

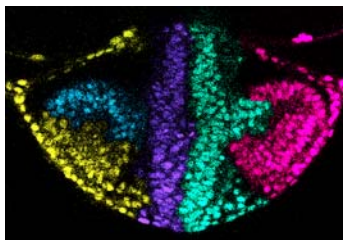
Heterogeneous collective motion or moving pattern formation?

the self-made puzzle

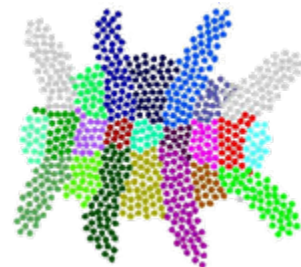
of embryogenesis under the light of multi-agent modeling

René Doursat

<http://www.iscpif.fr/~doursat>



INSTITUT
DES SYSTEMES COMPLEXES



Systems that are self-organized and architected



free self-organization

the challenge for complex systems:
integrate a true **architecture**



the challenge for complicated systems: integrate **self-organization**

deliberate design



designed self-organization / self-organized design

Toward programmed self-organization

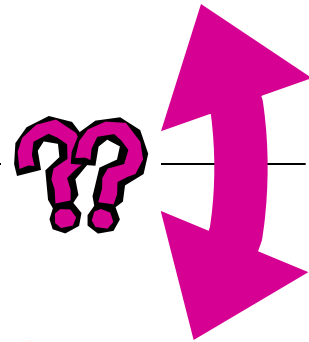
➤ Self-organized systems

- ✓ a myriad of self-positioning agents
- ✓ collective order is not imposed from outside (only influenced)
- ✓ comes from purely *local* information & interaction around each agent
- ✓ no agent possesses the global map or goal of the system
- ✓ but every agent may contain all the *rules* that contribute to it



➤ Structured systems

- ✓ true *architecture*: non-trivial, complicated morphology
 - *hierarchical*, multi-scale: regions, parts, details, agents
 - *modular*: reuse, quasi-repetition
 - *heterogeneous*: differentiation & divergence in the repetition
- ✓ *random* at the microscopic level, *but reproducible* (quasi deterministic) at the mesoscopic and macroscopic levels



Quick preview of multi-agent embryogenesis

➤ An abstract (computational) approach to development



- ✓ as a fundamentally *spatial* phenomenon
- ✓ highlighting the *broad principles* – necessary to absorb and integrate the data – and proposing a *computational* model of these principles

➤ Broad principles



1. *biomechanics* → collective motion → “sculpture” of the embryo
 2. *gene regulation* → gene expression patterns → “painting” of the embryo
- + *coupling* between *shapes* and *colors*

➤ Multi-agent models



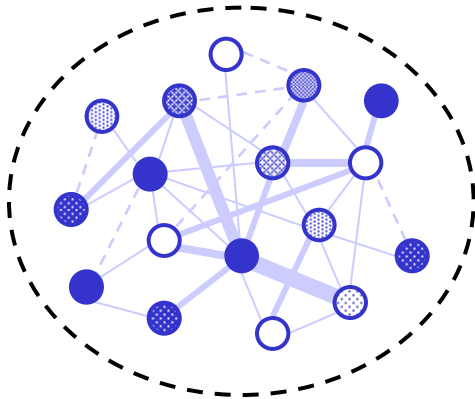
- ✓ best positioned to integrate both
- ✓ account for heterogeneity, modularity, hierarchy
- ✓ each agent carries a set of *biomechanical* and *regulatory* rules

The self-made puzzle of embryogenesis

1. Self-organized and structured systems
2. Two-side challenge: heterogeneous motion / moving patterns
3. A multi-agent model of embryogenesis
4. Evolutionary development (evo-devo)

Self-organized and structured systems

➤ Complex systems in many domains



- large number of elementary **agents** interacting **locally**
- simple individual behaviors creating a complex **emergent** collective behavior
- *decentralized dynamics: no master blueprint or grand architect*

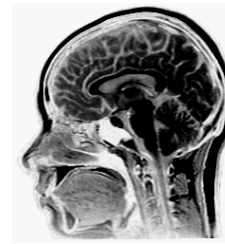
✓ **physical**, **biological**, **technical**, **social** systems (natural or artificial)



pattern
formation
○ = matter



biological
development
○ = cell

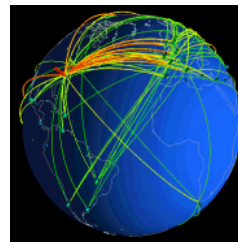


the brain
& cognition
○ = neuron

insect
colonies
○ = ant



Internet
& Web
○ = host/page




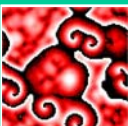
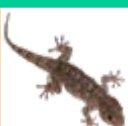



social
networks
○ = person



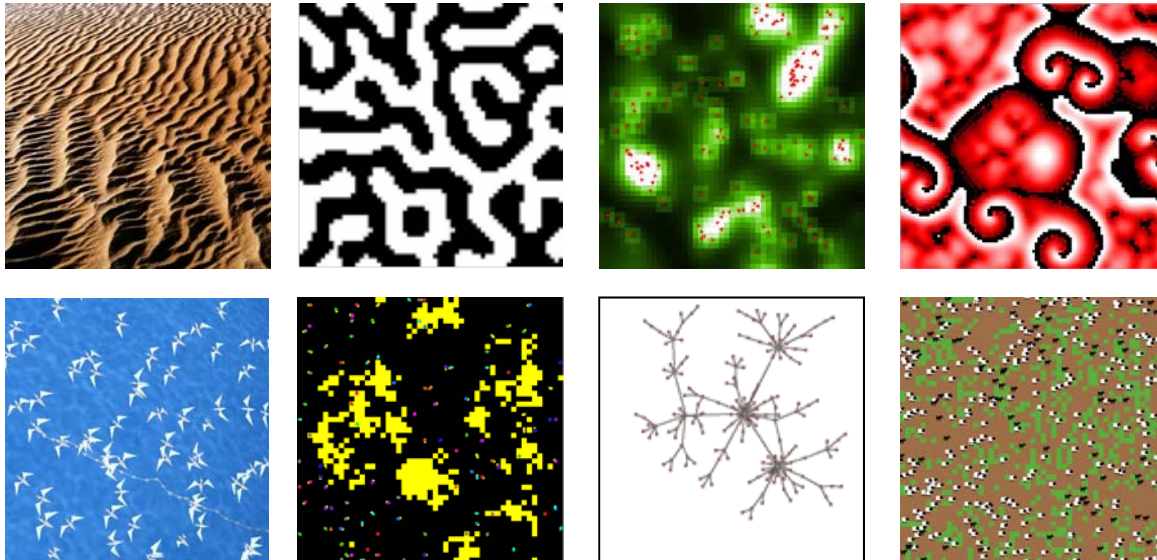
"Statistical" vs. "morphological" complex systems

➤ A brief taxonomy of systems

Category	<i>Agents / Parts</i>	<i>Local Rules</i>	<i>Emergent Behavior</i>	<i>A "Complex System"?</i>
 two-body problem	<i>few</i>	<i>simple</i>	<i>simple</i>	<i>NO</i>
 three-body pb, low-D chaos	<i>few</i>	<i>simple</i>	<i>complex</i>	<i>NO – too small</i>
 crystal, gas	<i>many</i>	<i>simple</i>	<i>simple</i>	<i>NO – few params suffice to describe it</i>
 patterns, swarms, complex networks	<i>many</i>	<i>simple</i>	<i>"complex"</i>	<i>YES – but mostly random and uniform</i>
 structured morphogenesis	<i>many</i>	<i>sophisticated</i>	<i>complex</i>	<i>YES – reproducible and heterogeneous</i>
 machines, crowds with leaders	<i>many</i>	<i>sophisticated</i>	<i>"simple"</i>	<i>COMPLICATED – not self-organized</i>

Statistical (self-similar) systems

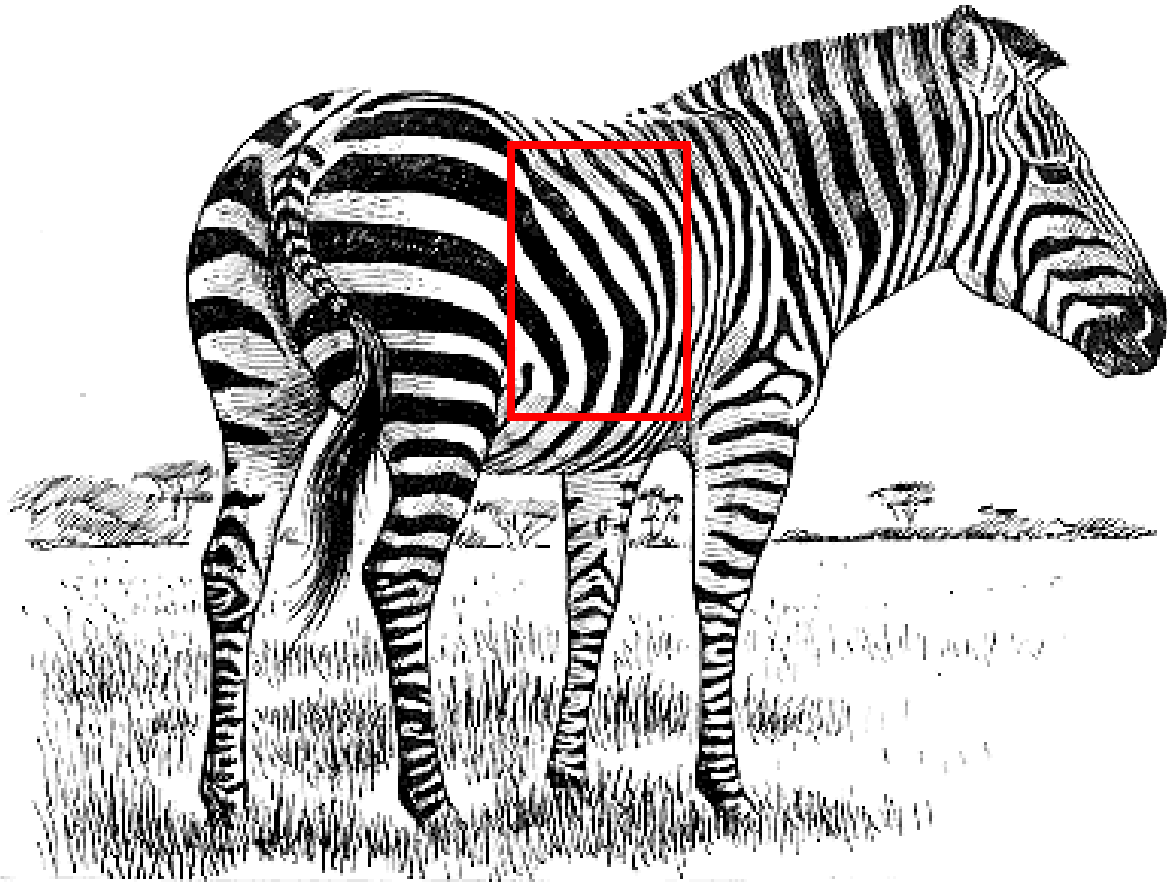
- Many agents, simple rules, “complex” emergent behavior
 - the “clichés” of complex systems: diversity of pattern formation (spots, stripes), swarms (clusters, flocks), complex networks, etc.



