

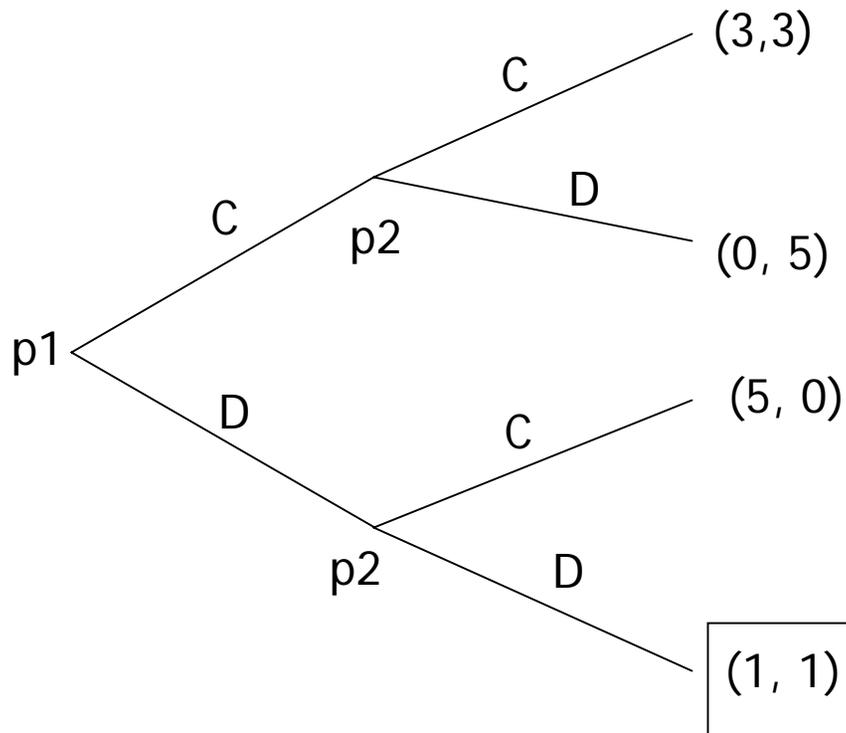
# Iterated Prisoner's Dilemma

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CS 790R — Spring 2005

presented by Jeff Wallace

# Extended Form



- imperfect information
- Nash equilibrium
- backward induction finds (1,1)

# Single Iteration

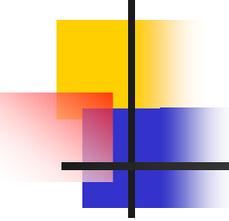
p2 p1	<b>C</b>	<b>D</b>
<b>C</b>	(3,3)	(5,0)*
<b>D</b>	*(5,0)	<b>*(1,1)*</b>

- matrix view
- hold one player's move constant and mark choice with \*
- one perfect NE

# One Iteration – General Form

$p_2$ p1	<b>C</b>	<b>D</b>
<b>C</b>	(R,R)	(S,T)*
<b>D</b>	*(T,S)	*(P,P)*

- dilemma where  $T > R > P > S$  and  $2R > T + S$
- $(R, S, T, P) = (3, 0, 5, 1)$   
or  $(1, 0, \frac{5}{3}, \frac{1}{3})$
- aka  $(p, q) = (\frac{5}{3}, \frac{1}{3})$

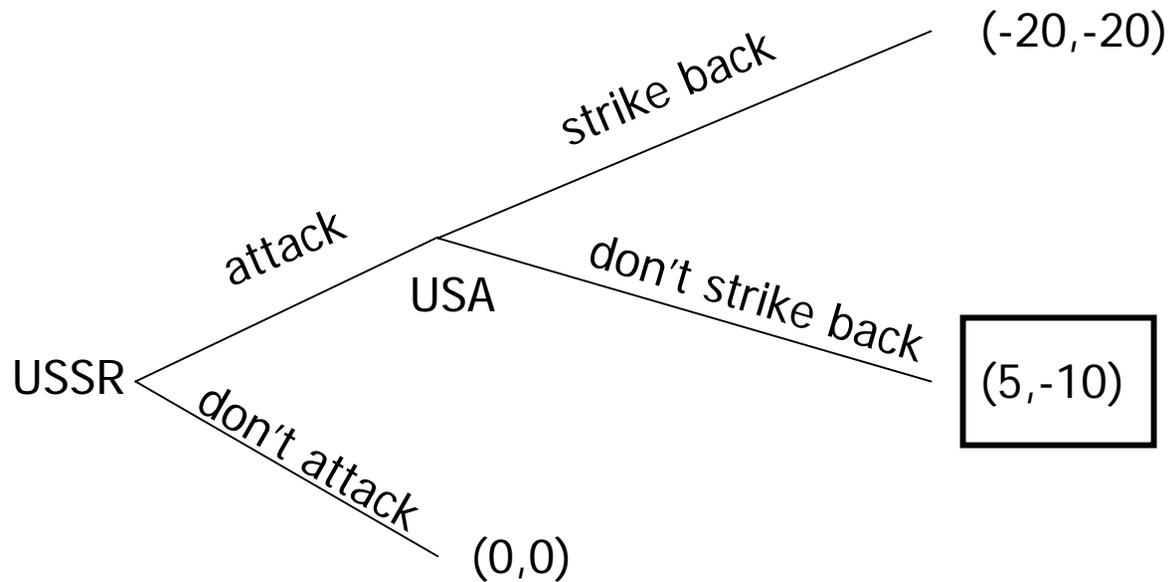


# Requirements for NE

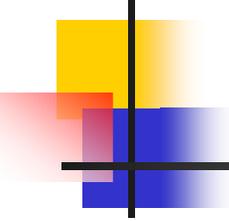
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- Reinforcement of beliefs: players believe they know how other will play, which is self-enforcing
- No incentive for “do over.” Players are rational.

