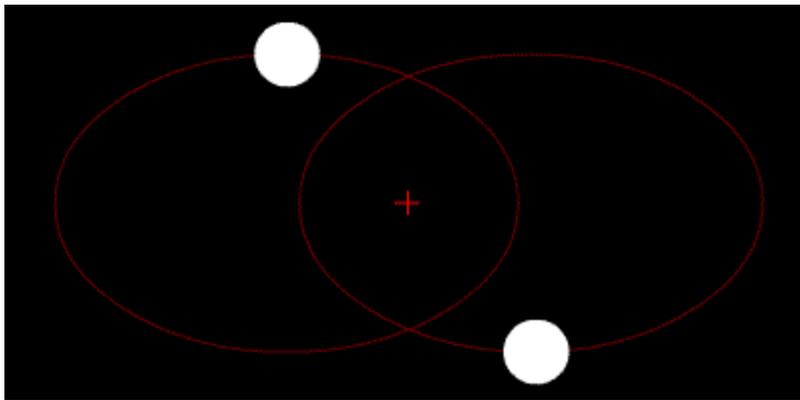
1. Introduction — a. What are complex systems?

➤ Few agents, “simple” emergent behavior

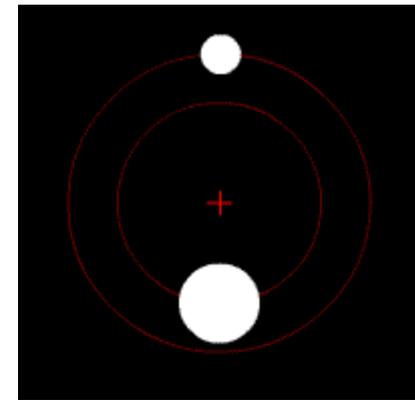
→ *ex: two-body problem*

- ✓ fully solvable and *regular* trajectories for inverse-square force laws (e.g., gravitational or electrostatic)

$$\left\{ \begin{array}{l} \mathbf{F}_{12}(\mathbf{x}_1, \mathbf{x}_2) = m_1 \ddot{\mathbf{x}}_1 \quad (\text{Equation 1}) \\ \mathbf{F}_{21}(\mathbf{x}_1, \mathbf{x}_2) = m_2 \ddot{\mathbf{x}}_2 \quad (\text{Equation 2}) \end{array} \right.$$



Two bodies with similar mass
Wikimedia Commons



Two bodies with different mass
Wikimedia Commons

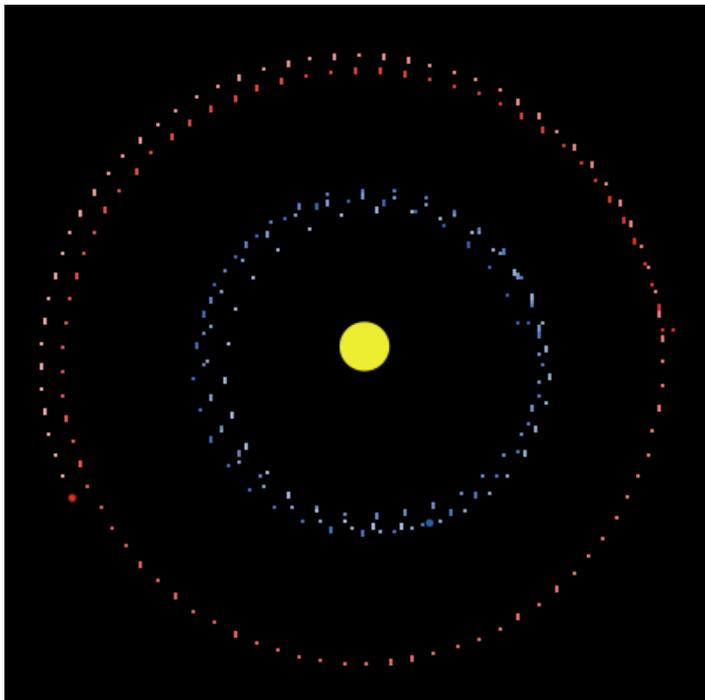
1. Introduction — a. What are complex systems?

➤ Few agents, **complex emergent behavior**

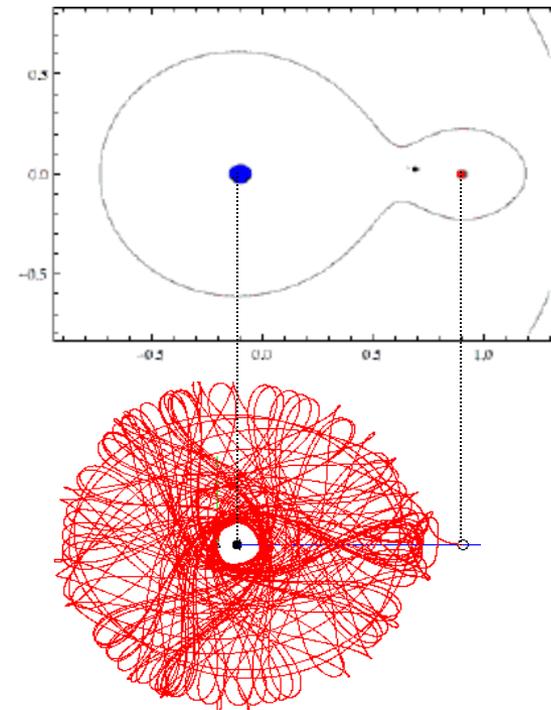
→ *ex: three-body problem*

- ✓ generally no exact mathematical solution (even in “restricted” case $m_1 \ll m_2 \approx m_3$): must be solved numerically → **chaotic** trajectories

NetLogo model: /Chemistry & Physics/Mechanics/Unverified



Transit orbit of the planar circular restricted problem
Scholarpedia: Three Body Problem & Joachim Köppen Kiel's applet



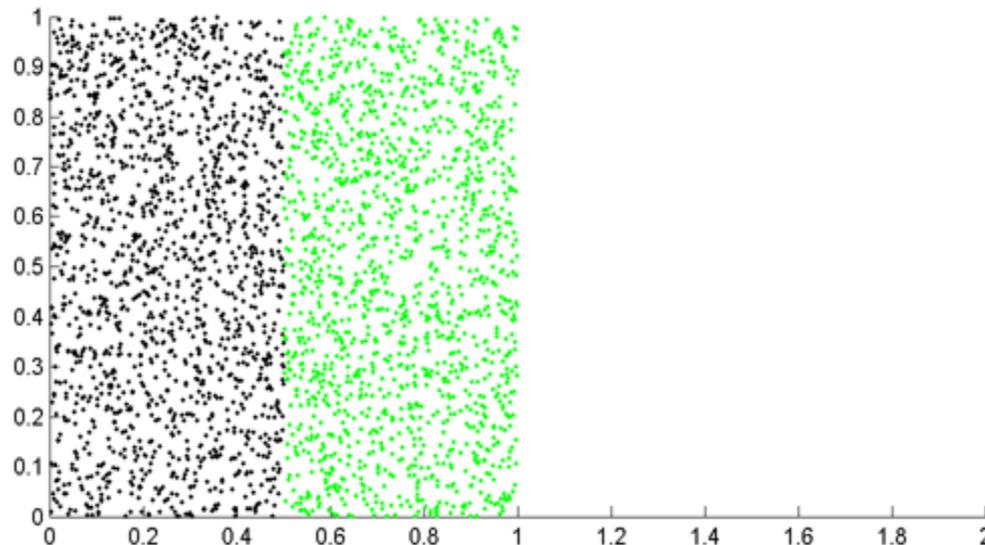
1. Introduction — a. What are complex systems?

➤ Few agents, complex emergent behavior

→ *ex: more chaos (baker's/horseshoe maps, logistic map, etc.)*

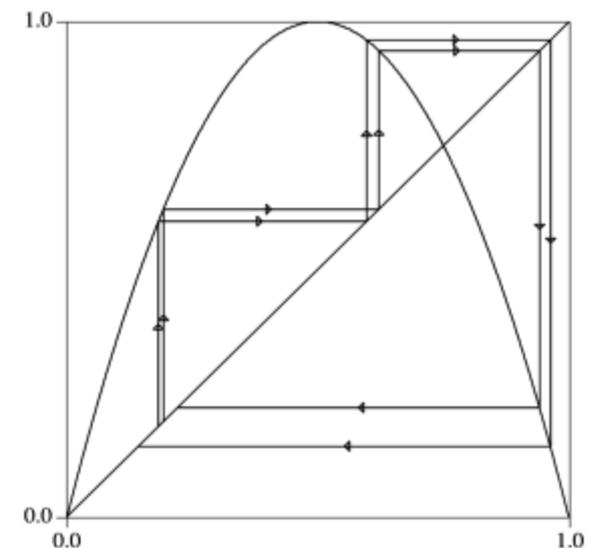
✓ *chaos* generally means a **bounded, deterministic** process that is **aperiodic** and **sensitive on initial conditions** → small fluctuations create large variations ("butterfly effect")

✓ even one-variable iterative functions: $x_{n+1} = f(x_n)$ can be "complex"



Baker's transformation

Craig L. Zirbel, Bowling Green State University, OH



Logistic map

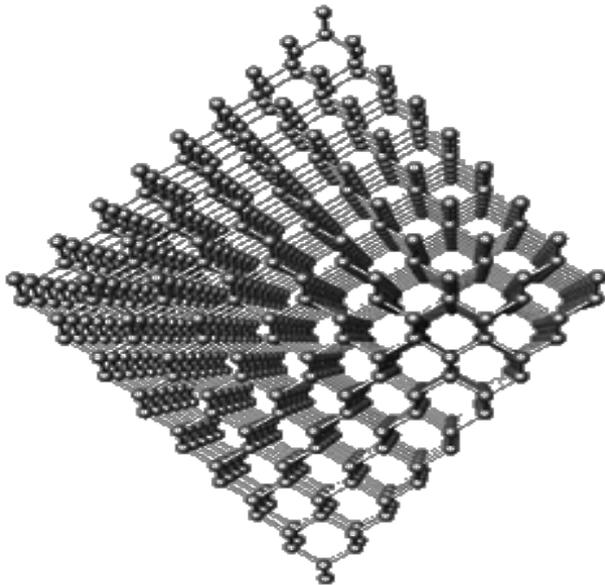
1. Introduction — a. What are complex systems?

➤ Many agents, simple rules, “simple” emergent behavior

→ *ex: crystal and gas (covalent bonds or electrostatic forces)*

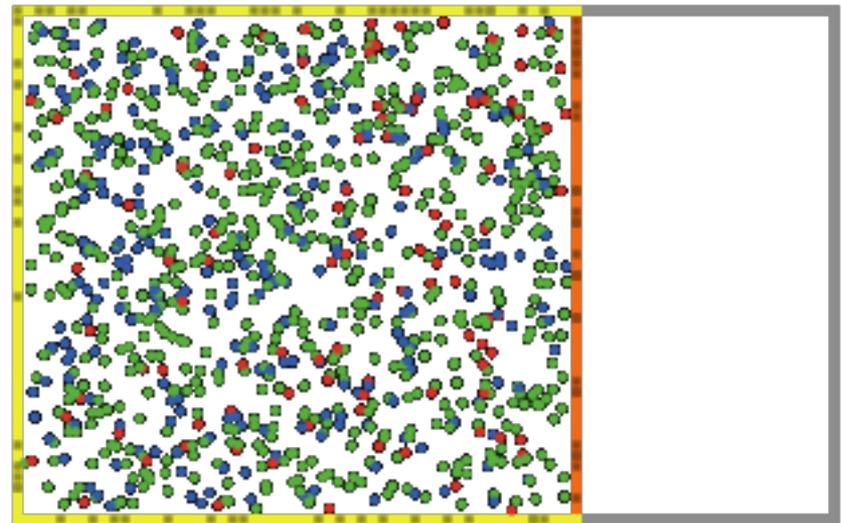
✓ either highly ordered, *regular* states (crystal)

✓ or disordered, random, statistically *homogeneous* states (gas):
a few global variables (P, V, T) suffice to describe the system



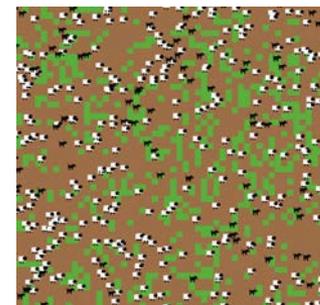
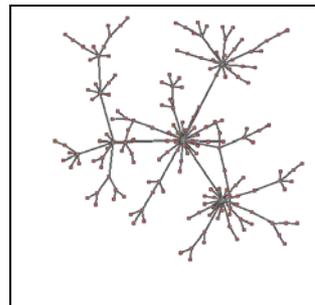
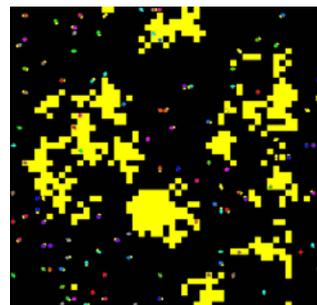
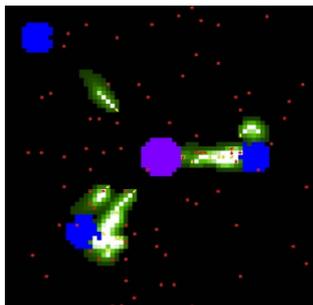
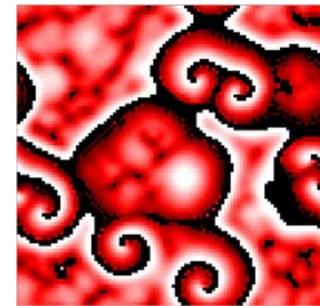
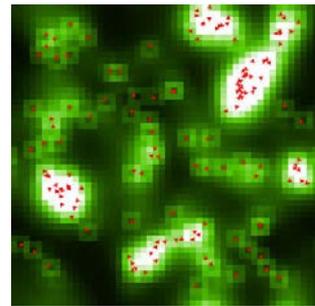
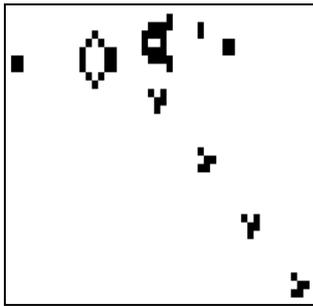
Diamond crystal structure
Tonci Balic-Zunic, University of Copenhagen

NetLogo model: /Chemistry & Physics/GasLab Isothermal Piston



1. Introduction — a. What are complex systems?

- **Many agents, simple rules, complex emergent behavior**
 - *ex: cellular automata, pattern formation, swarm intelligence (insect colonies, neural networks), complex networks, spatial communities*
 - ✓ the “clichés” of complex systems: a major part of this course and NetLogo models