- ✓ yet, often like “textures”: repetitive, statistically *uniform*, information-poor
- ✓ spontaneous order arising from amplification of *random* fluctuations
- ✓ *unpredictable* number and position of mesoscopic entities (spots, groups)

Morphological (self-dissimilar) systems

compositional systems: pattern formation \neq morphogenesis



*"I have the stripes, but where is the zebra?" OR
 "The stripes are easy, it's the horse part that troubles me"*
 —attributed to A. Turing, after his 1952 paper on morphogenesis

Morphological (self-dissimilar) systems

➤ Many agents, sophisticated rules, complex emergence

→ *natural ex: organisms (cells)*



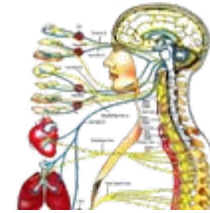
plants



vertebrates



arthropods



humans

- ✓ mesoscopic organs and limbs have intricate, *nonrandom* morphologies
- ✓ development is highly *reproducible* in number and position of body parts
- ✓ *heterogeneous* elements arise under information-rich genetic control

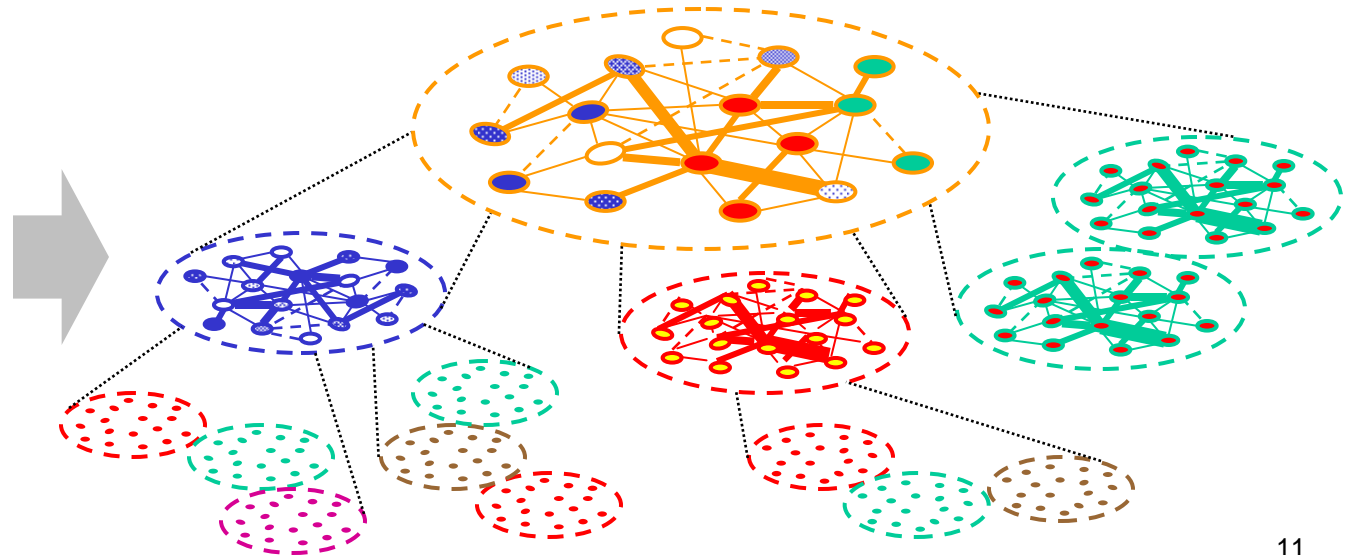
➤ Biological organisms are self-organized and structured

- ✓ because the pieces of the puzzle (agent rules) are more “sophisticated” (than inert matter): depend on agent’s *type* and/or *position* in the system
- ✓ the outcome (development) is truly complex but, paradoxically, can also be more *controllable* and *programmable*

Beyond statistics: heterogeneity, modularity, reproducibility

➤ Complex systems can be much more than a "soup"

- ✓ "complex" doesn't necessarily imply "homogeneous"...
→ *heterogeneous agents and diverse patterns, via positions*
- ✓ "complex" doesn't necessarily imply "flat" (or "scale-free")...
→ *modular, hierarchical, detailed architecture (at specific scales)*
- ✓ "complex" doesn't necessarily imply "random"...
→ *reproducible patterns relying on programmable agents*

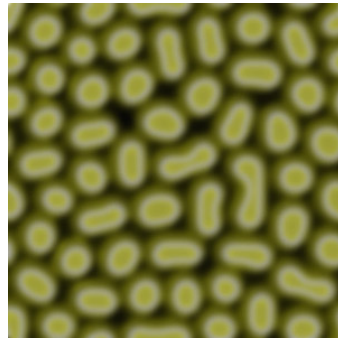


Statistical vs. morphological systems

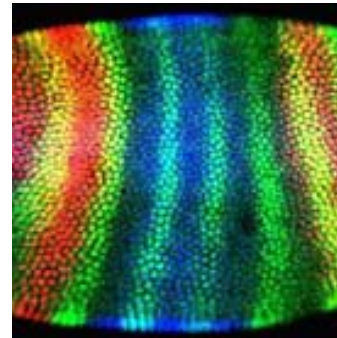
- Physical pattern formation is “free” –
Biological (multicellular) pattern formation is “guided”



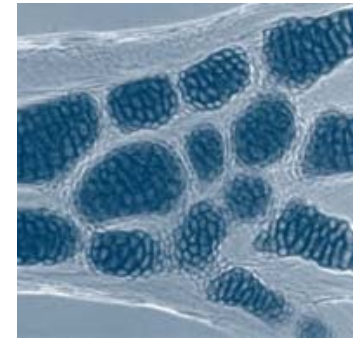
convection cells
www.chabotspace.org



reaction-diffusion
texturegarden.com/java/rd



fruit fly embryo
Sean Carroll, U of Wisconsin



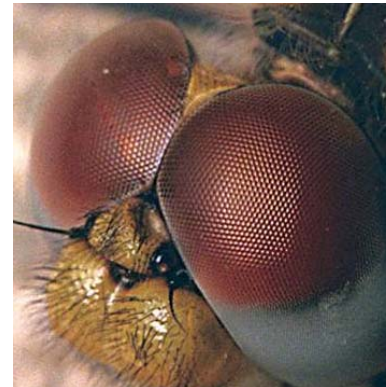
larval axolotl limb
Gerd B. Müller

Statistical vs. morphological systems

- Multicellular forms = a bit of “free” + a lot of “guided”
 - ✓ domains of free pattern embedded in a guided morphology



spots, stripes in skin
angelfish, www.sheddaquarium.org



ommatidia in eye
dragonfly, www.phy.duke.edu/~hsg/54

- ✓ repeated copies of a guided form, distributed in free patterns



flowers in tree
cherry tree, www.phy.duke.edu/~fortney



segments in insect
centipede, images.encarta.msn.com

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Morphogenesis couples **assembly** and **patterning**

➤ Sculpture → forms

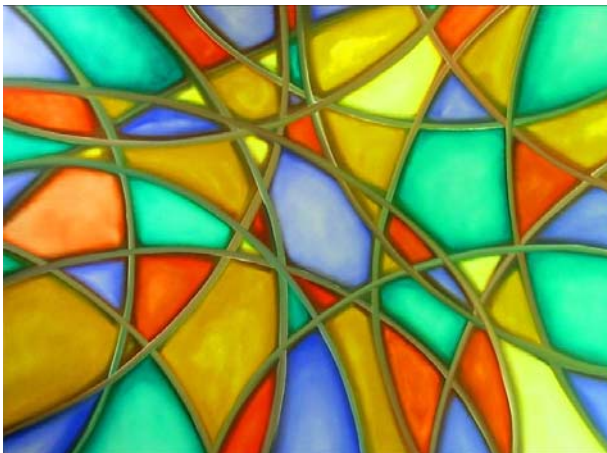
Ádám Szabó, *The chicken or the egg* (2005)
<http://www.szaboadam.hu>



"shape from patterning"

- ✓ the **forms** are "sculpted" by the self-assembly of the elements, whose behavior is triggered by the **colors**

➤ Painting → colors



"patterns from shaping"

- ✓ new **color** regions appear (domains of genetic expression) triggered by **deformations**

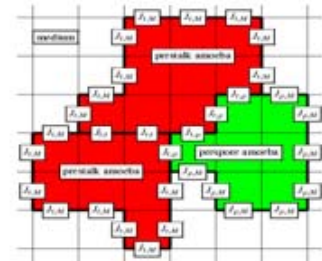
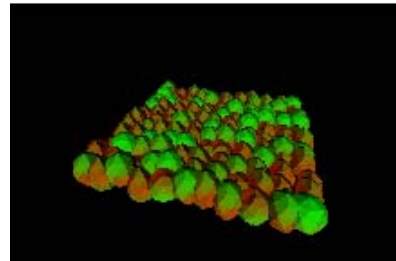
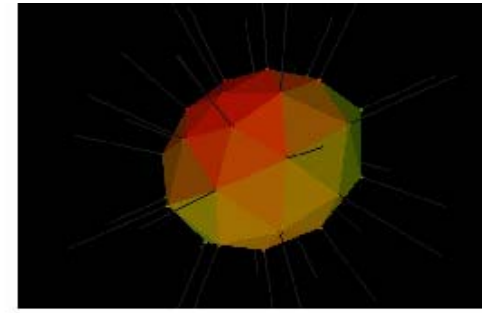
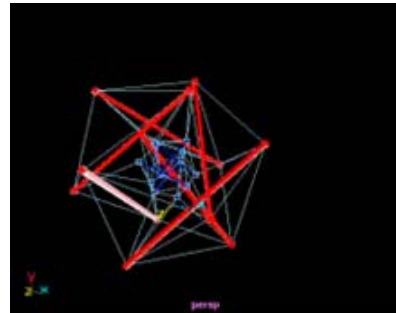


Embryogenesis couples **mechanics** and **regulation**

➤ Cellular mechanics

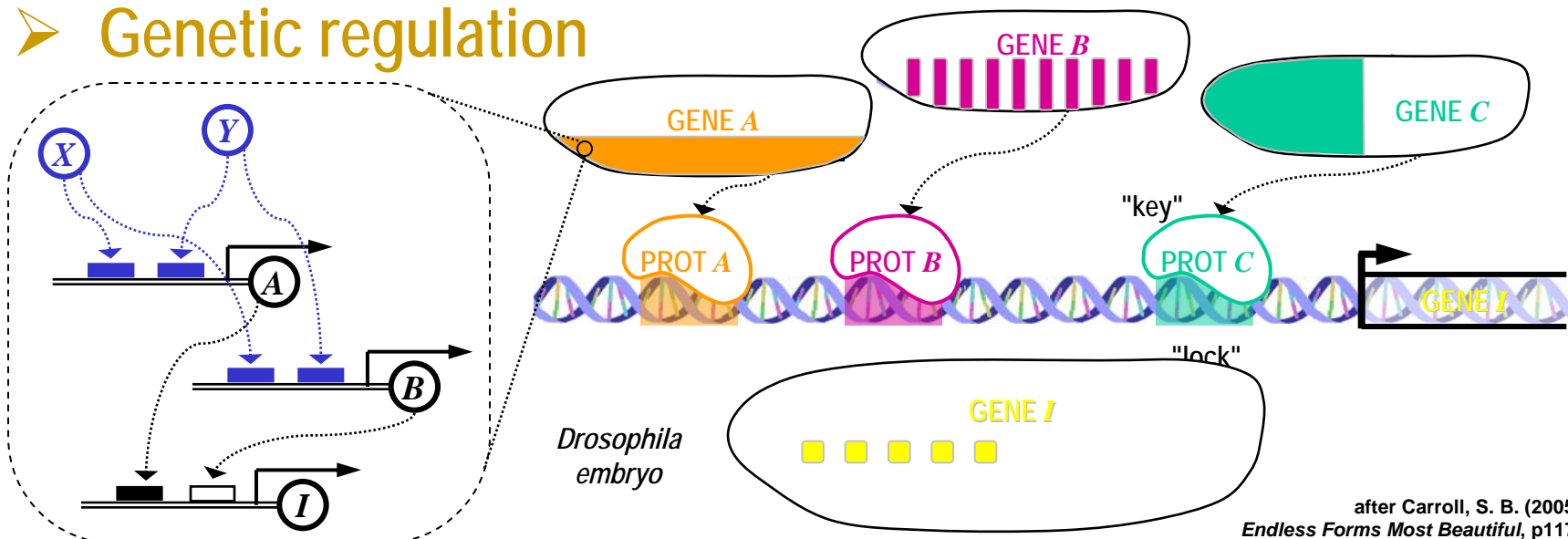
- ✓ adhesion
- ✓ deformation / reformation
- ✓ migration (motility)
- ✓ division / death

tensional integrity (Ingber)



cellular Potts model
(Graner, Glazier, Hogeweg)