# Payoffs Dictate Equilibriums



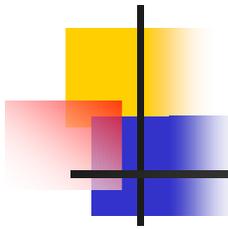
- nuclear holocaust “game” of the cold war
- why didn't the perfect NE occur?



# Iterated Prisoner's Dilemma

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- Extended form (view from Elmo device)
- Backwards induction shows one perfect NE resulting from 'DD', with average payoff =  $(1,1)$
- Proof: if either player deviates, he earns zero at each step, therefore there's no incentive to deviate?

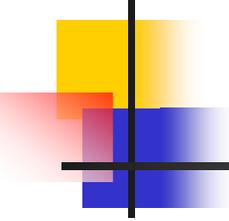


# Iterated PD (CONT'D)

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What about...

- Play 'C' in period 1, then keep playing 'C' in subsequent periods until p2 plays 'D'. Thereafter, play 'D'. Same for p2.
  - this gives outcome C-C, C-C, ..., C-C with average payoff = (3,3). It's another NE!
  - proof: can either player deviate? A: no, because if p1 plays 'D', p2 will switch to 'D' forever, leading to long-term avg payoff = (1,1). P2 can't deviate for same reason.



# Iterated PD (CONT'D)

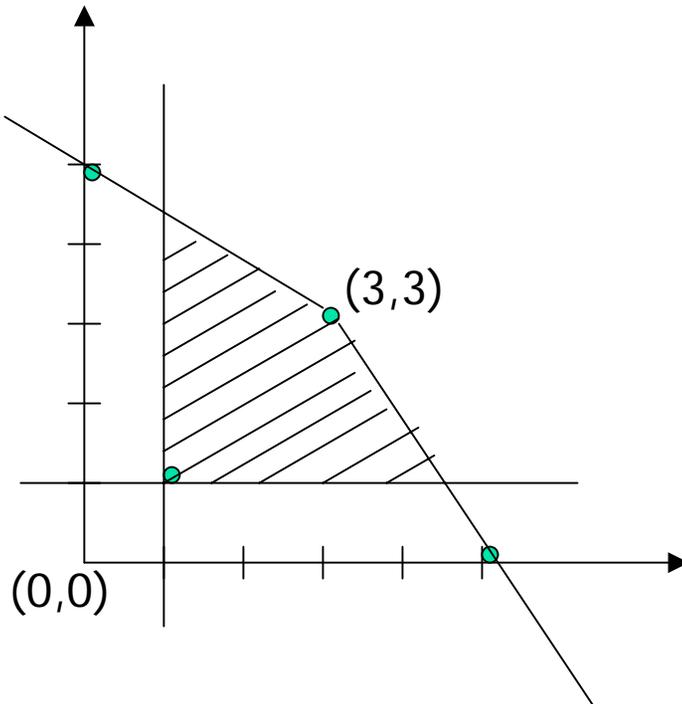
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What about...

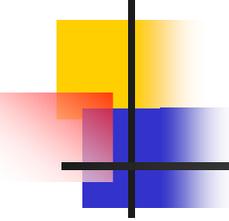
- Play C,D,C,D...as long as opponent plays same. If opponent deviates, play 'D' forever.
  - this gives outcome C-C, D-D,... with average payoff =  $(2,2)$ . It's another NE!
  - proof: can either player deviate? A: no. Same reasons as before.

# Individually Rational Zone

- Convex hull within which players get at least  $(1,1)$ .



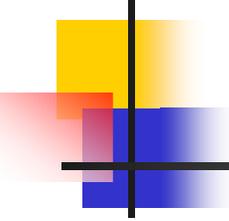
- Infinite number of NEs within IRZ
- this leads to mixed strategies as NE (demonstrate mixed strat on board)



# TFT is a Mixed Strategy

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- Ex. C-C, C-C, D-C, C-D, C-C, ...
  - Result =  $(3,3) + (3,3) + (5,0) + (0,5) + (3,3) =$
  - average payoff =  $(2 \frac{4}{5}, 2 \frac{4}{5})$
  - This is within IRZ (convex hull)
- PAV strategy is similar. It also lies within IRZ



# Other Mixed Strategy Results

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- ALL-D approaches (1,1) and is therefore eventually self-destructive. It almost gets wiped out. "Good parasite, but needs a healthy host."
- RAND is overcome by "nice" strategies.
- TFT dominates in environments without noise, but PAV dominates with noise.
- ALL-C marginally survives without noise, but becomes extinct with noise.