1. Introduction – a. What are complex systems?

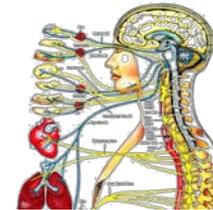
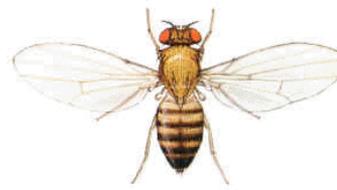
➤ Many agents, complicated rules, complex emergent behavior

→ *natural ex: organisms (cells), societies (individuals + techniques)*

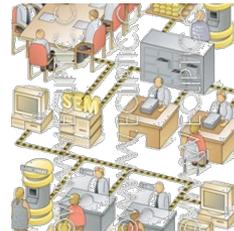
✓ agent rules become more “complicated”, e.g., *heterogeneous* depending on the element’s *type* and/or *position* in the system

✓ behavior is also complex but, paradoxically, can become more *controllable*, e.g., *reproducible* and *programmable*

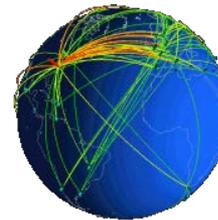
biological development & evolution



termite mounds



companies



techno-networks

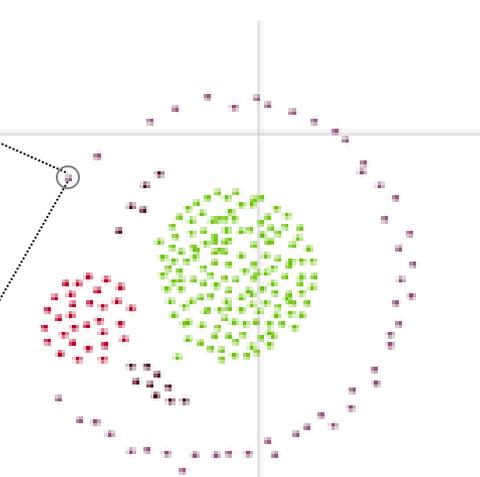


cities

1. Introduction – a. What are complex systems?

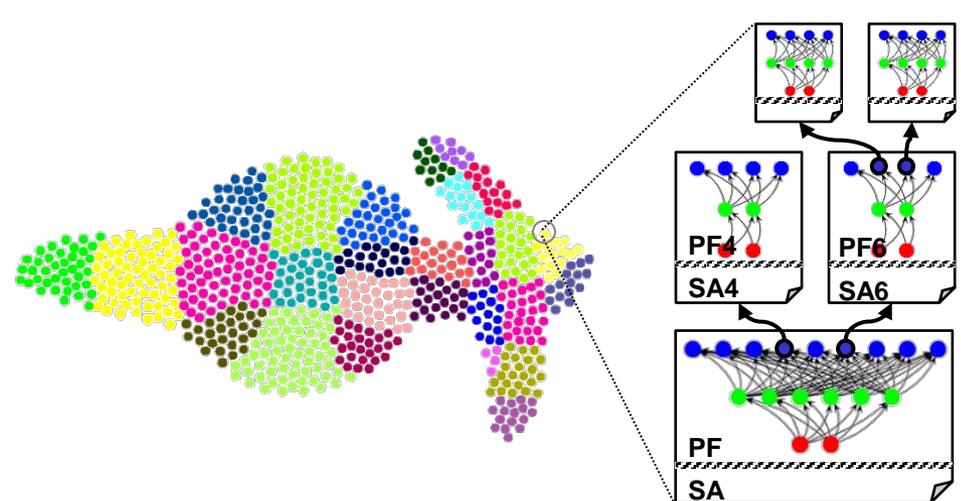
- **Many agents, complicated rules, complex emergent behavior**
 - *ex: self-organized "artificial life": swarm chemistry, morphogenesis*
 - ✓ in *swarm chemistry* (Sayama 2007), mixed self-propelled particles with different flocking parameters create nontrivial formations
 - ✓ in *embryomorphic engineering* (Doursat 2006), cells contain the same genetic program, but differentiate and self-assemble into specific shapes

Name	Min	Max
R^i	0	300
V_n^i	0	20
V_m^i	0	40
c_1^i	0	1
c_2^i	0	1
c_3^i	0	100
c_4^i	0	0.5
c_5^i	0	1



Swarm chemistry

Hiroki Sayama, Binghamton University SUNY



Embryomorphic engineering

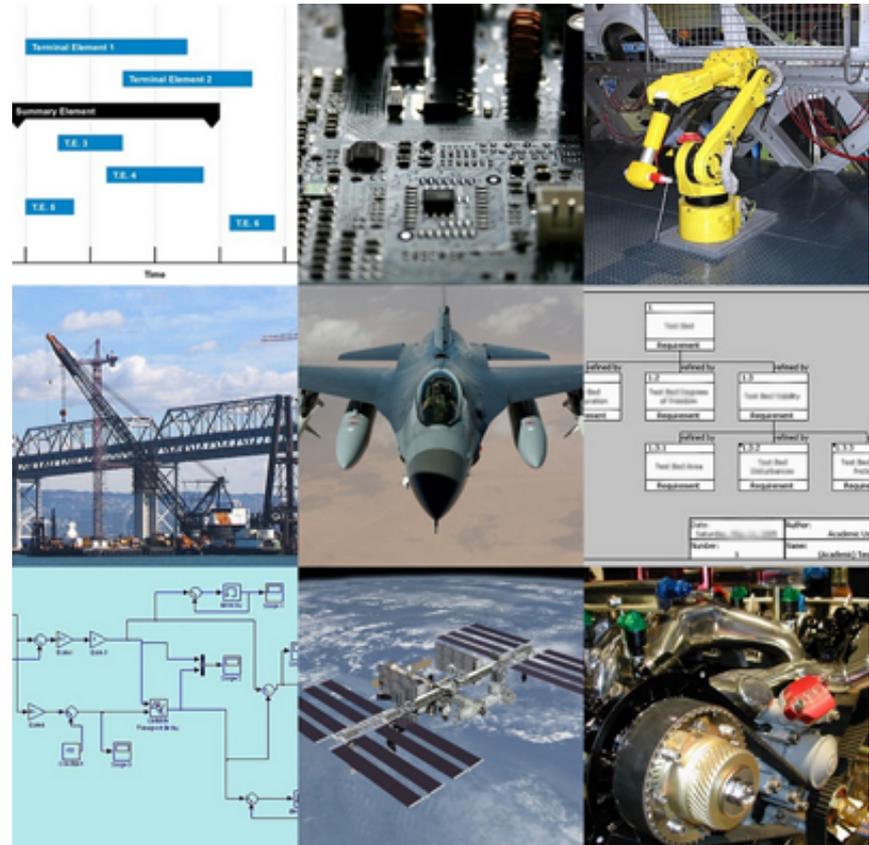
René Doursat, Institut des Systèmes Complexes, Paris

1. Introduction — a. What are complex systems?

➤ Many agents, complicated rules, "deterministic" behavior

→ *classical engineering: electronics, machinery, aviation, civil construction*

- ✓ artifacts composed of a immense number of parts
- ✓ yet still designed globally to behave in a limited and **predictable** (reliable, controllable) number of ways — "I don't want my aircraft to be creatively emergent in mid-air"
- ✓ not "complex" systems in the sense of:
 - little decentralization
 - no emergence
 - no self-organization



Systems engineering

Wikimedia Commons, http://en.wikipedia.org/wiki/Systems_engineering

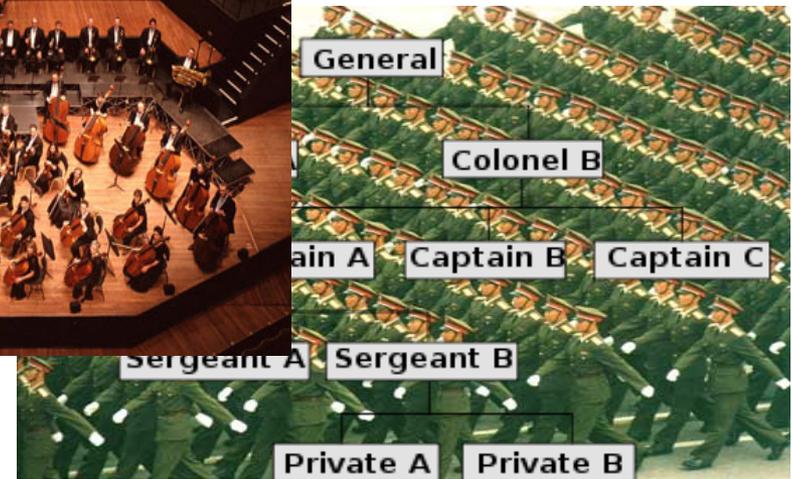
1. Introduction — a. What are complex systems?

➤ Many agents, complicated rules, "centralized" behavior

→ *spectators, orchestras, military, administrations*

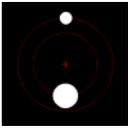
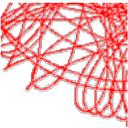
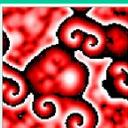
✓ people reacting similarly and/or simultaneously to cues/orders coming from a *central cause*: event, leader, plan

✓ **hardly "complex" systems**: little decentralization, little emergence, little self-organization



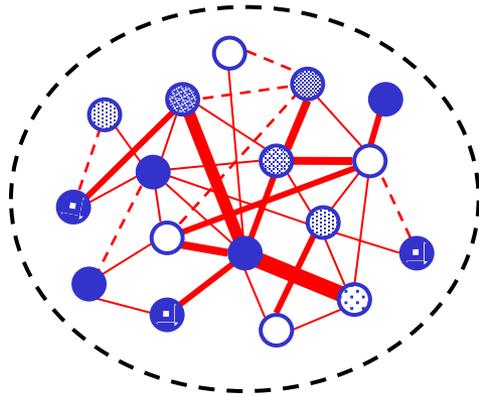
1. Introduction – a. What are complex systems?

➤ Recap: complex systems in this course

Category	<i>Agents / Parts</i>	<i>Local Rules</i>	<i>Emergent Behavior</i>	A "Complex System"?
 2-body problem	<i>few</i>	<i>simple</i>	<i>"simple"</i>	<i>NO</i>
 3-body problem, low-D chaos	<i>few</i>	<i>simple</i>	<i>complex</i>	<i>NO – too small</i>
 crystal, gas	<i>many</i>	<i>simple</i>	<i>"simple"</i>	<i>NO – few params suffice to describe it</i>
 patterns, swarms, complex networks	<i>many</i>	<i>simple</i>	<i>"complex"</i>	<i>YES – but mostly random and uniform</i>
 structured morphogenesis	<i>many</i>	<i>complicated</i>	<i>complex</i>	<i>YES – reproducible and heterogeneous</i>
 machines, crowds with leaders	<i>many</i>	<i>complicated</i>	<i>deterministic/centralized</i>	<i>COMPLICATED – not self-organized</i>

1. Introduction — a. What are complex systems?

➤ Complex systems in this course

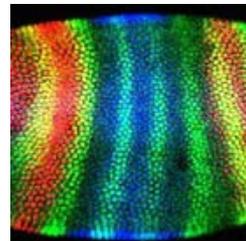


- large number of elementary agents interacting **locally**
- (more or less) simple individual agent behaviors creating a complex **emergent, self-organized** behavior
- *decentralized dynamics: no master blueprint or grand architect*

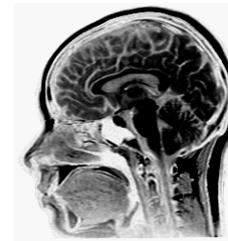
✓ **physical, biological, technical, social** systems (natural or artificial)



pattern formation
○ = matter



biological development
○ = cell

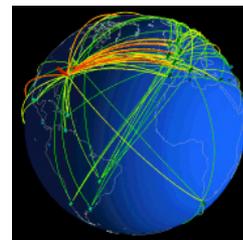


the brain & cognition
○ = neuron

insect colonies
○ = ant



Internet & Web
○ = host/page



social networks
○ = person



1. Introduction — a. What are complex systems?

Physical pattern formation: Convection cells



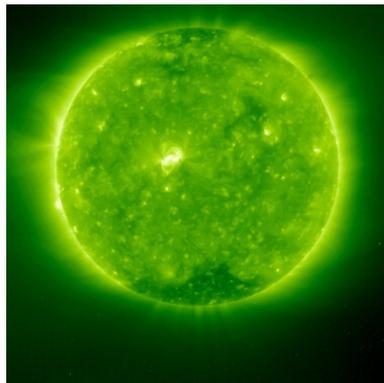
Rayleigh-Bénard convection cells in liquid heated uniformly from below
(Scott Camazine, <http://www.scottcamazine.com>)



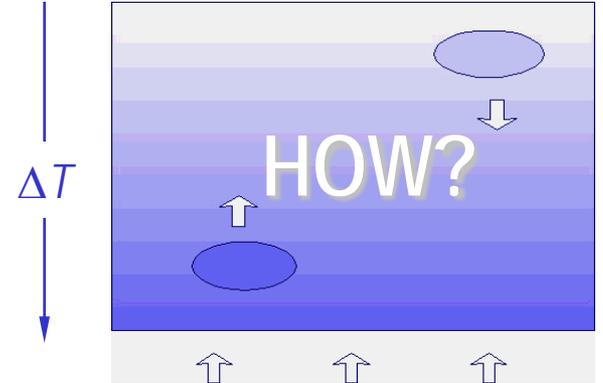
Convection cells in liquid (detail)
(Manuel Velarde, Universidad Complutense, Madrid)



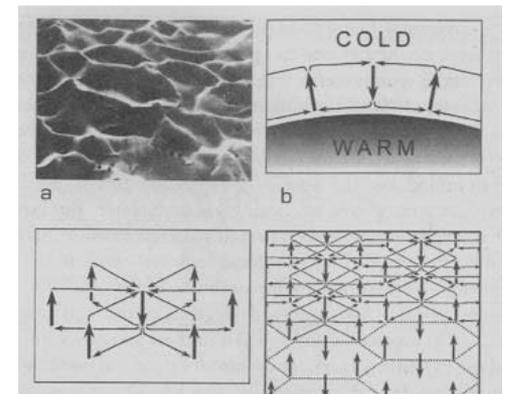
Sand dunes
(Scott Camazine, <http://www.scottcamazine.com>)



Solar magnetoconvection
(Steven R. Lantz, Cornell Theory Center, NY)