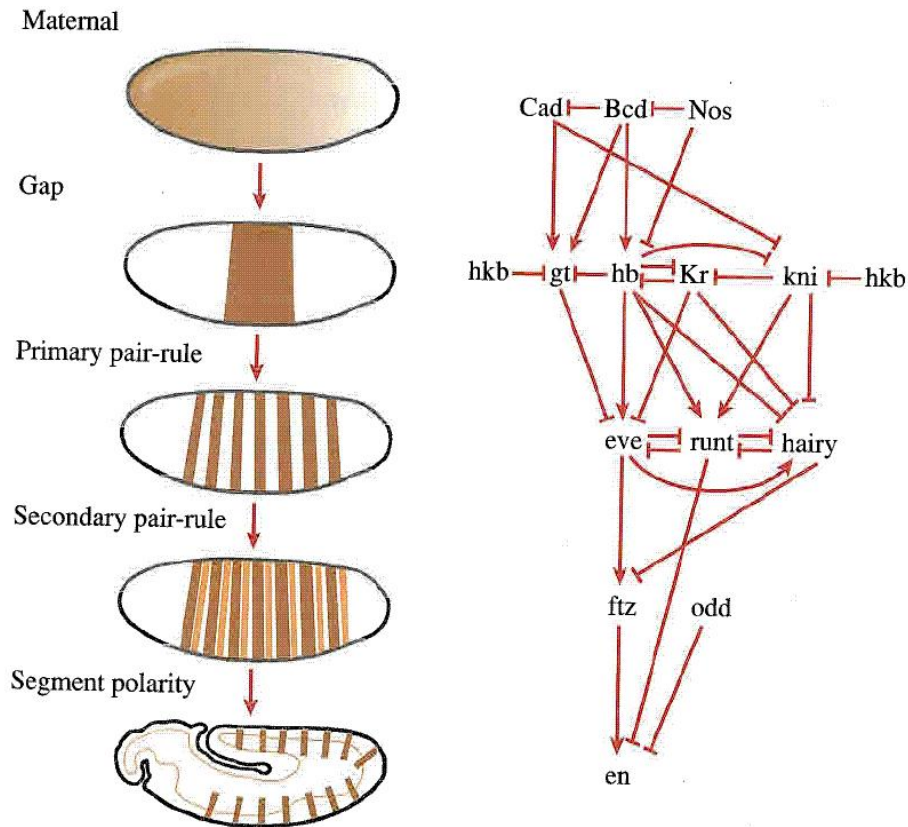
➤ Genetic regulation



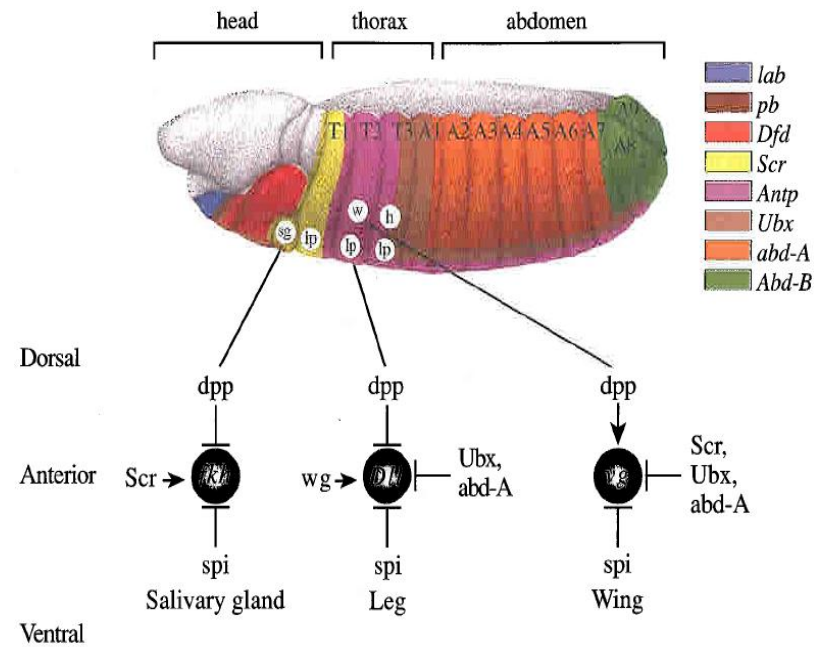
Gene regulatory pattern formation

➤ Segmentation & identity domains in *Drosophila*

- ✓ periodic A/P band patterns are controlled by a 5-tier gene regulatory hierarchy



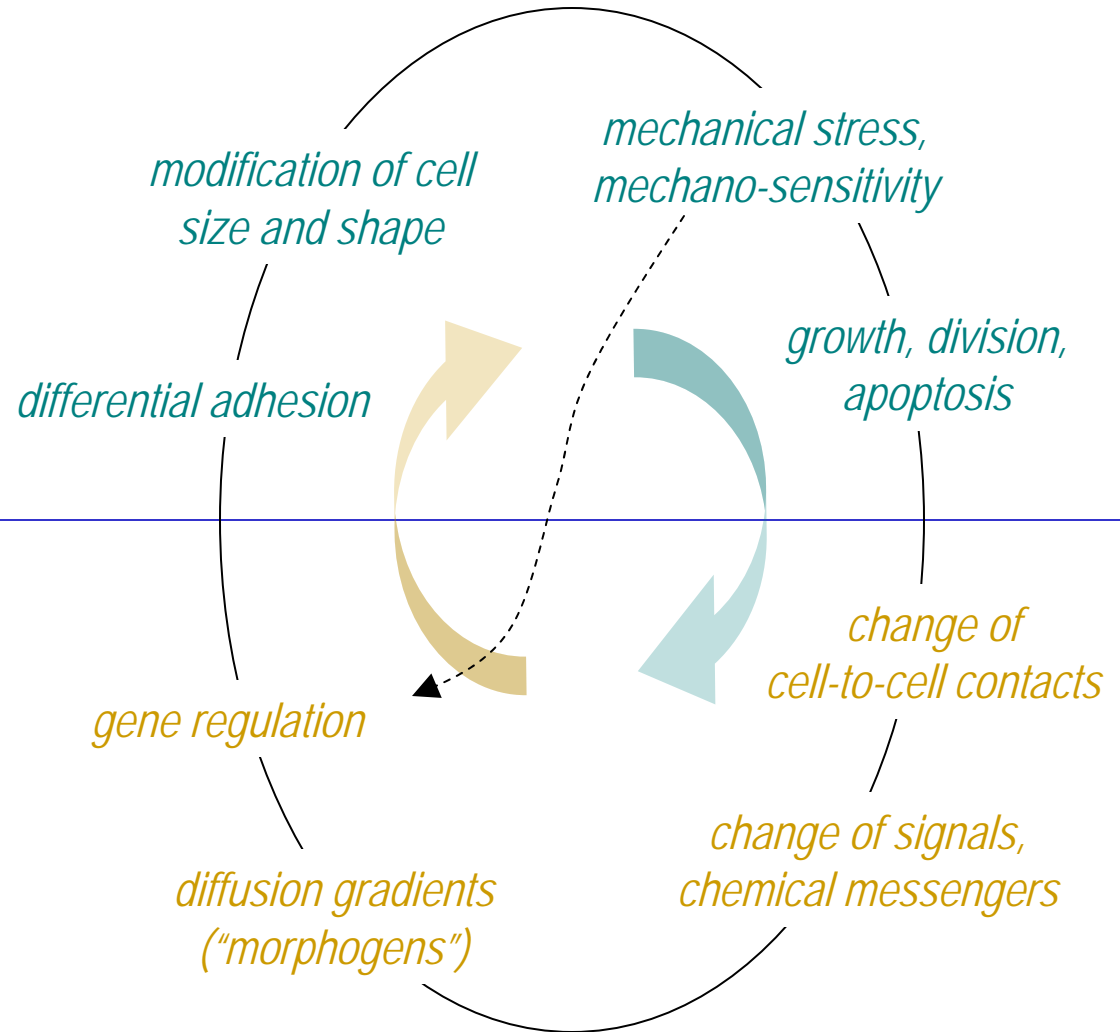
- ✓ intersection with other axes creates organ primordia and imaginal discs (identity domains of future legs, wings, antennae, etc.)



from Carroll, S. B., et al. (2001)
From DNA to Diversity, p63

Embryogenesis couples **mechanics** and **regulation**

➤ Cellular mechanics

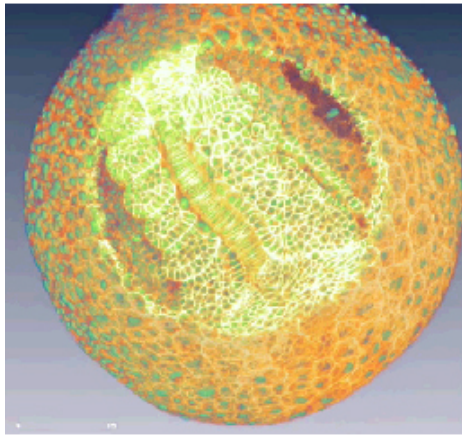


➤ Genetic regulation

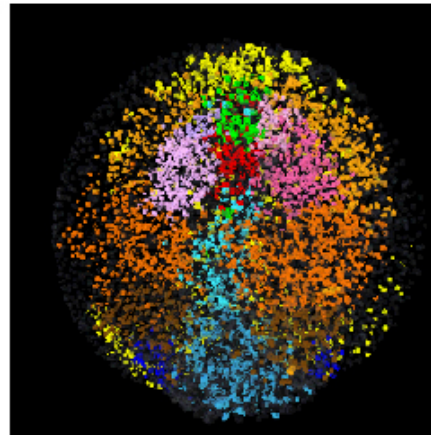
Embryogenesis couples motion and patterns

Nadine Peyrière, Paul Bourguin, Thierry Savy,
 Benoît Lombardot, Emmanuel Faure et al.
Embryonics & BioEmergences

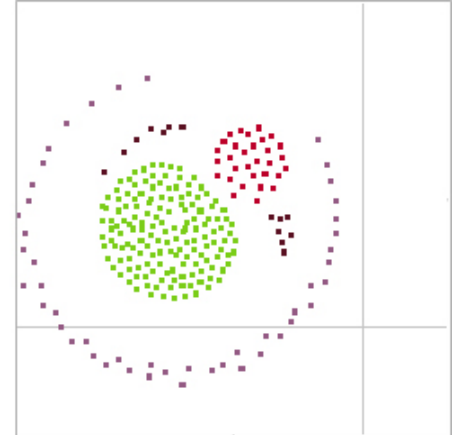
Collective motion regionalized into patterns



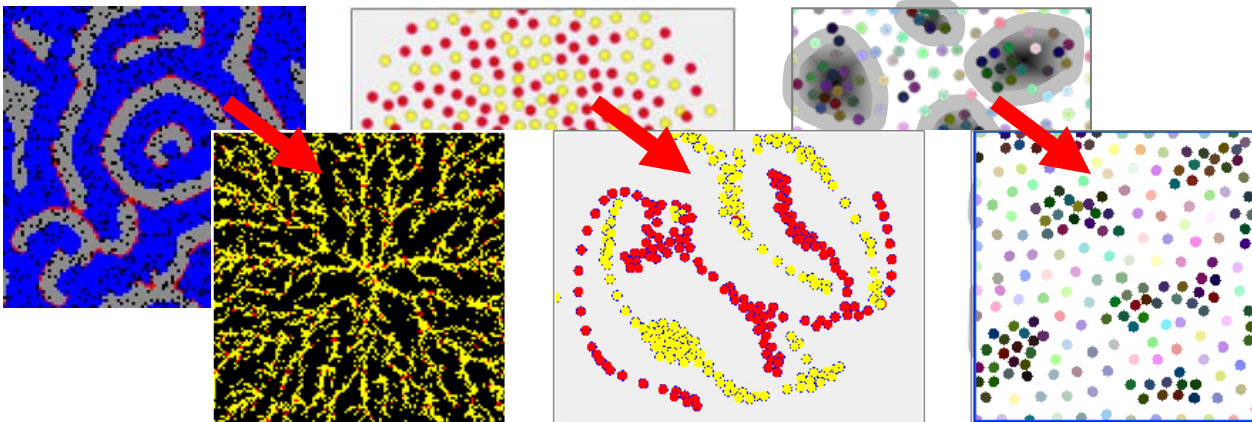
zebrafish



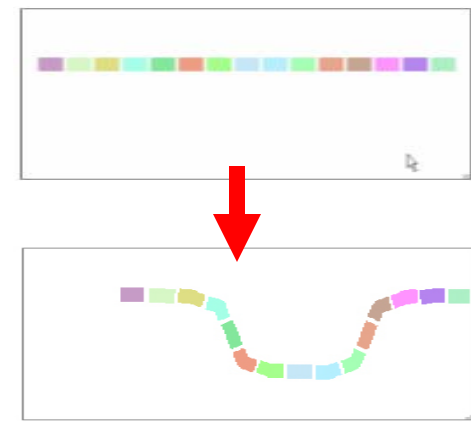
Hiroki Sayama (Swarm Chemistry)
<http://bingweb.binghamton.edu/~sayama/SwarmChemistry/>



➤ Pattern formation that triggers motion



<http://zool33.uni-graz.at/schmickl>



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Why multi-agent modeling?