Schematic convection dynamics
(Arunn Narasimhan, Southern Methodist University, TX)

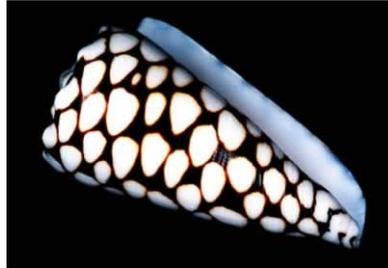


Hexagonal arrangement of sand dunes
(Solé and Goodwin, "Signs of Life", Perseus Books)

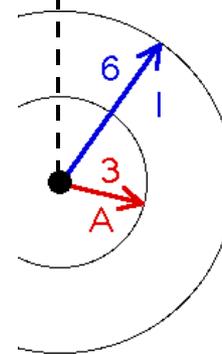
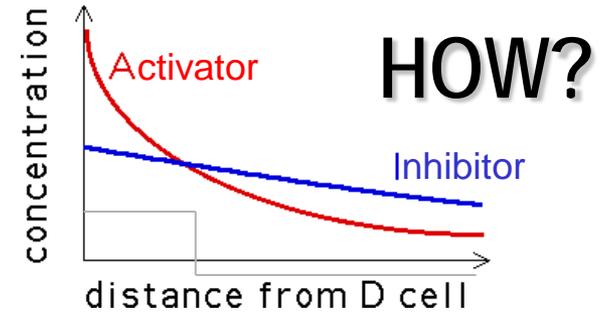
➤ thermal convection, due to temperature gradients, creates stripes and tilings at multiple scales, from tea cups to geo- and astrophysics

1. Introduction — a. What are complex systems?

Biological pattern formation: Animal colors



Mammal fur, seashells, and insect wings
(Scott Camazine, <http://www.scottcamazine.com>)

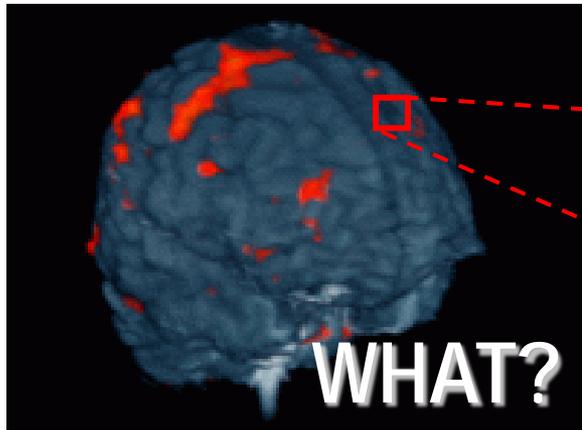


NetLogo fur coat simulation, after David Young's model of fur spots and stripes
(Michael Frame & Benoit Mandelbrot, Yale University)

- animal patterns (for warning, mimicry, attraction) can be caused by pigment cells trying to copy their nearest neighbors but differentiating from farther cells

1. Introduction – a. What are complex systems?

Spatiotemporal synchronization: Neural networks

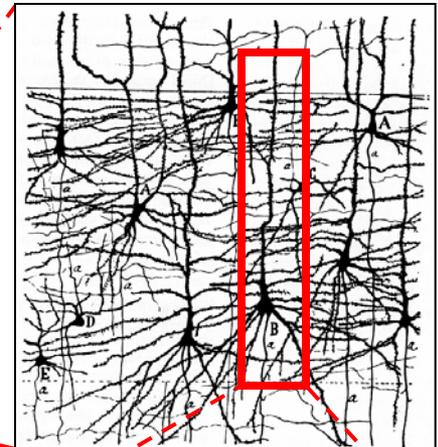
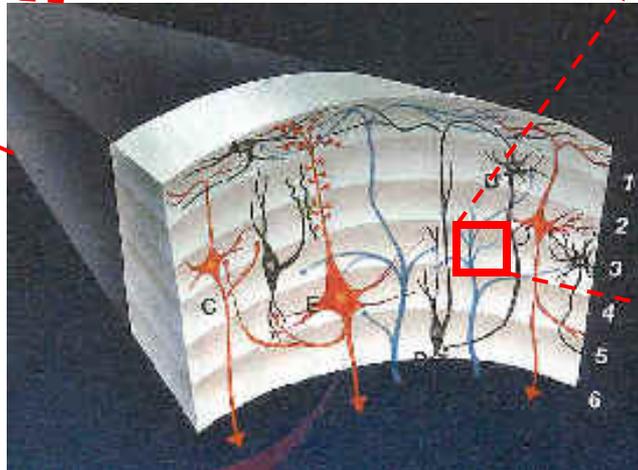


Animation of a functional MRI study
(J. Ellermann, J. Strupp, K. Ugurbil, U Minnesota)

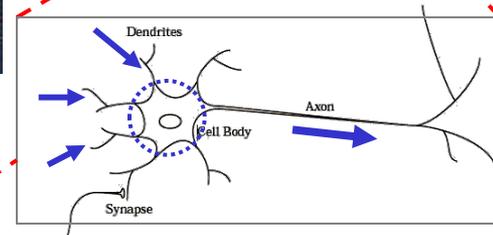
- the brain constantly generates patterns of activity ("the mind")
- they emerge from 100 billion neurons that exchange electrical signals via a dense network of contacts

HOW?

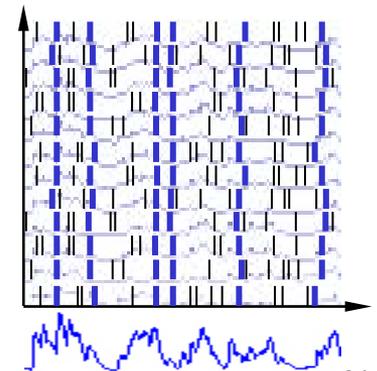
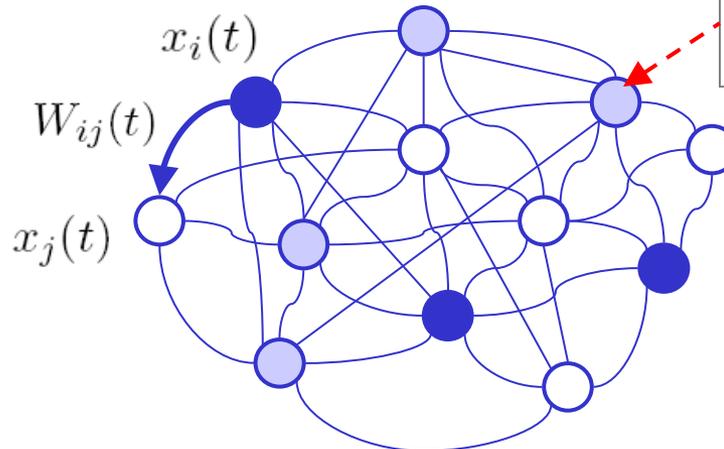
Cortical layers



Pyramidal neurons & interneurons
(Ramón y Cajal 1900)



Schematic neural network



1. Introduction — a. What are complex systems?

Swarm intelligence: Insect colonies (ant trails, termite mounds)



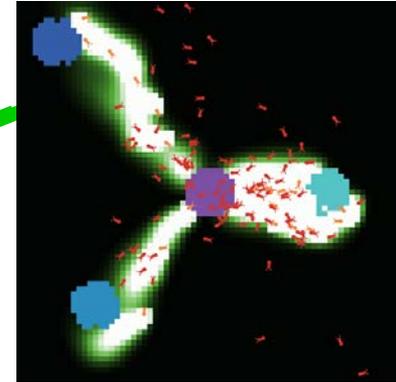
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<http://picasaweb.google.com/tridentoriginal/Ghana>



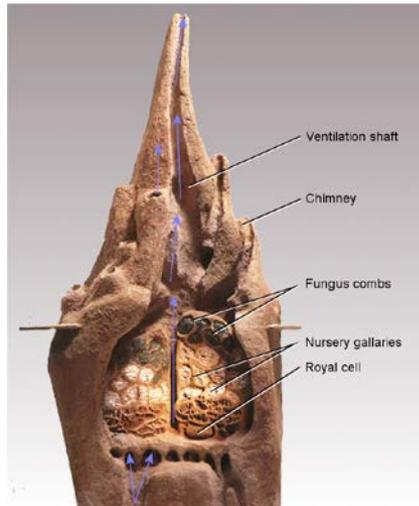
Harvester ant
(Deborah Gordon, Stanford University)



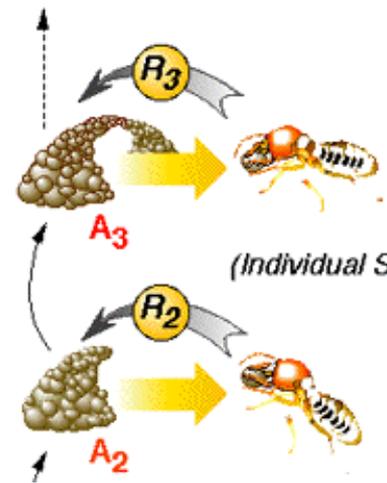
HOW?



Termite mound
(J. McLaughlin, Penn State University)



<http://cas.bellarmine.edu/tietjen/TermiteMound%20CS.gif>



Termite stigmergy
(after Paul Grassé; from Solé and Good "Signs of Life", Perseus Books)

➤ ants form trails by following and reinforcing each other's pheromone path

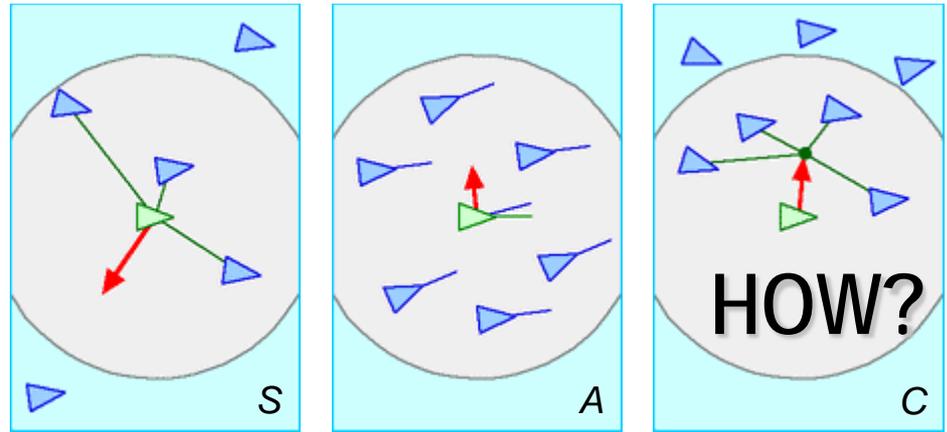
➤ termite colonies build complex mounds by "stigmergy"

1. Introduction — a. What are complex systems?

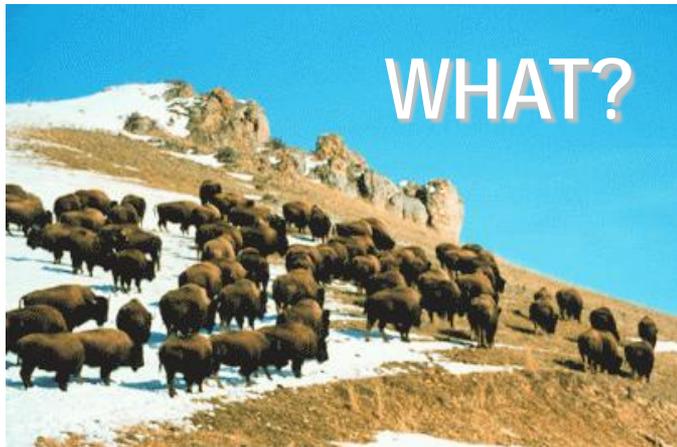
Collective motion: flocking, schooling, herding



Fish school
(Eric T. Schultz, University of Connecticut)

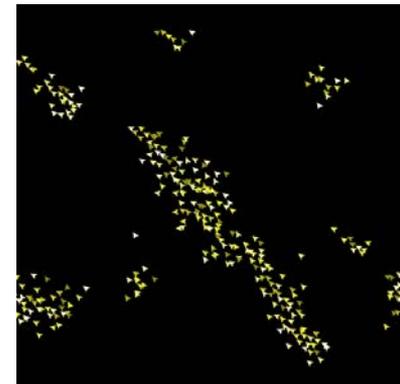


Separation, alignment and cohesion
(“Boids” model, Craig Reynolds, <http://www.red3d.com/cwr/boids>)



Bison herd
(Center for Bison Studies, Montana State University, Bozeman)

- coordinated collective movement of dozens or 1000s of individuals (confuse predators, close in on prey, improve motion efficiency, etc.)

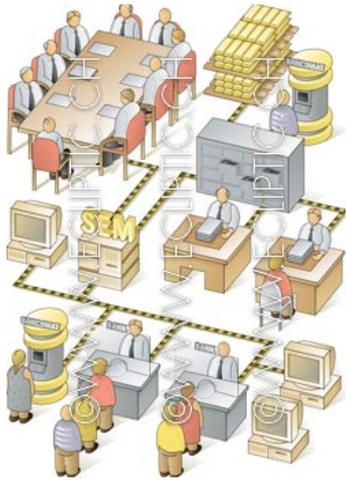


- each individual adjusts its position, orientation and speed according to its nearest neighbors

1. Introduction — a. What are complex systems?

Complex networks and morphodynamics: human organizations

organizations



(Thomas Thü Hürlimann, <http://ecliptic.ch>)

urban dynamics



SimCity (<http://simcitysocieties.ea.com>)



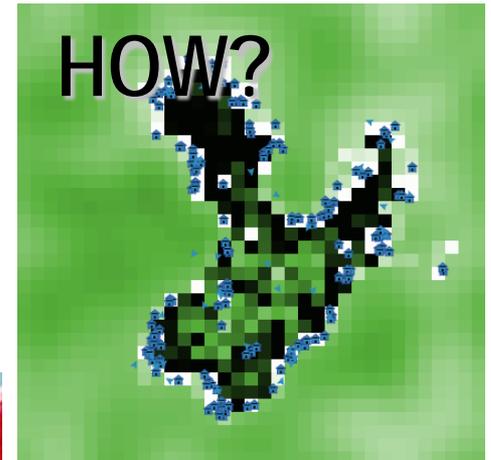
techno-social networks



NSFNet Internet (w2.eff.org)

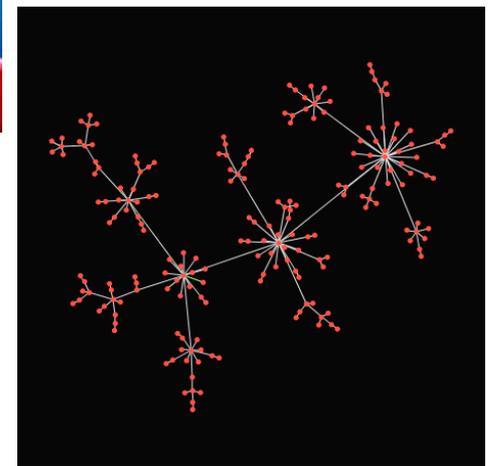
René Doursat: "A Tour of Complex Systems"

cellular automata model



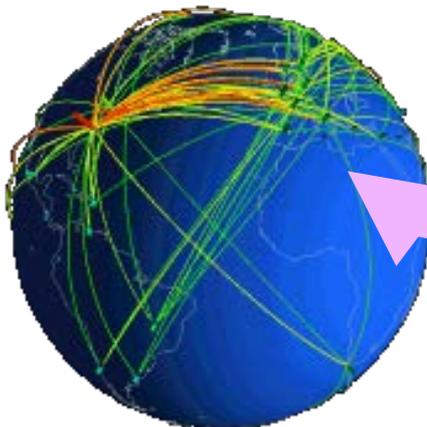
NetLogo urban sprawl simulation

"scale-free" network model

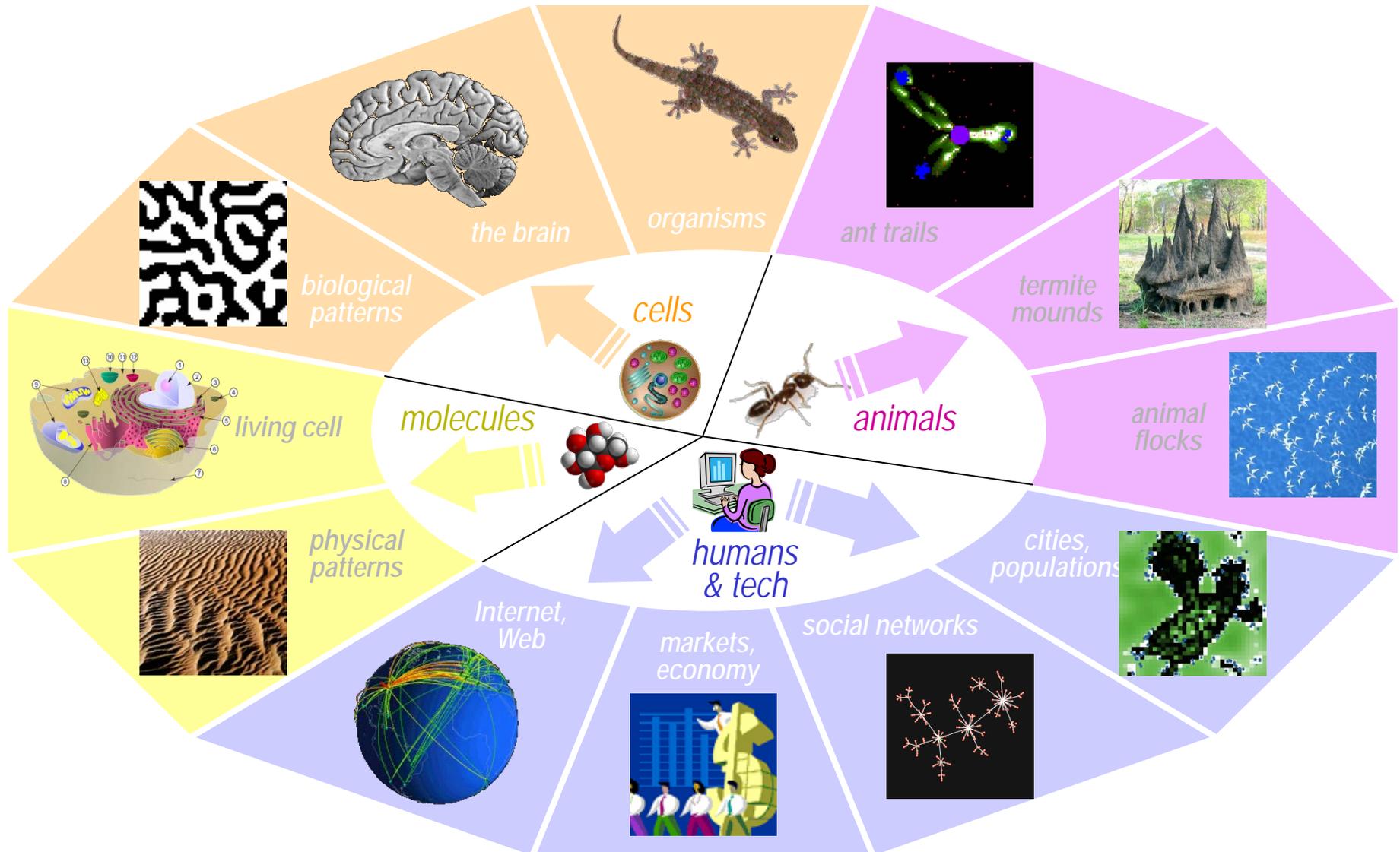


NetLogo preferential attachment simulation

global connectivity

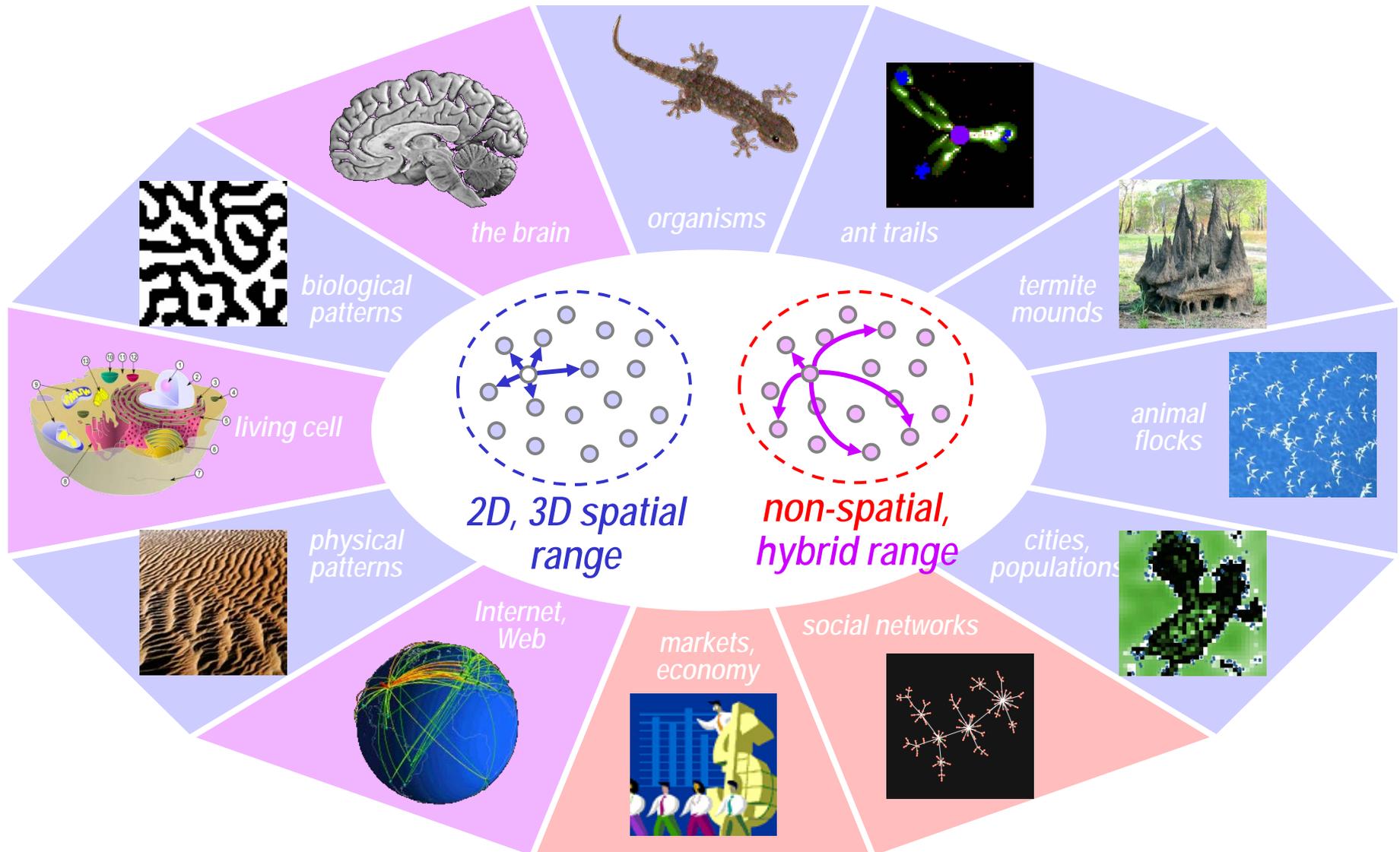


1. Introduction – a. What are complex systems? *Categories of complex systems by agents*



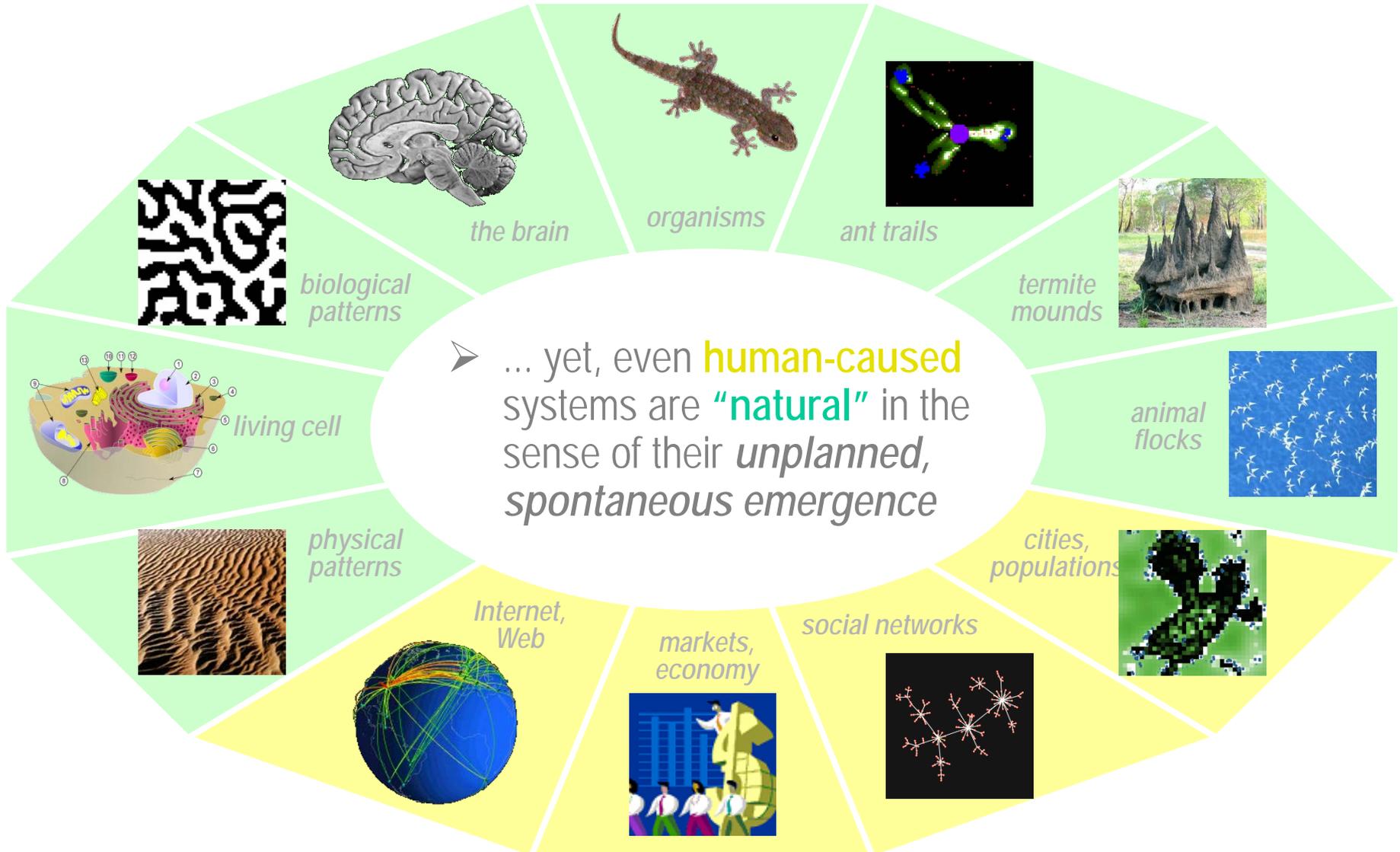
1. Introduction — a. What are complex systems?