➤ Equations and laws can be hard or impossible to find...

✓ *“The study of non-linear physics is like the study of non-elephant biology.” —Stanislaw Ulam*

- the physical world is a fundamentally *non-linear* and *out-of-equilibrium* process
- focusing on linear approximations and stable points is missing the big picture in most cases

✓ let's push this quip: *“The study of **non-analytical complex systems** is like the study of non-elephant biology.” —??*

- complex systems have their own “elephant” species, too: dynamical systems that can be described by diff. eqs or statistical laws
- many real-world complex systems do not obey neat macroscopic laws

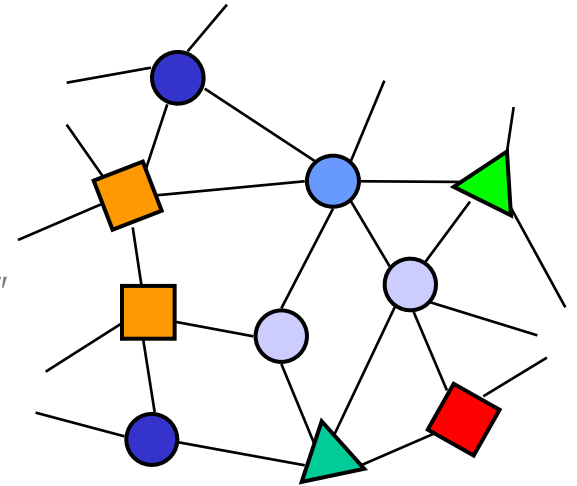


Why multi-agent modeling?

➤ Equations and laws can be hard or impossible to find in...

morphogenesis

- ✓ systems that *no macroscopic quantity* suffices to explain ~~(ODE)~~
 - no law of "concentration", "pressure", or "gross domestic product"
 - even if global metrics can be designed to give an indication about the system's dynamical regimes, they rarely obey a given equation or law
- ✓ systems that require a *non-Cartesian* decomposition of space ~~(PDE)~~
 - network of irregularly placed or mobile *agents*
- ✓ systems that contain *heterogeneity*
 - segmentation into different *types of agents*
 - at a fine grain, this would require a "patchwork" of regional equations
- ✓ systems that are dynamically *adaptive*
 - the topology and strength of the interactions depend on the short-term activity of the agents and long-term "fitness" of the system in its environment



Different approaches and families of models

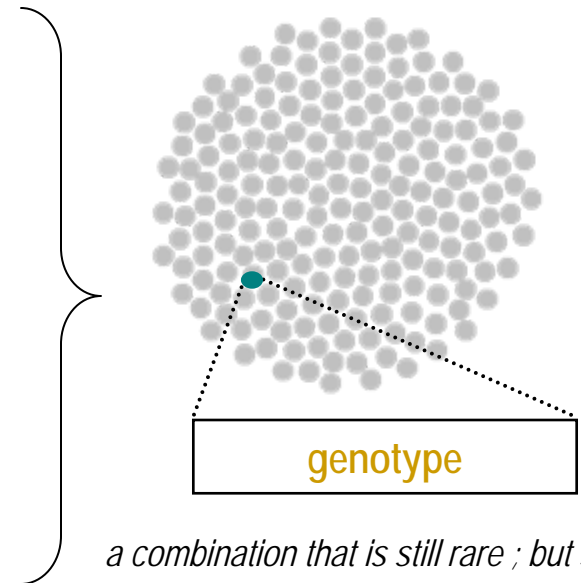
➤ Biological, bio-inspired or artificial models

✓ focused on spatial differentiation patterns (little or no motion)

- reaction-diffusion (PDEs, cellular automata)
- gene networks (Boolean or real concentrations)
- "amorphous computing"

✓ focused on motion (little or no patterning)

- (sub)cellular Potts model
- self-assembly, aggregation
- flocking, swarm formation, cellular sorting



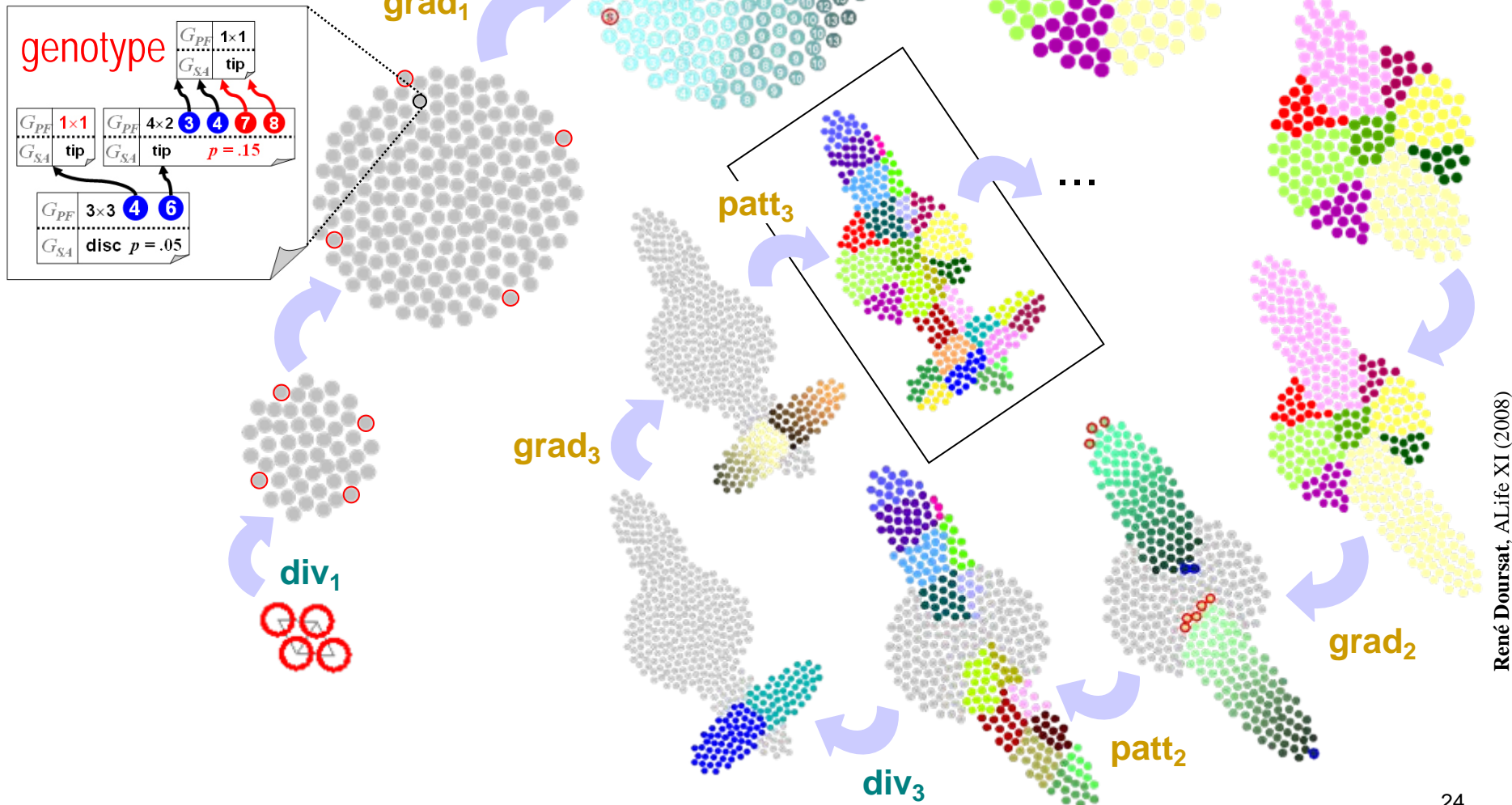
a combination that is still rare ; but see Hogeweg / Salazar-Ciudad / Mjolsness..

✓ at different scales

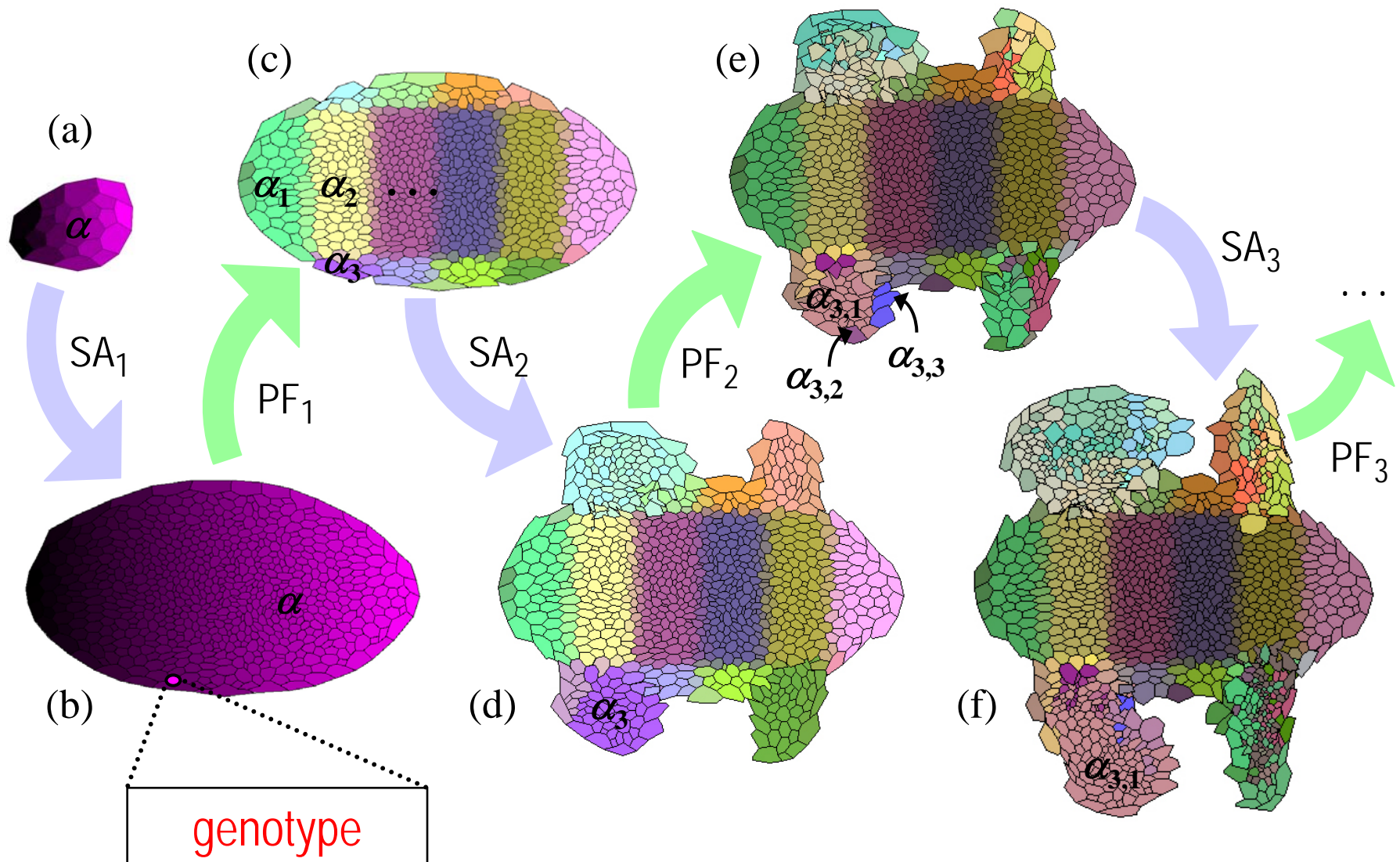
- macroscopic models (densities, differential geometry) → no individual information
- mesoscopic models (cellular centers, Potts) → no membrane or nuclei
- microscopic models (elastic polyedra, drop models) → cellular deformations