Categories of complex systems by range of interactions



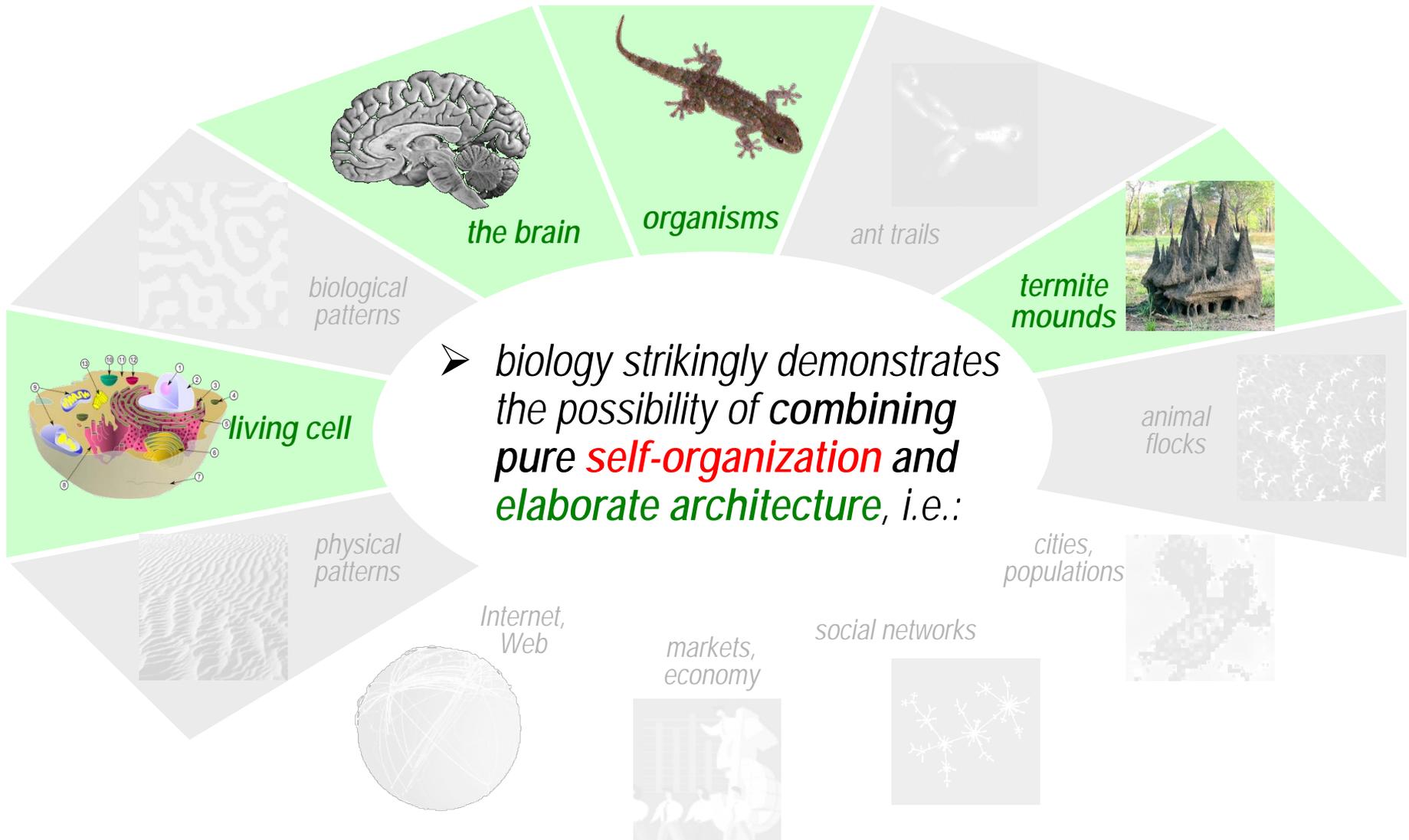
1. Introduction – a. What are complex systems?

Natural and human-caused categories of complex systems



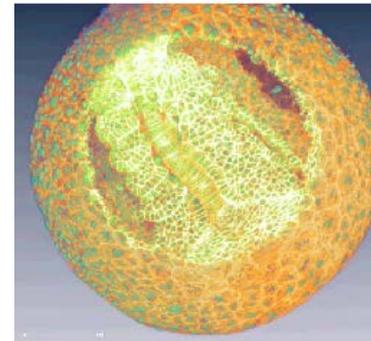
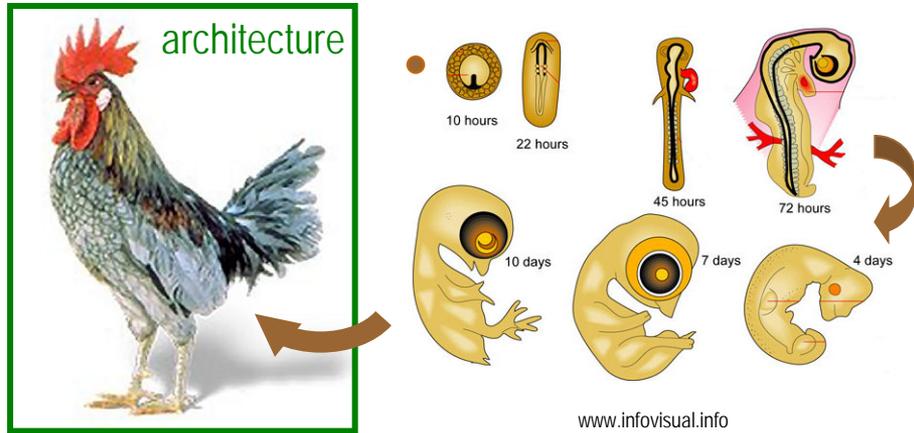
1. Introduction — a. What are complex systems?

“Simple/random” vs. *architected* natural complex systems



1. Introduction — a. What are complex systems?

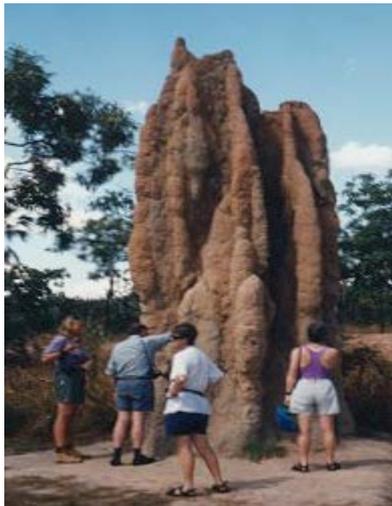
➤ Ex: Morphogenesis – Biological development



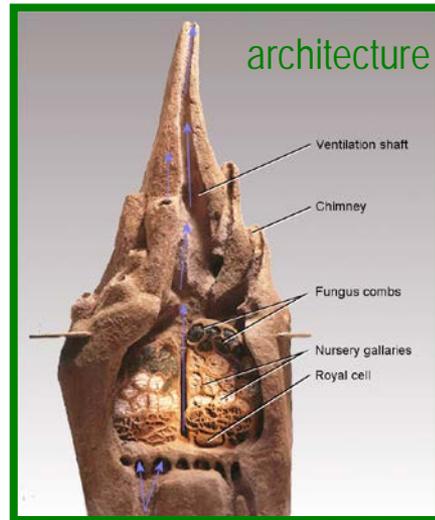
Nadine Peyri ras, Paul Bourguine et al. (Embryomics & BioEmergences)

➤ cells build sophisticated organisms by division, genetic differentiation and biomechanical self-assembly

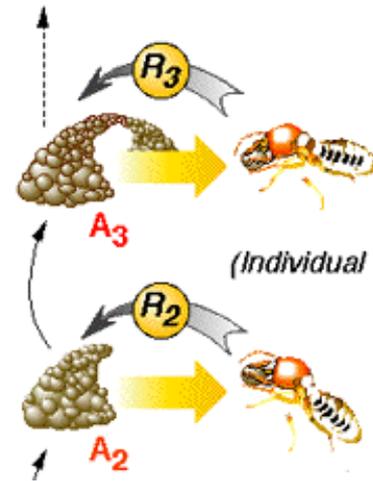
➤ Ex: Swarm intelligence – Termite mounds



Termite mound
(J. McLaughlin, Penn State University)



<http://cas.bellarmine.edu/tietjen/TermiteMound%20CS.gif>



Termite stigmergy

(after Paul Grass ; from Sol  and Goodwin, "Signs of Life", Perseus Books)

➤ termite colonies build sophisticated mounds by "stigmergy" = loop between modifying the environment and reacting differently to these modifications

1. Introduction — a. What are complex systems?

Human superstructures are "natural" CS

by their unplanned, spontaneous emergence and adaptivity...

geography: cities, populations

people: social networks

wealth: markets, economy

technology: Internet, Web

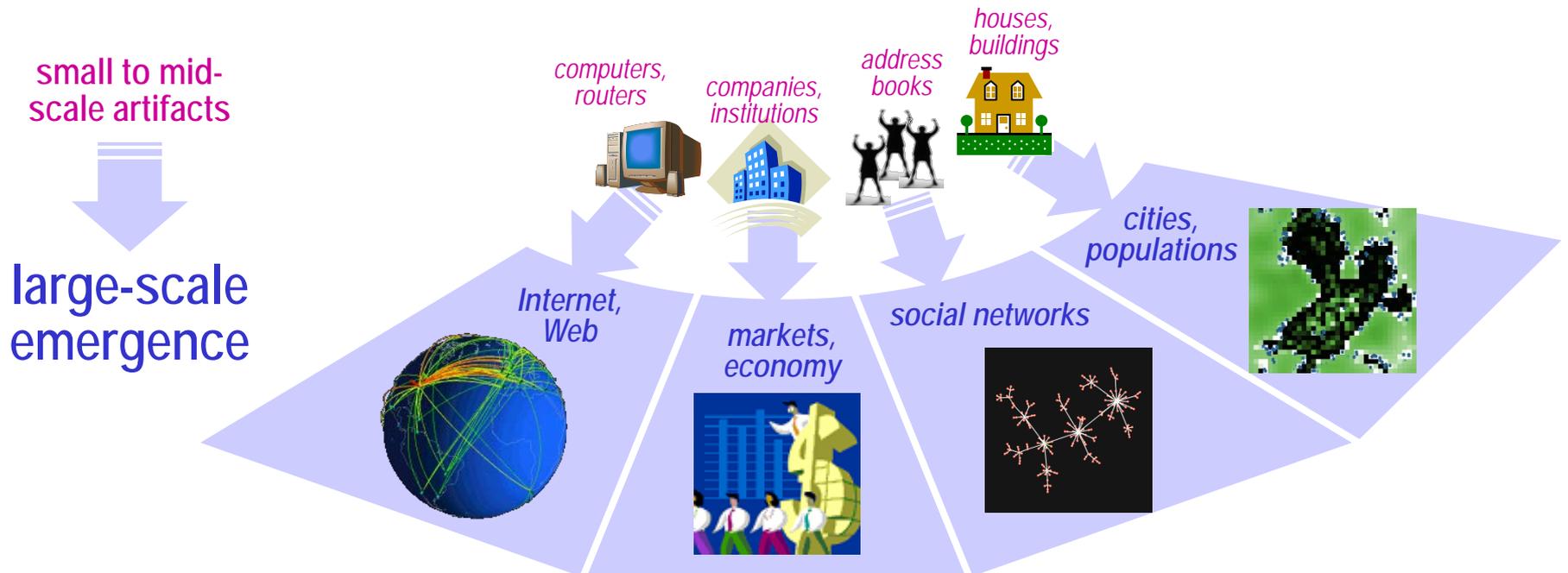
... arising from a multitude of traditionally designed artifacts

← houses, buildings

← address books

← companies, institutions

← computers, routers



A Tour of Complex Systems

1. Introduction

a. What are complex systems?

b. A vast archipelago

- *Related disciplines*
- *Big questions × big objects*
- *Science ↔ engineering links*

c. Computational modeling

2. A Complex Systems Sampler

3. Commonalities

4. NetLogo Tutorial

1. Introduction — b. A vast archipelago

➤ Precursor and neighboring disciplines

complexity: measuring the length to describe, time to build, or resources to run, a system

adaptation: change in typical functional regime of a system

systems sciences: holistic (non-reductionist) view on interacting parts

dynamics: behavior and activity of a system over time

multitude, statistics: large-scale properties of systems

- ✓ different families of disciplines *focus* on different aspects
- ✓ (naturally, they intersect a lot: don't take this taxonomy too seriously)

1. Introduction — b. A vast archipelago

➤ Precursor and neighboring disciplines

complexity: measuring the length to describe, time to build, or resources to run, a system

- information theory (Shannon; entropy)
- computational complexity (P, NP)
- Turing machines & cellular automata

→ *Toward a unified "complex systems" science and engineering?*

dynamics: behavior and activity of a system over time

- nonlinear dynamics & chaos
- stochastic processes
- systems dynamics (macro variables)

adaptation: change in typical functional regime of a system

- evolutionary methods
- genetic algorithms
- machine learning

systems sciences: holistic (non-reductionist) view on interacting parts

- systems theory (von Bertalanffy)
- systems engineering (design)
- cybernetics (Wiener; goals & feedback)
- control theory (negative feedback)

multitude, statistics: large-scale properties of systems

- graph theory & networks
- statistical physics
- agent-based modeling
- distributed AI systems

1. Introduction — b. A vast archipelago

- Sorry, there is no general “complex systems science” or “complexity theory”...
 - ✓ there are a lot of theories and results in related disciplines (“systems theory”, “computational complexity”, etc.), yet
 - such generic names often come from one researcher with one particular view
 - there is no unified viewpoint on *complex systems*, especially *autonomous*
 - in fact, there is not even any agreement on their *definition*
 - ✓ we are currently dealing with an intuitive set of criteria, more or less shared by researchers, but still hard to formalize and quantify:
 - complexity
 - emergence
 - self-organization
 - multitude / decentralization
 - adaptation, etc.

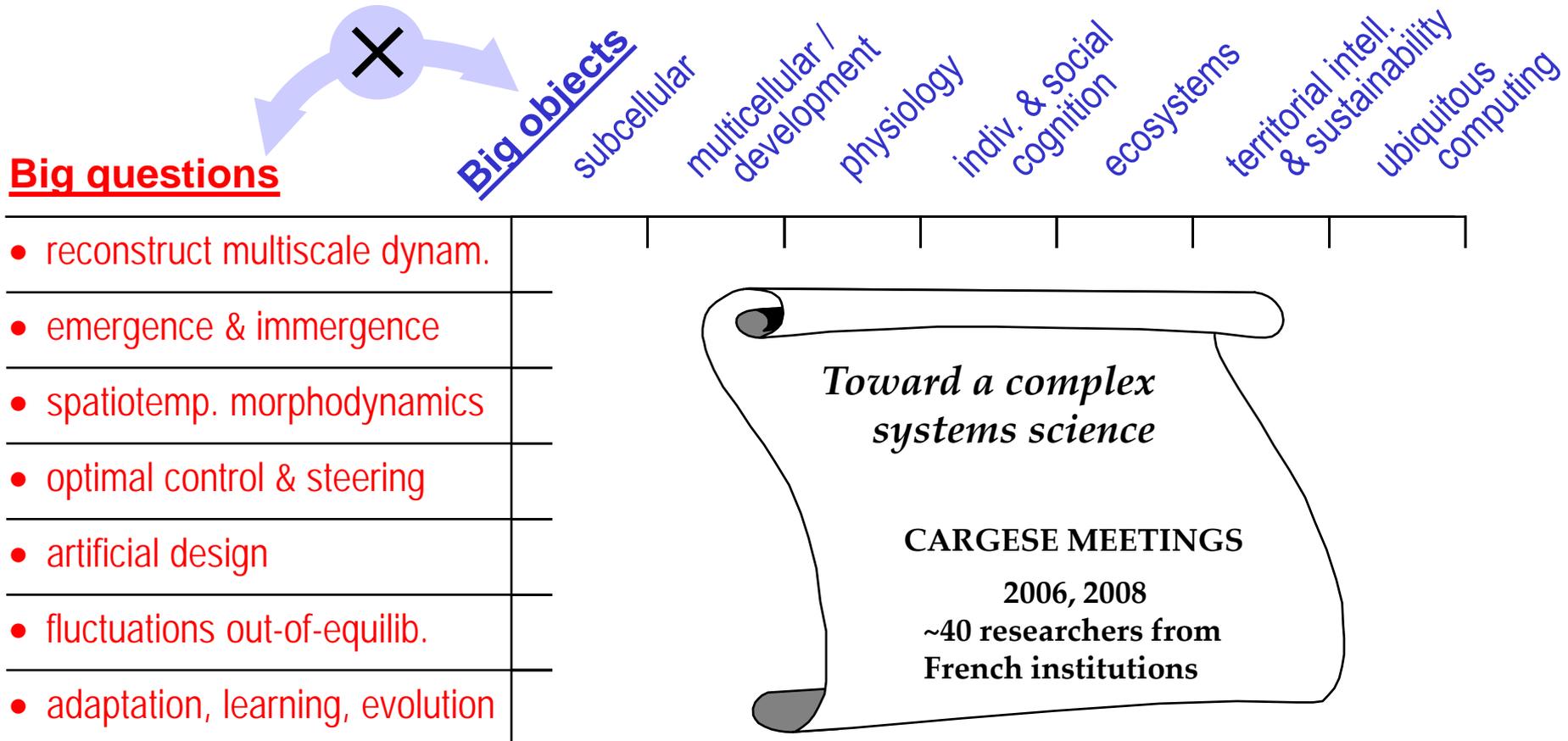


... but don't go packing yet!