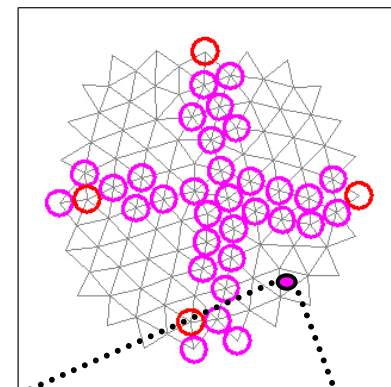
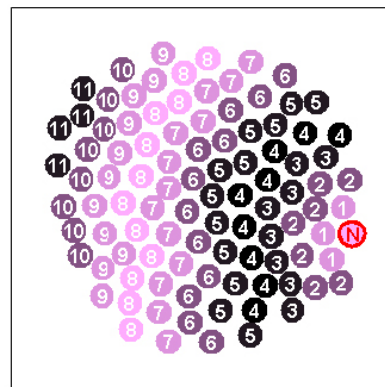
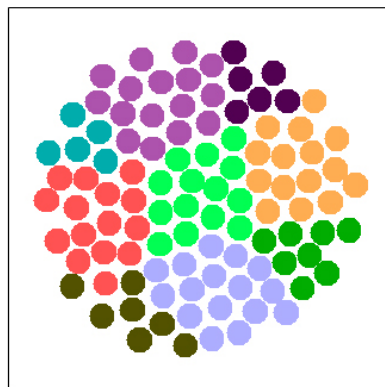
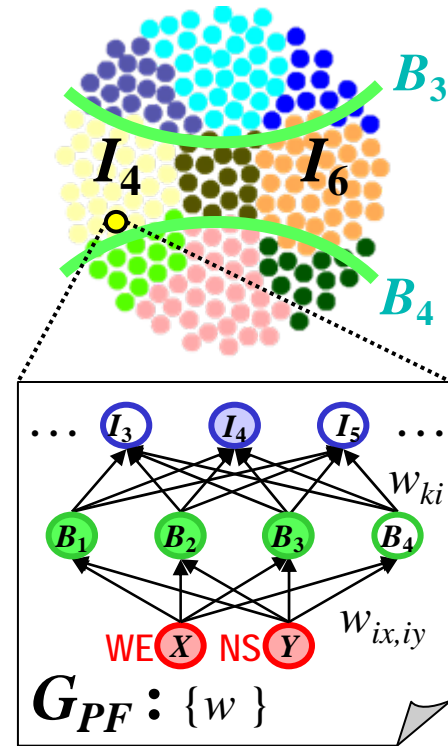
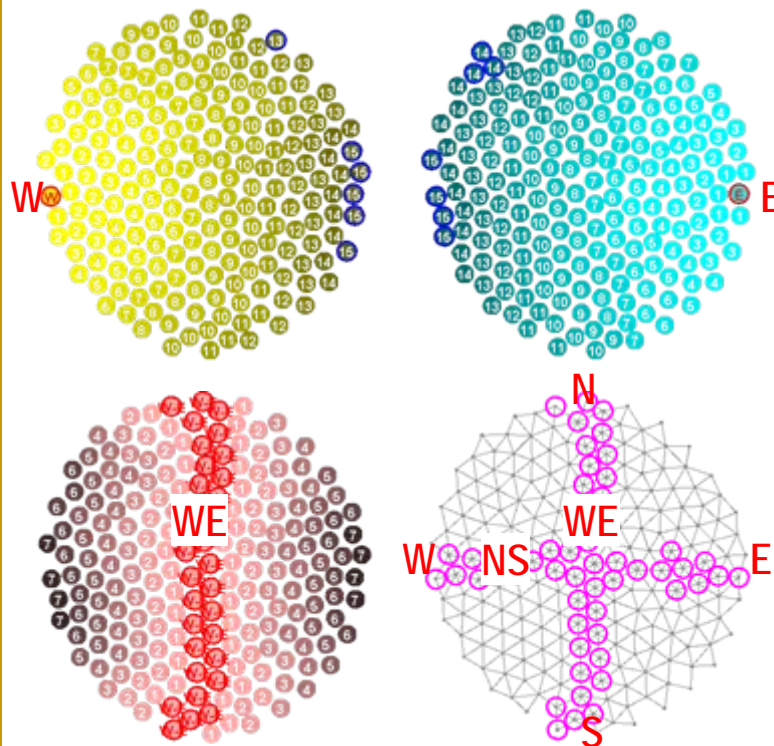
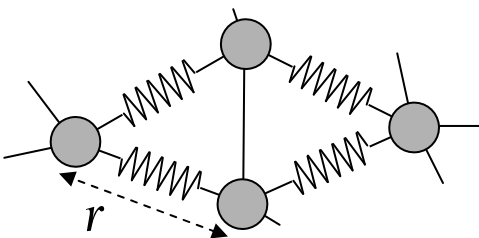
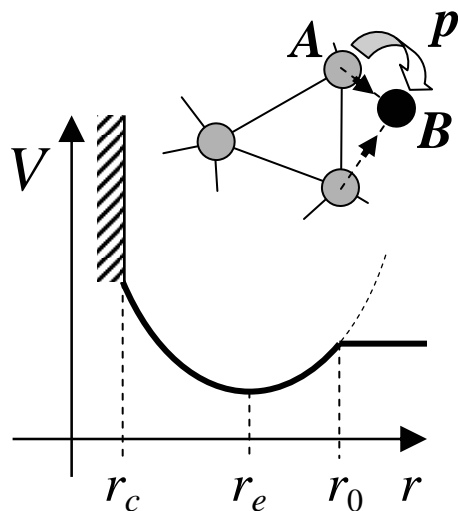
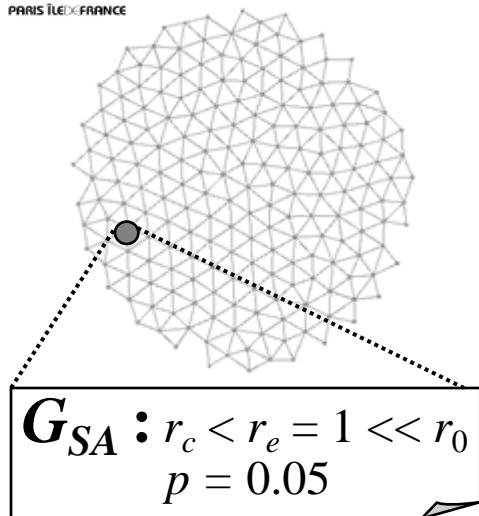
Exemple of hybrid mesoscopic model

➤ Recursive morphogenesis



1. Self-Assembly + 2. Pattern Formation = 3. Morphogenesis

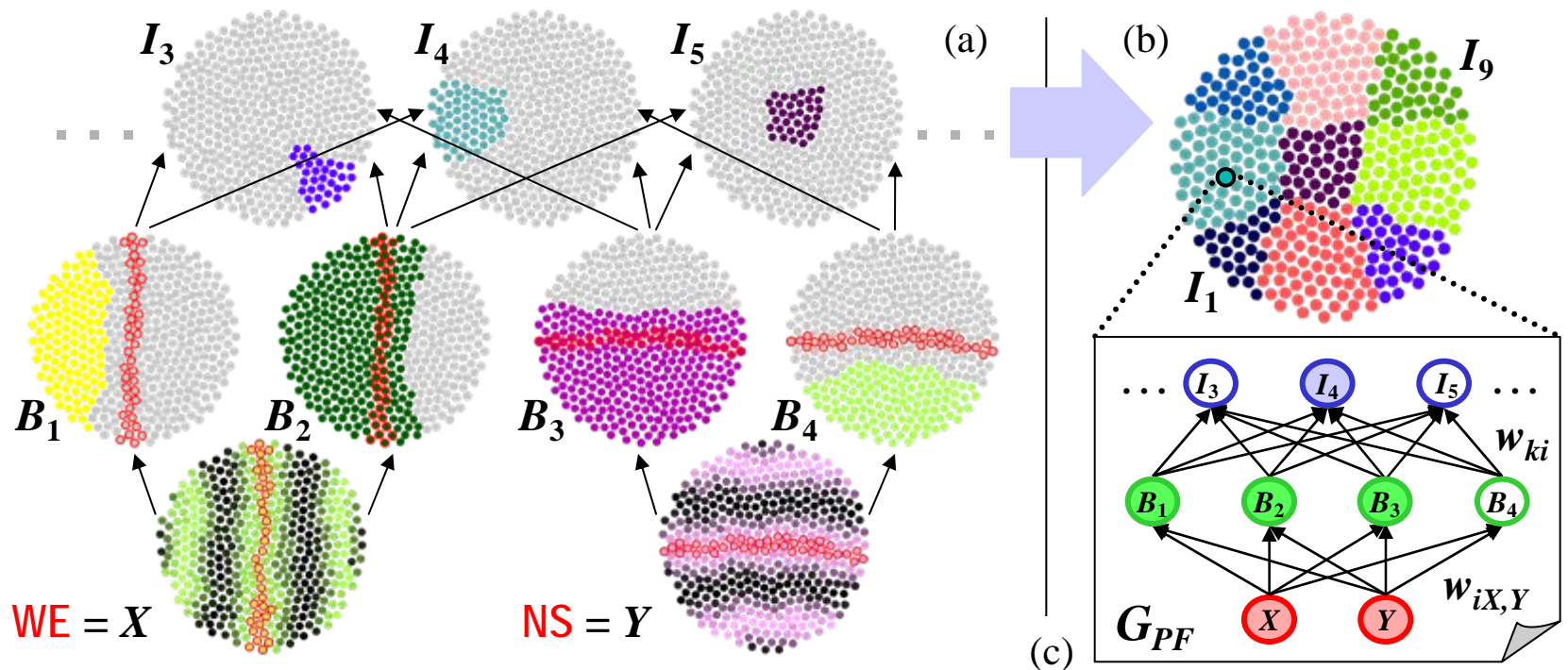




$$G_{SA} \cup G_{PF}$$

Virtual gene atlas

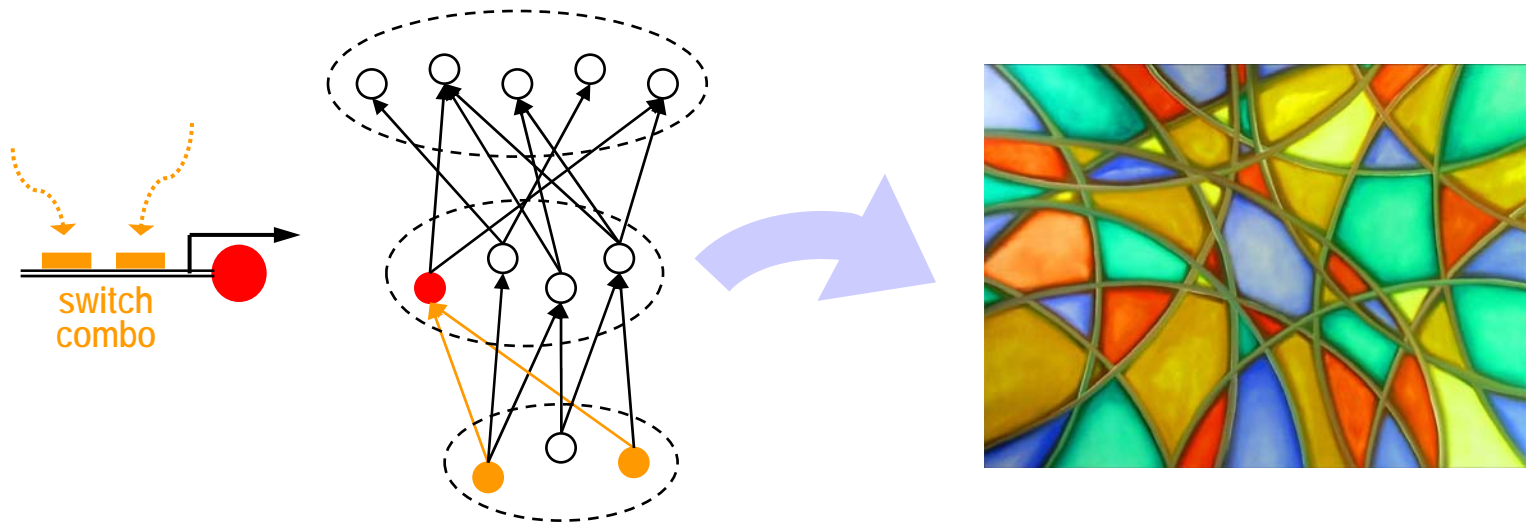
- **Programmed patterning (patt): the hidden embryo map**
 - a) same swarm in different colormaps to visualize the agents' internal patterning variables X , Y , B_i and I_k (virtual *in situ hybridization*)
 - b) consolidated view of all identity regions I_k for $k = 1 \dots 9$
 - c) gene regulatory network used by each agent to calculate its expression levels, here: $B_1 = \sigma(1/3 - X)$, $B_3 = \sigma(2/3 - Y)$, $I_4 = B_1 B_3 (1 - B_4)$, etc.



From feedforward to recurrent gene regulation

➤ Summary: simple feedforward hypothesis

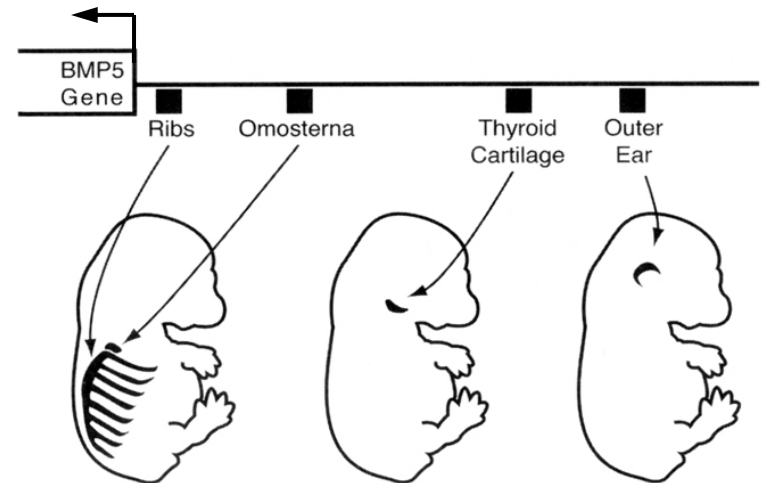
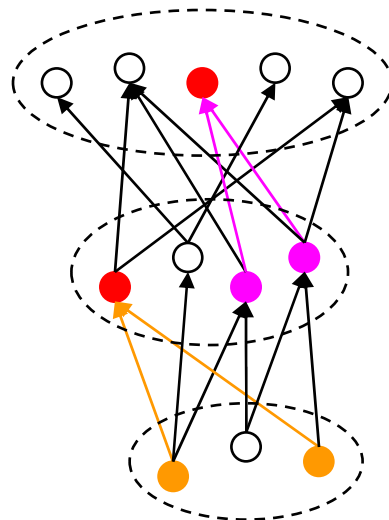
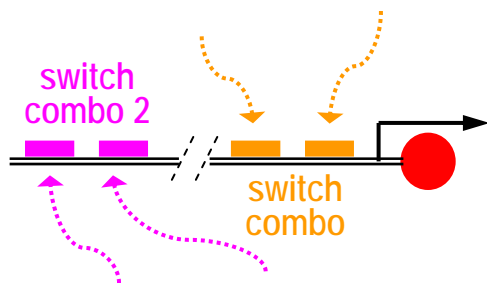
- ✓ developmental genes are broadly organized in tiers, or "generations": earlier genes map the way for later genes
- ✓ gene expression propagates in a directed fashion: first, positional morphogens create domains, then domains intersect



From feedforward to recurrent gene regulation

➤ Naturally, toolkit genes are often multivalent

- ✓ exception to the feedforward paradigm: “toolkit” genes that are reused at different stages and different places in the organism
- ✓ however, a toolkit gene is triggered by different switch combos, which can be represented by duplicate nodes in different tiers

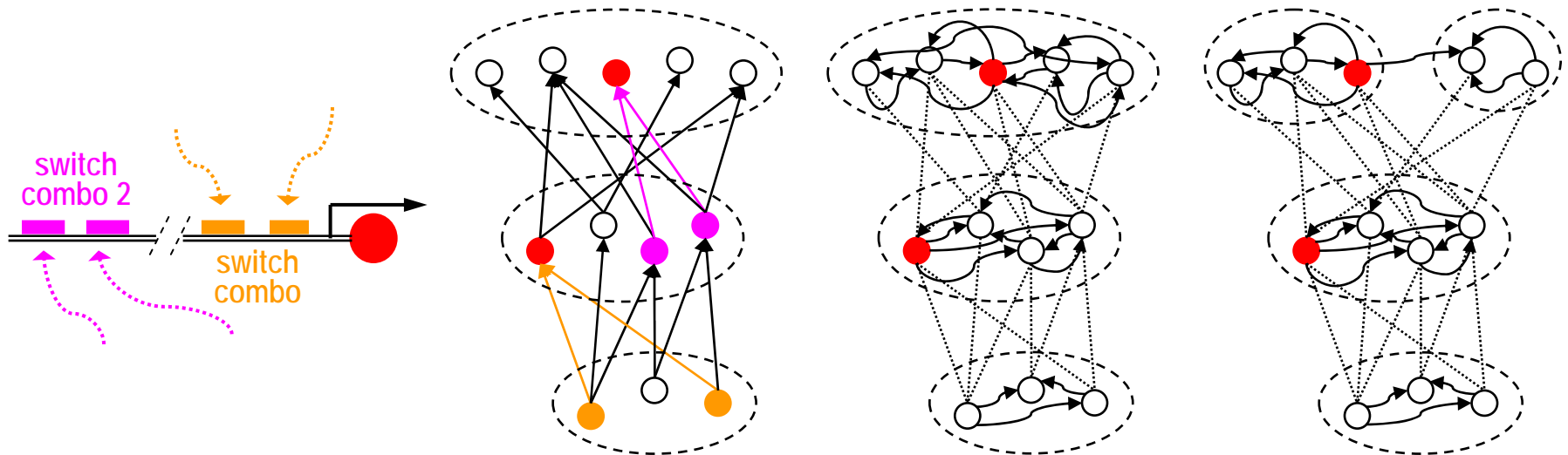


after David Kingsley, in Carroll, S. B. (2005)
Endless Forms Most Beautiful, p125

From feedforward to recurrent gene regulation

➤ More realistic variants of GRNs

- ✓ add recurrent links within tiers → domains are not established independently but influence and sharpen each other
- ✓ subdivide tiers into subnetworks → this creates **modules** that can be reused and starts a hierarchical architecture



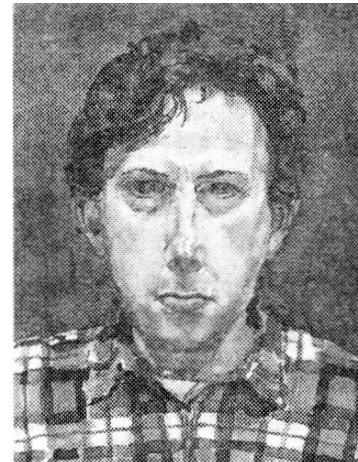
Hierarchical morphogenesis

➤ Morphological refinement by iterative growth

- ✓ details are not created in one shot, but gradually added. . .

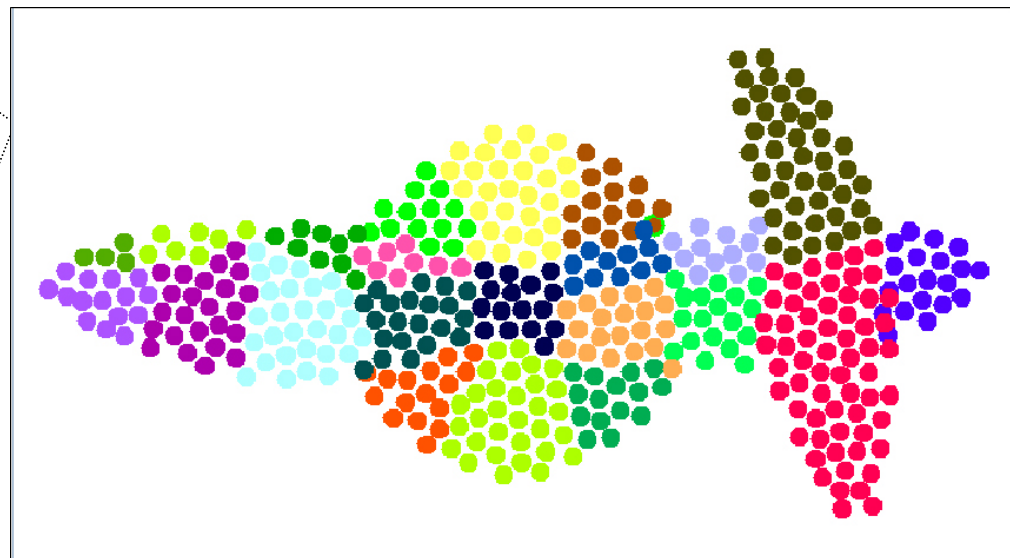
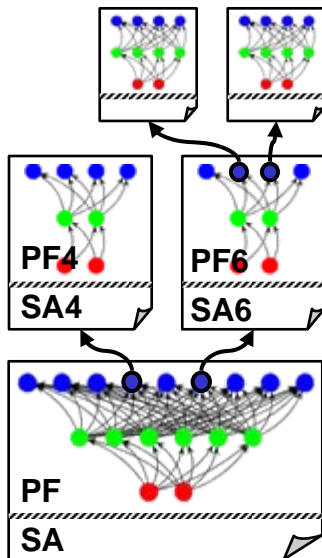
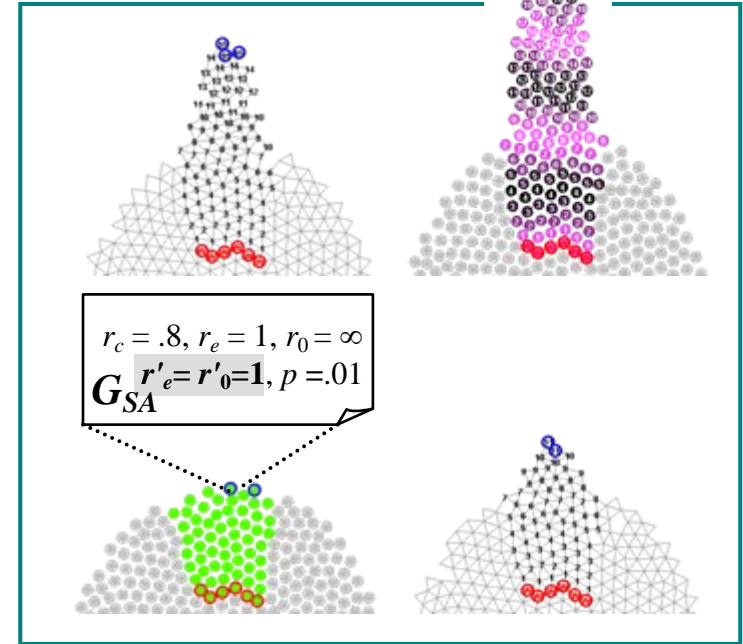
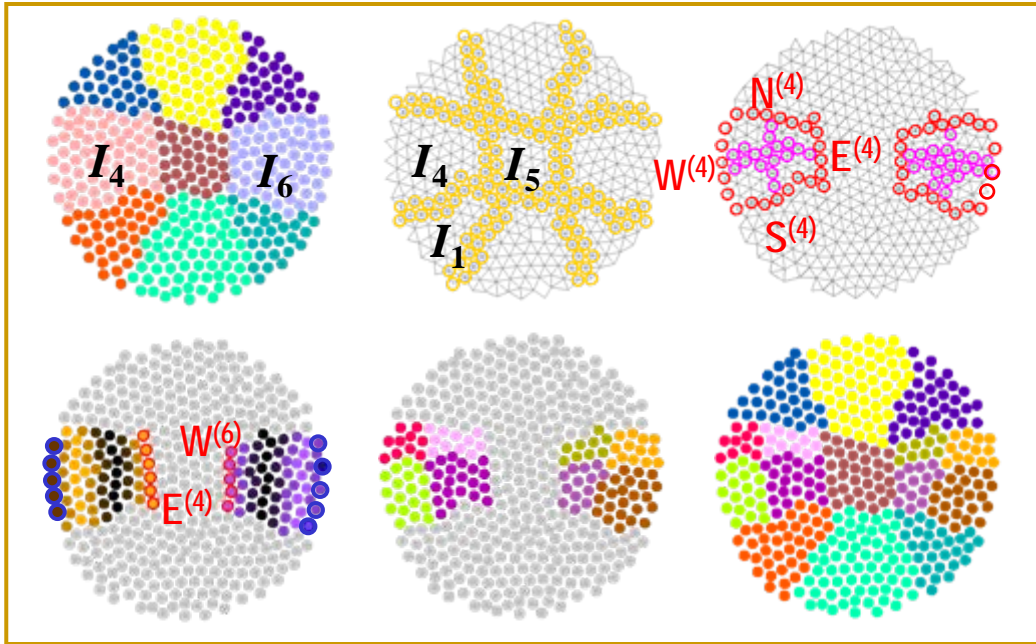