1. Introduction – b. A vast archipelago

➤ The French “roadmap” toward complex systems science

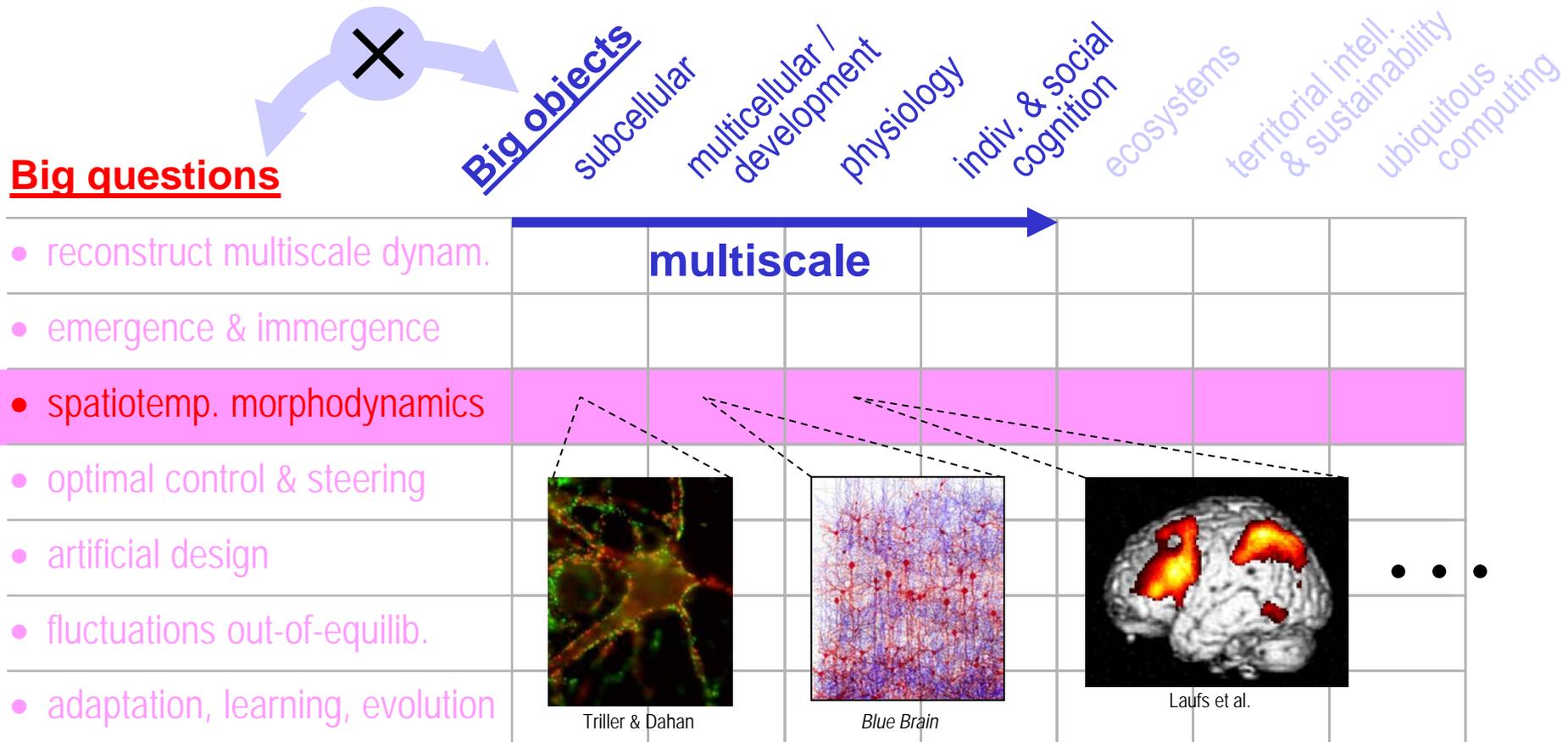
- ✓ another way to circumscribe complex systems is to list “big (horizontal) questions” and “big (vertical) objects”, and cross them



1. Introduction – b. A vast archipelago

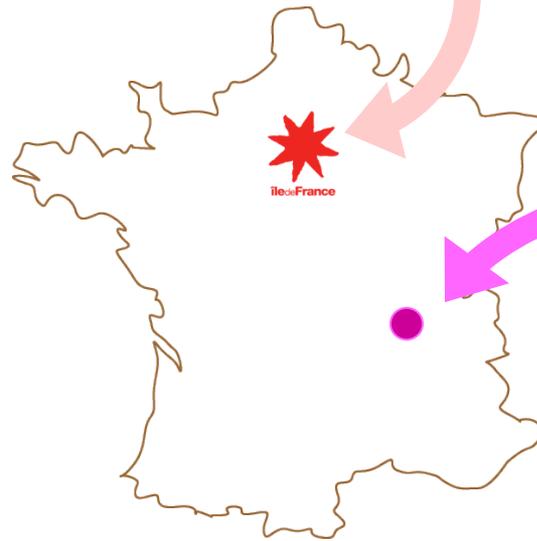
➤ The French “roadmap” toward complex systems science

- ✓ another way to circumscribe complex systems is to list “big (horizontal) questions” and “big (vertical) objects”, and cross them





INSTITUT DES SYSTÈMES COMPLEXES Paris Île-de-France



4th French Complex Systems
Summer School, 2010



Resident Researchers



Pierre Baudot

Information Theory - Adaptation - Topology - Thermodynamics of perception.

mathematical neuroscience



Romain Reuillon

High performance computing - Grid computing - Scientific workflows - Model exploration - Distributed stochastic simulations - Parallel pseudo-random number generation - Coffee maker.

high performance computing



René Doursat

Artificial development (self-assembly, pattern formation, spatial computing, evolutionary computation) - Mesoscopic neurodynamics (segmentation, schematization, categorization, perception, cognitive linguistics).

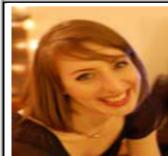
artificial life / neural computing



Jean-Baptiste Rouquier

Complex networks: communities, structure, dynamics. Links between fields. Large datasets. Cellular automata: model of complex systems, perturbation, asynchronism, robustness.

complex networks / cellular automata



Marie-Noëlle Comin

Urban systems, networks of cities, innovation, Europe, EU's Framework Programme for Research and Technological Development, converging technologies, NBIC (nanotechnology, biotechnology, information technology and cognitive science).

urban systems / innovation networks



Camilo Melani

Grid Computing, Bioemergences Platform (workflow), Morphodynamics reconstruction, Images processing algorithms.

embryogenesis



Francesco Ginelli

Nonequilibrium statistical mechanics (Active matter, collective motion, flocking, nonequilibrium wetting, directed percolation, long range interactions) - Dynamical system theory (Lyapunov exponents, Lyapunov vectors, synchronization, stable chaos, spatiotemporal chaos, structural stability, hyperbolicity).

statistical mechanics / collective motion



David Chavalarias

Web mining and Quantitative Epistemology - Cognitive economics and modelling of cultural dynamics - Collective discovery and scientific discovery.

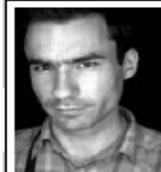
web mining / social intelligence



Ivan Junier

Bio-related: Genetic regulation - Cellular organization - DNA/chromatin modeling - -omics (Genomics, Transcriptomics, proteomics,...) - Condensed matter theory - Inference problems in statistical physics - Network analysis (topology, geometry) - Dynamical behaviors of complex systems. Statistical physics: Out-of equilibrium systems Thermodynamic description of small system

structural genomics



Srdjan Ostojic

Neuroscience théoriques - Spiking Neurons - Dynamiques Stochastiques-ques.

spiking neural dynamics



Taras Kowaliw

Evolutionary computation, artificial development, computer vision, visualization and electronic art.

computational evolution / development



Andrea Perna

Morphogenesis, Collective behavior, Spatial patterns, Spatial networks.

spatial networks / swarm intelligence



Telmo Menezes

Complex network analysis and simulation - Social networks - Evolutionary search for multi-agent models, Genetic programming applied to programmable networks - Bio-inspired algorithms.

social networks



Fernando Peruani

Biophysique - Active Matter - Complex Networks.

active matter / complex networks



Bivas Mitra

Peer-to-Peer networks, Blog networks, Complex networks, Statistical mechanics, Networks modeling, Optical networks, Wireless Internet.

peer-to-peer networks



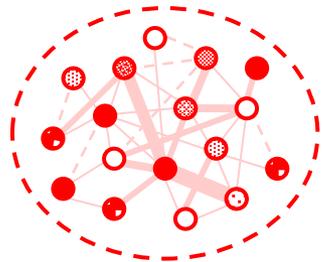
Francesco d'Ovidio

Applied nonlinear dynamics - Transport and mixing in geophysical flows - Interaction of physical and ecological processes in the ocean.

nonlinear dynamics / oceanography

1. Introduction — b. A vast archipelago

➤ The challenges of complex systems (CS) research



*CS science: understanding & modeling "natural" CS
(spontaneously emergent, including human-made)*

Transfers
▪ among systems

Exports

- decentralization
- autonomy, homeostasis
- learning, evolution

Imports

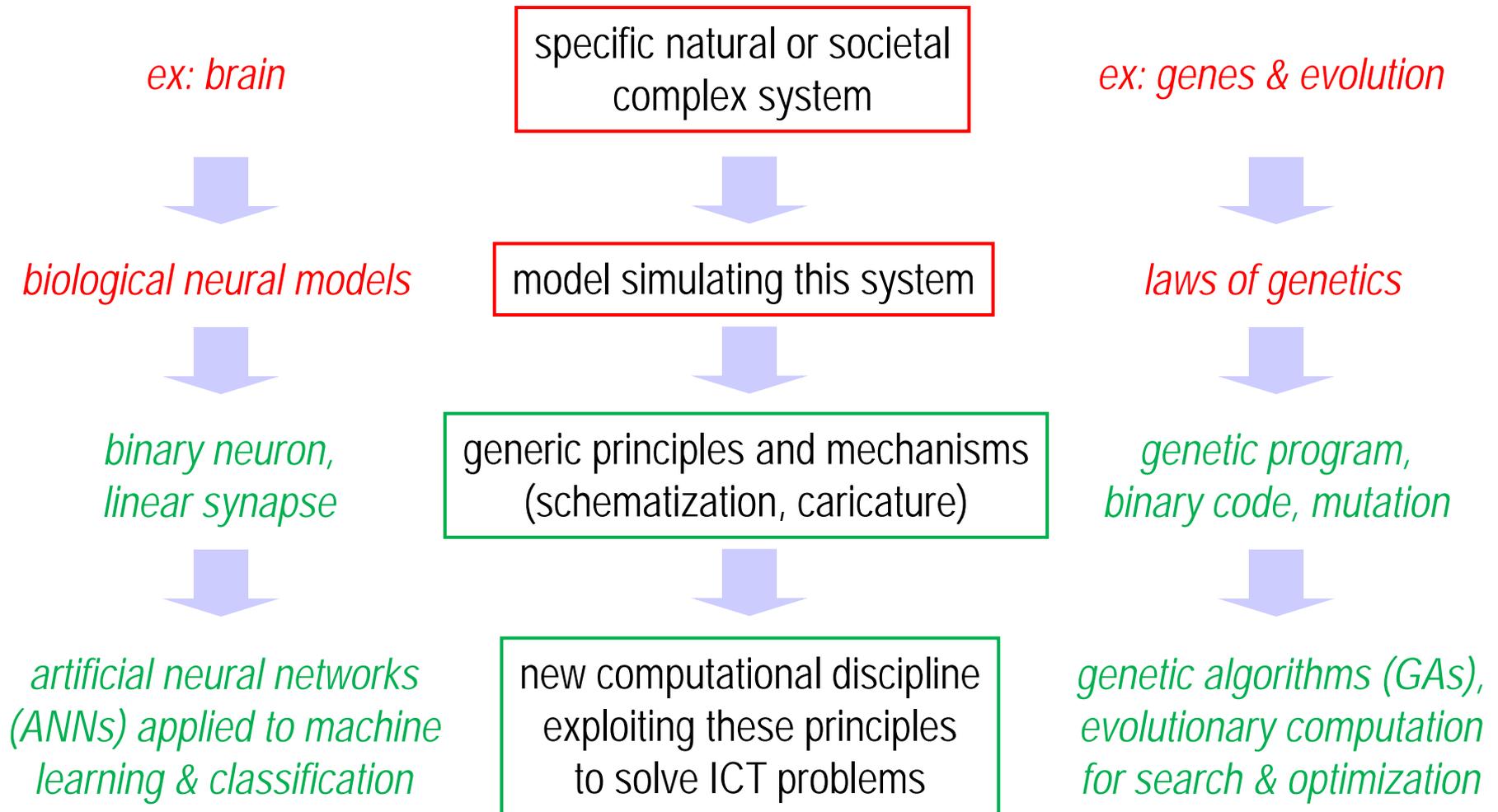
- observe, model
- control, harness
- design, use



*CS (ICT) engineering: designing a new generation of
"artificial/hybrid" CS (harnessed & tamed, including nature)*

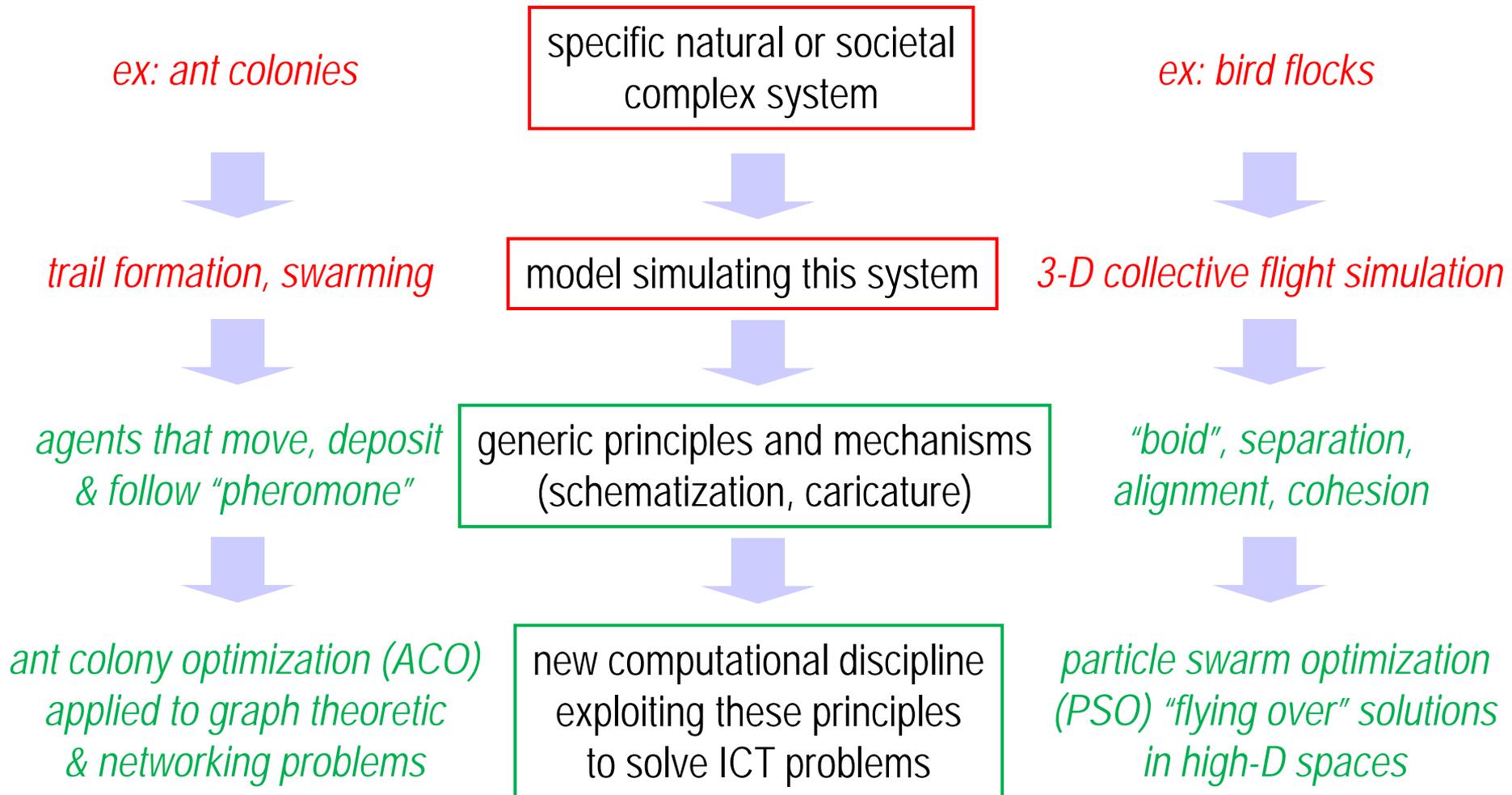
1. Introduction — b. A vast archipelago

➤ Exporting natural CS to artificial disciplines, such as ICT



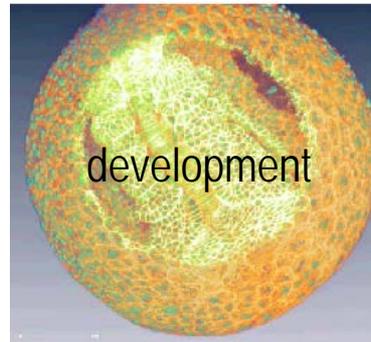
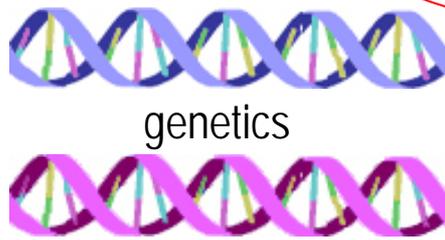
1. Introduction — b. A vast archipelago

➤ Exporting natural CS to artificial disciplines, such as ICT

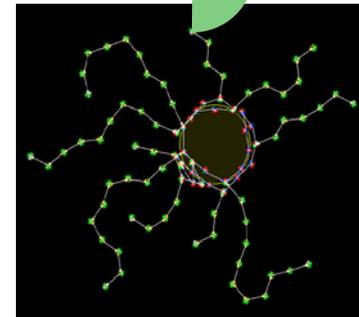
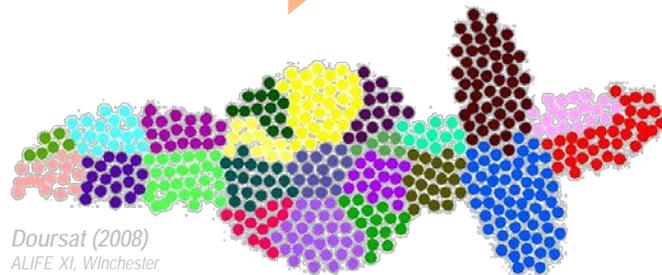
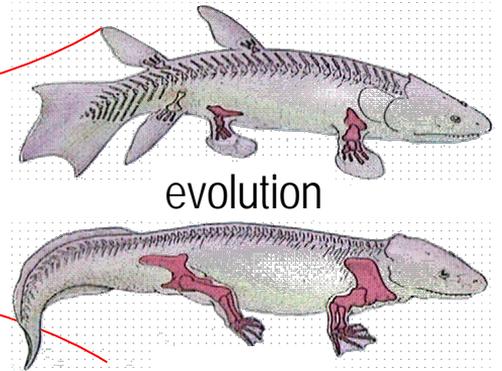


1. Introduction — b. A vast archipelago

- Another source of inspiration: biological morphogenesis—the epitome of a self-architecting system
 - *exploring computational multi-agent models of evolutionary development ...*



Nadine Peyri ras, Paul Bourguine et al.
(Embryomics & BioEmergences)



... toward possible outcomes in distributed, decentralized engineering systems

A Tour of Complex Systems

1. Introduction

- a. What are complex systems?
- b. A vast archipelago
- c. Computational modeling**

2. A Complex Systems Sampler

3. Commonalities

4. NetLogo Tutorial

1. Introduction — c. Computational modeling

➤ What this course is about

- ✓ an *exploration* of various complex systems *objects* (i.e., made of many agents, with simple or complex rules, and complex behavior):
 - cellular automata, pattern formation, swarm intelligence, complex networks, spatial communities, structured morphogenesis
- ✓ and their common *questions*:
 - emergence, self-organization, positive feedback, decentralization, between simple and disordered, “more is different”, adaptation & evolution
- ✓ by interactive *experimentation* (using NetLogo),
- ✓ introducing *practical* complex systems *modeling* and simulation
- ✓ from a *computational* viewpoint, in contrast with a “mathematical” one (i.e., formal or numerical resolution of symbolic equations),
- ✓ based on discrete *agents* moving in discrete or quasi-continuous space, and *interacting* with each other and their environment

1. Introduction — c. Computational modeling

➤ What this course is not

- ✓ a technical course about the archipelago of related disciplines
 - an information theory / computational complexity class
 - a dynamical systems / chaos / fractals / stochastic processes class
 - a systems engineering / control theory class
 - a graph theory / networks / statistical physics class
- ✓ a technical course about big questions × big objects
 - a fluid dynamics class
 - a condensed matter class
 - an embryology class
 - a neuroscience class
 - an entomology class
 - a sociology class
 - an economics class
 - ...



you can wake up now
... but what about the math?

1. Introduction — c. Computational modeling

- **Existence of macro-equations for some dynamic systems**
- ✓ we are typically interested in obtaining an explicit description or expression of the behavior of a whole system over time
 - ✓ in the case of dynamical systems, this means *solving* their evolution rules, traditionally a set of *differential equations* (DEs)
 - ✓ either *ordinary* (O)DEs of *macro-variables* in *well-mixed* systems
 - ex: in chemical kinetics, the law of mass action governing concentrations:
$$\alpha A + \beta B \rightarrow \gamma C \quad \text{described by} \quad d[A]/dt = -\alpha k [A]^\alpha [B]^\beta$$
 - ex: in economics, (simplistic) laws of gross domestic product (GDP) change:
$$dG(t)/dt = \rho G(t)$$
 - ✓ or *partial* (P)DEs of *local variables* in *spatially extended* systems
 - ex: heat equation: $\partial u/\partial t = \alpha \nabla^2 u$, wave equation: $\partial^2 u/\partial t^2 = c^2 \nabla^2 u$
 - ex: Navier-Stokes in fluid dynamics, Maxwell in electromagnetism, etc.

1. Introduction — c. Computational modeling

➤ Existence of macro-equations and an analytical solution

- ✓ in some cases, the explicit formulation of an exact solution can be found by calculus, i.e., the *symbolic manipulation of expressions*

- ex: geometric GDP growth \Rightarrow exponential function

$$dG(t)/dt = \rho G(t) \Rightarrow G(t) = G(0) e^{-\rho t}$$

- ex: heat equation \Rightarrow linear in 1D borders; widening Gaussian around Dirac

$$\partial u / \partial t = \alpha \partial^2 u / \partial x^2 \text{ and } u(x, 0) = \delta(x) \Rightarrow u(x, t) = \frac{1}{\sqrt{4\pi kt}} \exp\left(-\frac{x^2}{4kt}\right)$$

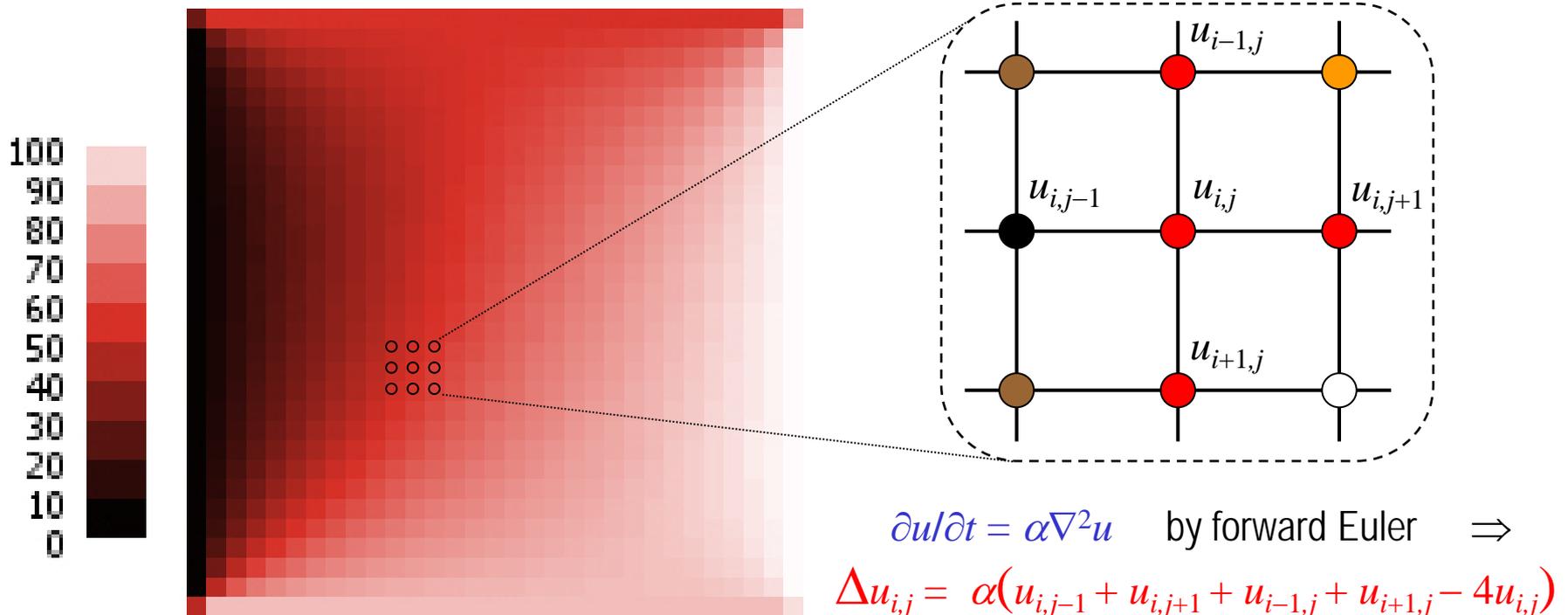
- ✓ calculus (or analysis) relies on known shortcuts in the world of mathematical “regularities”, i.e., mostly the family of continuous, derivable and integrable functions that can be expressed symbolically

→ *unfortunately, although vast, this family is in fact very small compared to the immense range of dynamical behaviors that natural complex systems can exhibit!*

1. Introduction — c. Computational modeling

- Existence of macro-equations **but no analytical solution**
 - ✓ when there is no symbolic resolution of an equation, *numerical analysis* involving algorithms (step-by-step recipes) can be used
 - ✓ it involves the discretization of space into cells, and time into steps

NetLogo model: /Chemistry & Physics/Heat/Unverified/Heat Diffusion



1. Introduction — c. Computational modeling

➤ Absence of macro-equations

✓ “*The study of non-linear physics is like the study of non-elephant biology.*” —Stanislaw Ulam

- the physical world is a fundamentally *non-linear* and *out-of-equilibrium* process
- focusing on linear approximations and stable points is missing the big picture in most cases

✓ let's push this quip: “*The study of non-analytical complex systems is like the study of non-elephant biology.*” —??

- complex systems have their own “elephant” species, too: dynamical systems that can be described by diff. eqs or statistical laws

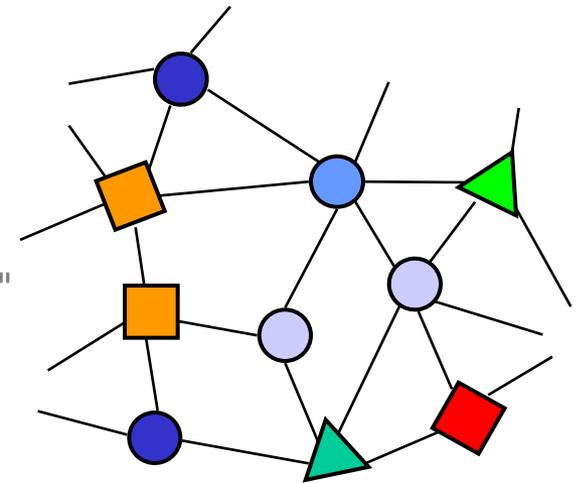
→ *most real-world complex systems do not obey neat macroscopic laws*



1. Introduction — c. Computational modeling

➤ Where global ODEs and spatial PDEs break down...