- ✓ . . . while, at the same time, the canvas grows



from Coen, E. (2000)
The Art of Genes, pp131-135

Hierarchical morphogenesis



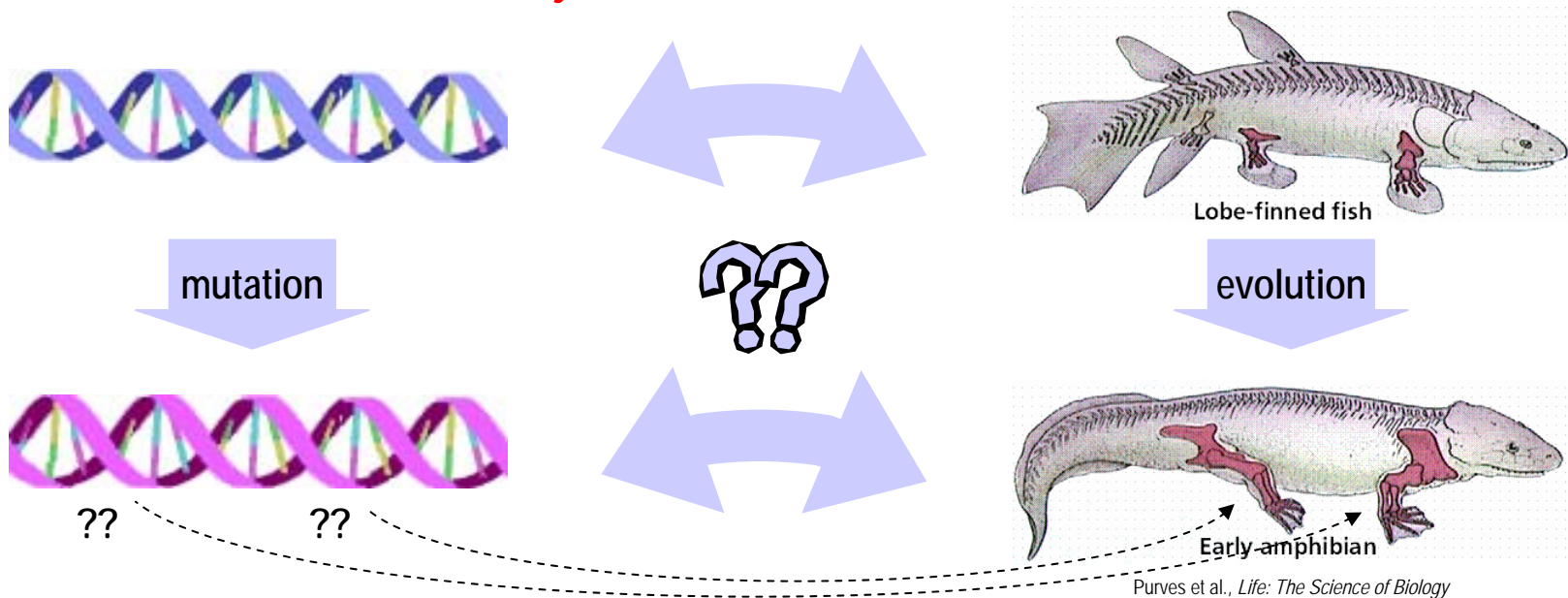
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4. Evolutionary development (evo-devo)

Evolutionary development (evo-devo)

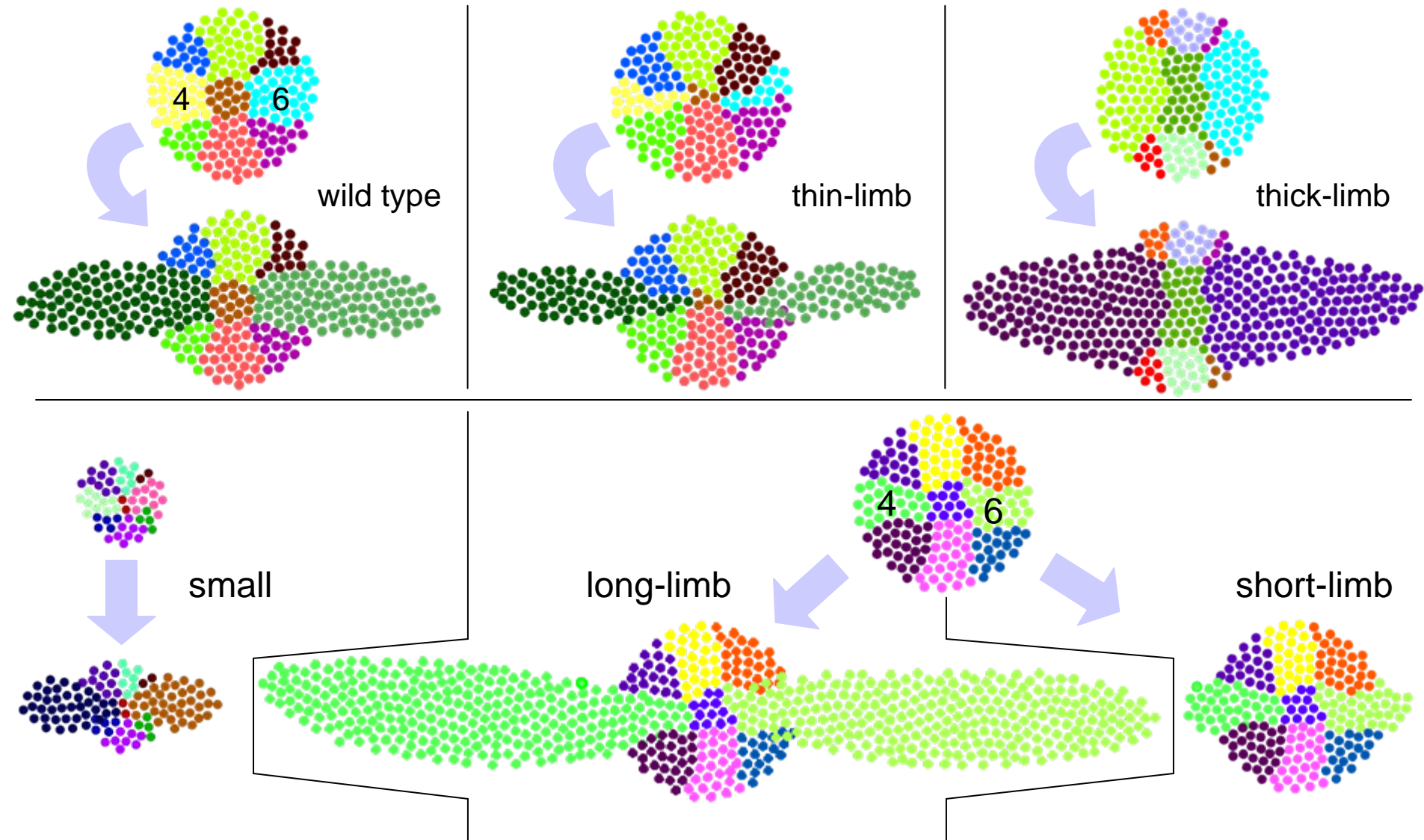
➤ Development: the missing link of the Modern Synthesis

- ✓ biology's "Modern Synthesis" demonstrated a fundamental correlation between genotype and phenotype, yet the molecular and cellular mechanisms of development are still unclear
- ✓ the genotype-phenotype link cannot remain an abstraction if we want to understand evolution as *producing innovation by variation* and not just as a selection force



Multi-agent evolutionary development (evo-devo)

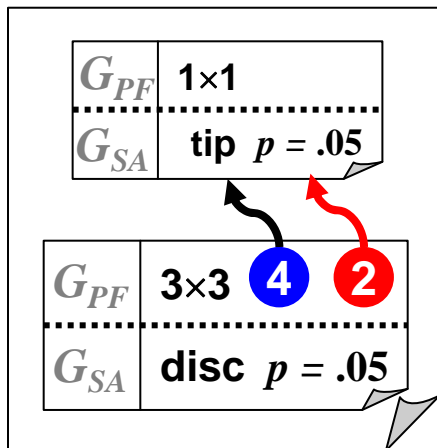
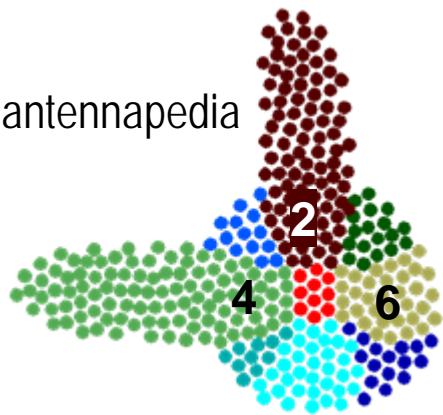
➤ Genotype mutations → phenotype variations (*quantitative*)



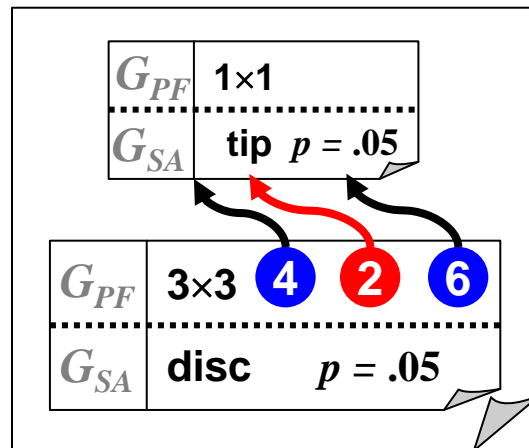
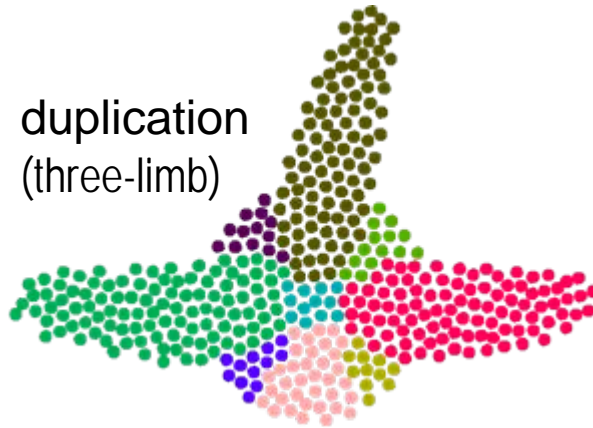
Multi-agent evolutionary development (evo-devo)

➤ Genotype mutations → phenotype variations (*qualitative*)