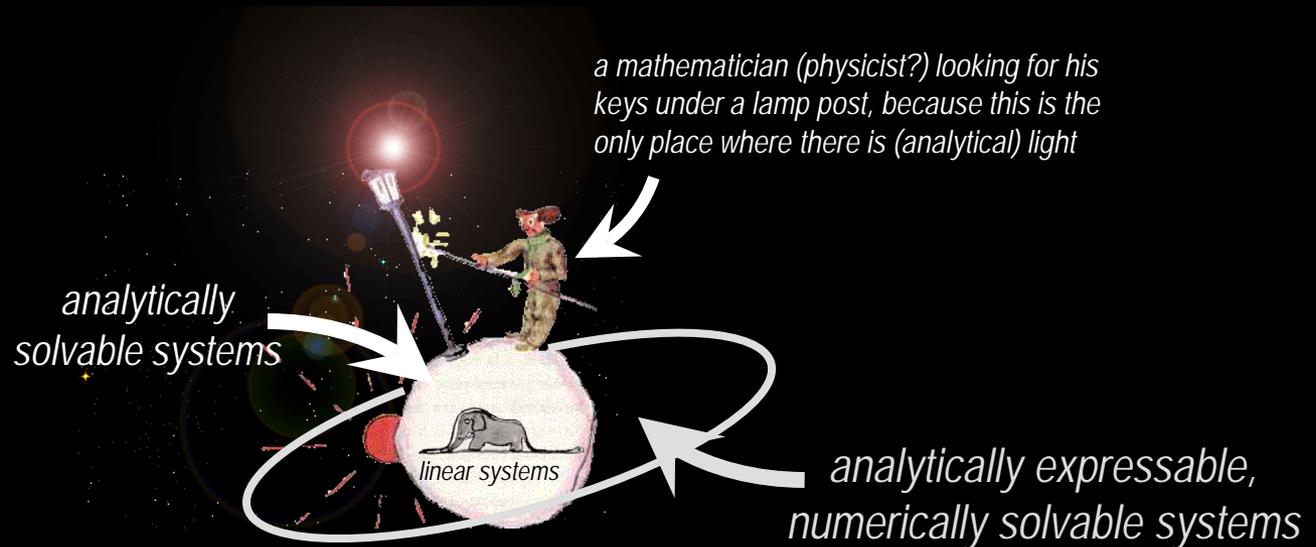
- ✓ systems that *no macroscopic quantity* suffices to explain ~~(ODE)~~
 - no law of "concentration", "pressure", or "gross domestic product"
 - even if global metrics can be designed to give an indication about the system's dynamical regimes, they rarely obey a given equation or law
- ✓ systems that require a *non-Cartesian* decomposition of space ~~(PDE)~~
 - network of irregularly placed or mobile *agents*
- ✓ systems that contain *heterogeneity*
 - segmentation into different *types of agents*
 - at a fine grain, this would require a "patchwork" of regional equations (ex: embryo)
- ✓ systems that are dynamically *adaptive*
 - the topology and strength of the interactions depend on the short-term activity of the agents and long-term "fitness" of the system in its environment



ex: embryogenesis

1. Introduction — c. Computational modeling

➤ The world of complex systems modeling



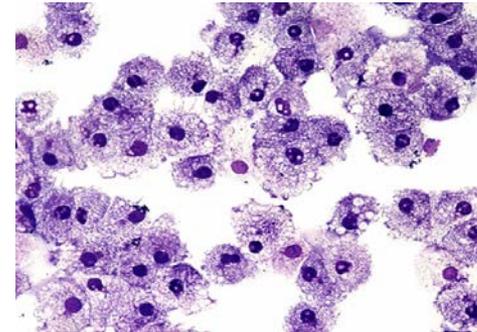
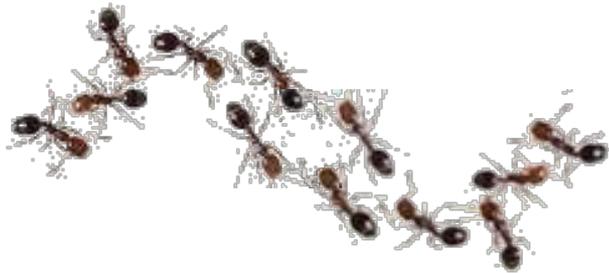
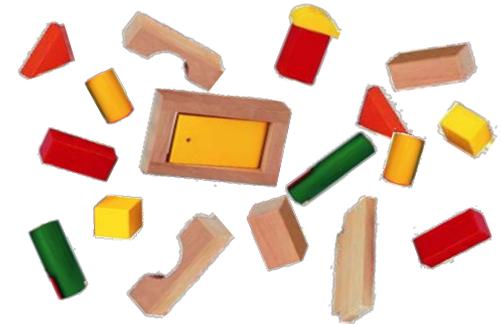
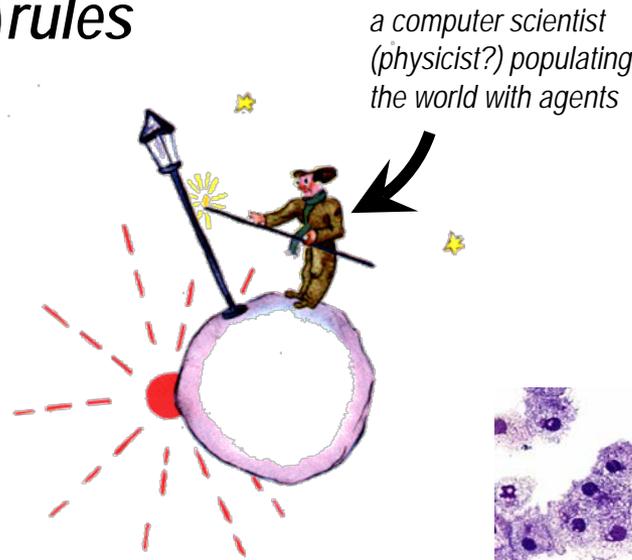
all the rest:
non-analytically expressable systems
⇒ computational models

The Lamplighter & the Elephant-Digesting Boa, from "The Little Prince"
Antoine de Saint-Exupéry

1. Introduction — c. Computational modeling

➤ The world of computational (agent) modeling

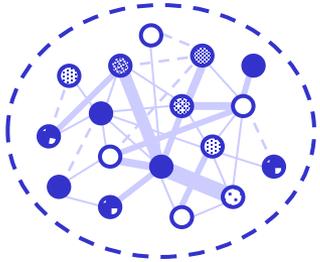
- ✓ not a cold and dark place!... it is teeming with myriads of *agents* that carry (micro-)*rules*



- ✓ the operational concept of "agent" is inspired from "social" groups: people, insects, cells, modules: agents have *goals* and *interactions*

1. Introduction — c. Computational modeling

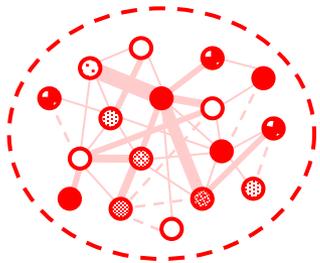
- **ABM** meets **MAS**: two (slightly) different perspectives



CS science: understand "natural" CS
→ *Agent-Based Modeling (ABM)*

... "Multi Agent-Based
Modeling and Simulation
Systems" (MABMSS)??

computational complex systems



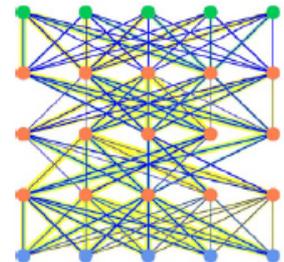
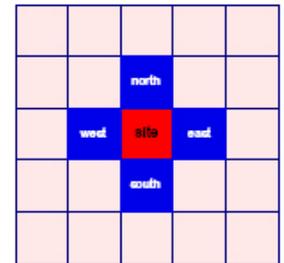
*CS engineering: design a new generation of
"artificial" CS* → *Multi-Agent Systems (MAS)*

- ✓ but again, don't take this distinction too seriously! they overlap a lot

1. Introduction — c. Computational modeling

➤ ABM: the modeling perspective from CA & social science

- ✓ *agent-* (or individual-) *based modeling* (ABM) arose from the need to model systems that were too complex for analytical descriptions
 - ✓ one origin: cellular automata (CA)
 - von Neumann self-replicating machines → Ulam's "paper" abstraction into CAs → Conway's *Game of Life*
 - based on *grid* topology
 - ✓ other origins rooted in economics and social sciences
 - related to "methodological individualism"
 - mostly based on grid and *network* topologies
 - ✓ later: extended to ecology, biology and physics
 - based on grid, network and 2D/3D *Euclidean* topologies
- *the rise of fast computing made ABM a practical tool*



1. Introduction — c. Computational modeling

➤ MAS: the engineering perspective from computer sci. & AI

- ✓ in software engineering, the need for clean *architectures*
 - historical trend: breaking up big monolithic code into *layers*, *modules* or *objects* that communicate via application programming *interfaces* (APIs)
 - this allows fixing, upgrading, or replacing parts without disturbing the rest

- ✓ in AI, the need for *distribution* (formerly “DAI”)
 - break up big systems into smaller units creating a decentralized computation: *software/intelligent agents*

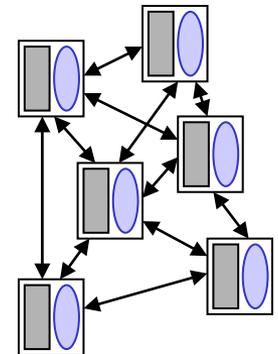
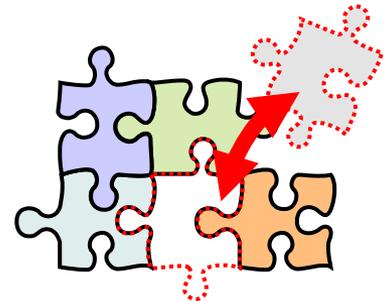
- ✓ difference with object-oriented programming:

- agents are “proactive” / autonomously threaded

- ✓ difference with distributed (operating) systems:

- agents don't appear transparently as one coherent system

→ *the rise of pervasive networking made distributed systems both a necessity and a practical technology*



1. Introduction — c. Computational modeling

➤ MAS: the engineering perspective from computer sci. & AI

- ✓ emphasis on software agent as a *proxy* representing human users and their interests; users state their prefs, agents try to satisfy them
 - ex: internet agents searching information
 - ex: electronic broker agents competing / cooperating to reach an agreement
 - ex: automation agents controlling and monitoring devices
- ✓ main tasks of MAS programming: agent design and society design
 - an agent can be ± reactive, proactive, deliberative, social (Wooldridge)
 - an agent is caught between (a) its own (complicated) goals and (b) the constraints from the environment and exchanges with the other agents

→ *slight contrast between the MAS and ABM philosophies*

- MAS: focus on few "heavy-weight" (big program), "selfish", intelligent agents
 - ABM: many "light-weight" (few rules), highly "social", simple agents
- MAS: focus on game theoretic gains – ABM: collective emergent behavior

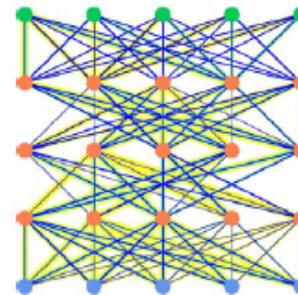
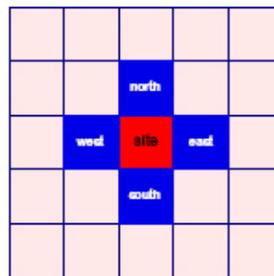
1. Introduction — c. Computational modeling

➤ An agent in this course

- ✓ a (small) program deemed “local” or “autonomous” because it has
 - its own scheduling (execution process or thread)
 - its own memory (data encapsulation)
 - ... generally simulated in a virtual machine
- ✓ this agent-level program can consist of
 - *a set of dynamical equations (“reactive”) at the microscopic level*
 - *a set of logical rules (AI)... or a mix of both*
- ✓ peer-to-peer interactions among agents under different topologies



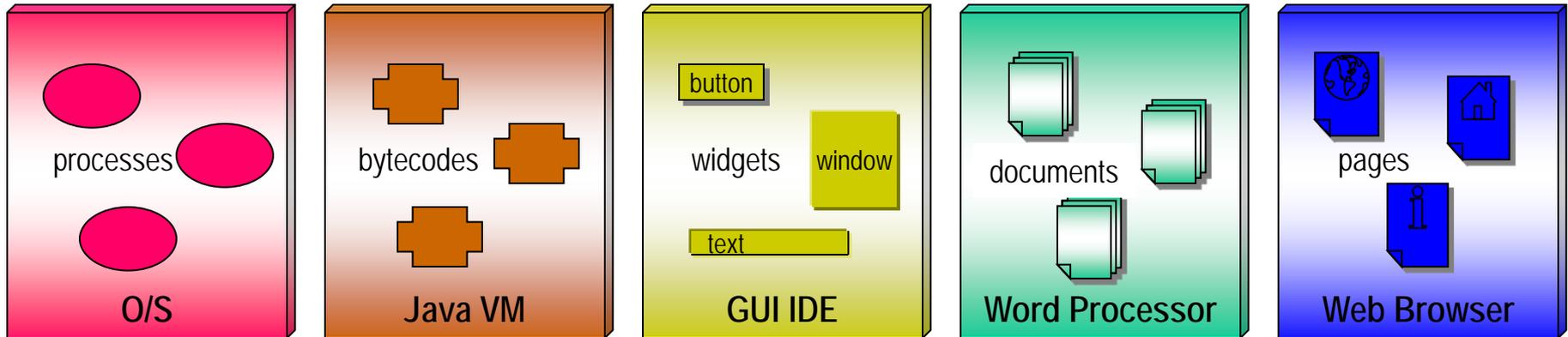
Hugo Weaving as Agent Smith
The Matrix Revolutions, Warner Bros.



1. Introduction — c. Computational modeling

➤ Agent virtual machines or “platforms”

✓ just like there are various middleware-componentware frameworks...



✓ ... there are also ABM platforms, e.g., *NetLogo*, *Swarm*, or *Repast*