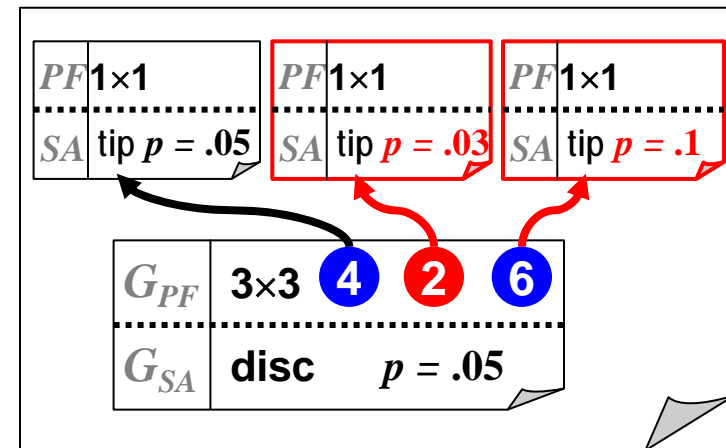
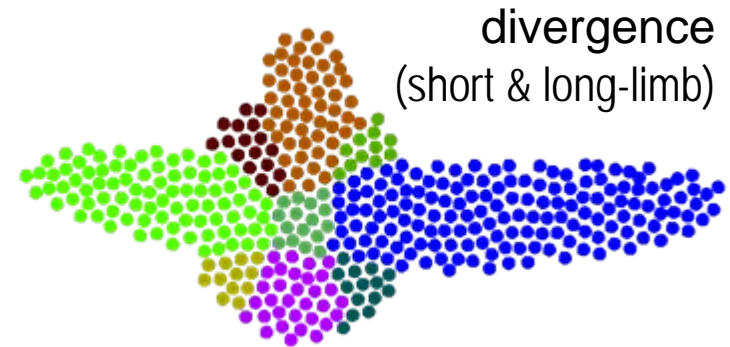
antennapedia



homology by duplication

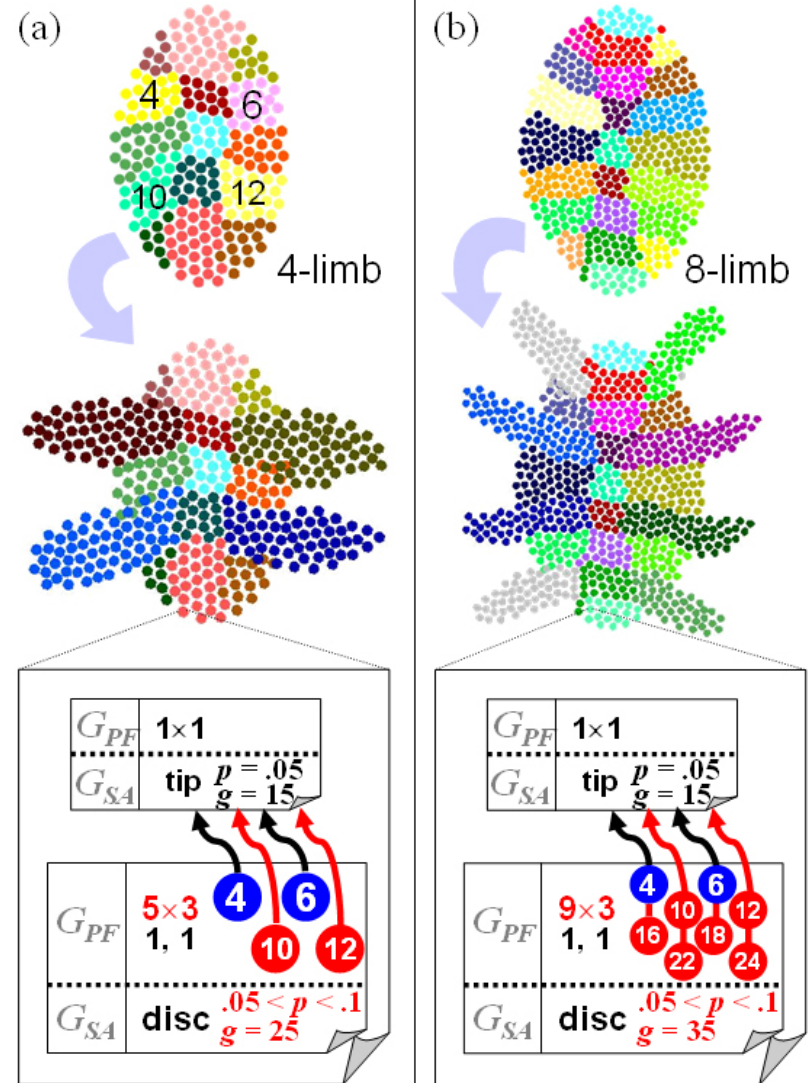
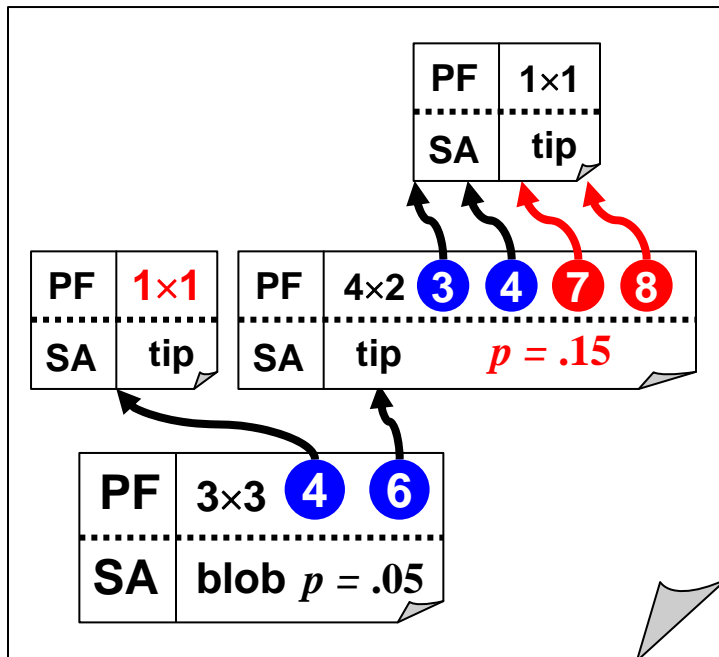
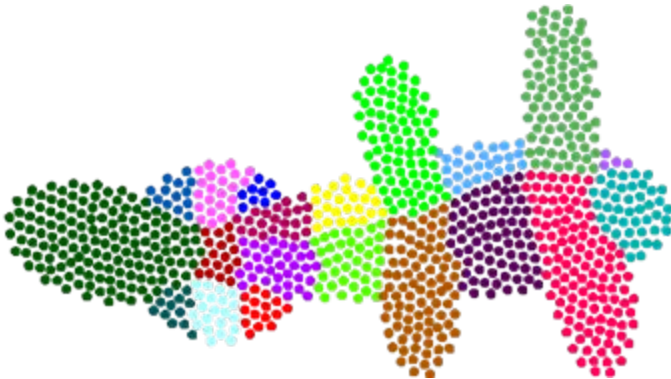


divergence of the homology



Multi-agent evolutionary development (evo-devo)

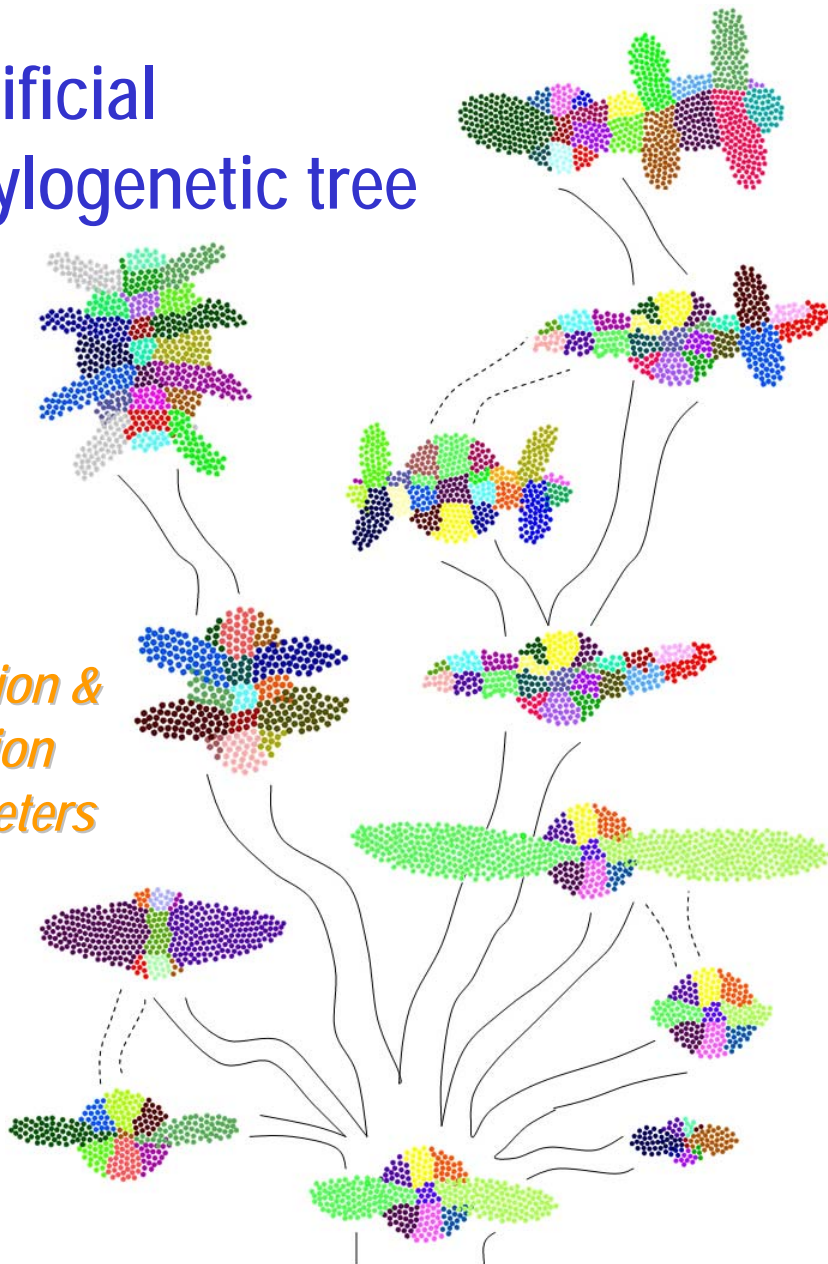
- Genotype mutations → phenotype variations (*qualitative*)



Multi-agent evolutionary development (evo-devo)

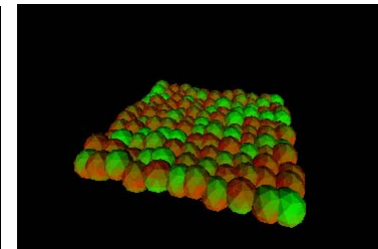
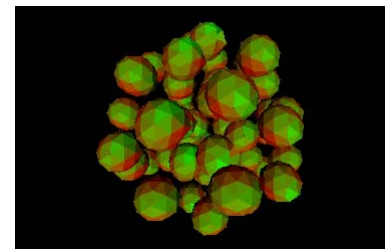
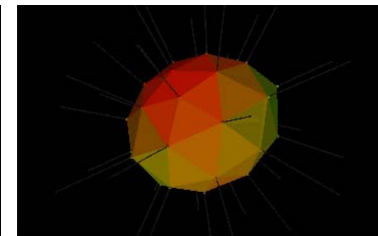
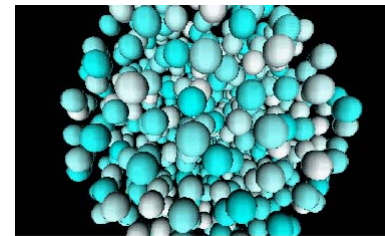
➤ Artificial phylogenetic tree

optimization & validation of parameters



future directions:

- better biomechanics (3D) :
cytoskeleton, migration
- better gene regulation



The self-made puzzle of embryogenesis

1. Self-organized and structured systems
2. Two-side challenge: heterogeneous motion / moving patterns
3. A multi-agent model of embryogenesis
4. Evolutionary development (evo-devo)